# MIXED QUANTUM-CLASSICAL SIMULATIONS ON MODEL DONOR-BRIDGE-ACCEPTOR TRIADS 

A Dissertation Presented to the Faculty of the Department of Chemistry University of Houston

In Partial Fulfillment of the Requirements for the Degree

Doctor of Philosophy

By
Kush Patel
August 2019

# MIXED QUANTUM-CLASSICAL SIMULATIONS ON MODEL DONOR-BRIDGE-ACCEPTOR TRIADS 

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## Abstract

Marcus theory predicts electron transfer rates between donor and acceptor systems. Since its inception in the 1950's, this theory has been widely applied to topics in many disciplines and has become an instrumental model in describing the efficiencies of photovoltaics. A key aspect of this theory requires knowledge of the nuclear reorganization of system and solvent alike and computation of energies associated with such nuclear motions is often difficult or impossible for systems with large number of degrees of freedom. We develop here a mixed quantum mechanical/molecular dynamics model to investigate charge transfer dynamics in a set of large organic Donor-Bridge-Acceptor triad molecules. Specifically, we are interested in the differences in electron and nuclear behavior relating to small changes in the molecular makeup of Carotenoid-Porphyrin-Fullerene triads.

Our model approximates excitation energies on the order of 1.9 eV which agrees with absorption spectra for these triads and isolated porhyrins. Via electron population analysis, we monitor charge migration to the acceptor in time. Approximations of the charge transfer rates reveal ultrafast (picosecond scale) electron dynamics consistent with experimental literature. We then correlate nuclear dynamics with the charge transfer process using the Short-Time Fourier Transform technique. Broadly, the porphyrins undergo higher energy vibrations, whereas the fullerenes see low energy modes. Aryl side groups exhibit torsional motions relative to the porphyrin. Aryl linkers between bridge and acceptor are restricted from such motions and therefore express ring distortion modes. Finally, we find an amide linker mode that is directionally sensitive to electron motion.

This work supports the notion of vibrationally coupled ultrafast charge transfer found in both experimental and theoretical studies and lays a foundational method for identifying key vibrational modes for parameterizing future theoretical models.

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## Chapter 1

## Introduction

In the mid-1950s, Rudolph Marcus published what would become the standard model for predicting rate constants in electron transfer (ET) mechanisms[1, 2]. In his originating work, he considers the self-exchange reaction between pairs of small Iron and Magnesium complexes. In particular, he wanted to reconcile the Franck-Condon Principle (FCP) and energy conservation in the context of these nonradiative reductionoxidation reactions[3]. Under the FCP, an electron would jump from one ion to another instantaneously without an immediate response from slower nuclei. The resulting products are the same two ions $\left(\mathrm{Fe}^{2+}+\mathrm{Fe}^{3+} \rightleftharpoons \mathrm{Fe}^{3+}+\mathrm{Fe}^{2+}\right)$, but each ion is now in a foreign, non-equilibrium environment. With larger ionic complexes, the change in the local electric fields is smaller after electron transfer, eliciting less response from the solvent. However, the nature of the bond between metal ion and ligand changes, and this becomes the foreign environment. Nuclear coordinates and their coupling to the electronic state are, therefore, an integral part of the potential energy description.

While the original work focused on small metal ions and complexes, the resulting


Figure 1.1: Selection of topics related to electron transfer. Reproduced with permission from Springer Science and Bus Media B V.
theory is widely predictive in many current topics as electron transfer is at the heart of the vast majority of chemical and biochemical processes. Figure 1.1 depicts a small subset of related topics and illustrates the ubiquity of this theory.

Marcus aimed to describe the rate of ET in the Arrhenius (kinetic) sense, $k \propto$ $e^{-\Delta G^{\ddagger} / R T}$. Here, $\Delta G^{\ddagger}$ is the activation energy between an initial and final electronic state. Figure 1.2 plots the parabolic form ( $2^{\text {nd }}$ order Taylor expansion) of the free energy surfaces along a single normal coordinate for such states. With this approximation, one can relate the activation energy to two parameters, $\lambda$ and $\Delta G^{0}$. With exponential prefactor from the Fermi Golden Rule, one can then elegantly write the
transition rate as

$$
\begin{equation*}
k_{E T}=\frac{2 \pi|V|^{2}}{\hbar} \frac{1}{\sqrt{4 \pi \lambda k_{B} T}} \exp \left[-\frac{\left(\Delta G^{0}+\lambda\right)^{2}}{4 \lambda k_{B} T}\right] \tag{1.1}
\end{equation*}
$$

where $V$ is the electronic coupling between the initial and final states; $\lambda$ is the reorganization energy associated with the nuclear relaxation from the minima of the first state to the minimum of the final state along the surface of the final state; and $\Delta G^{0}$ is the free energy offset (driving force) between the states. The reorganization energy term includes both the rearrangement of the ions of interest and solvent molecule reorientation as a result of the redistribution of charge. Many experimental comparisons highlight the predictive power of this theory[4], and it remains as a comparison point for new theoretical models $[5,6,7]$.

The Gaussian-like exponential term dictates that the rate is maximal, for a given $V$, when $-\Delta G^{0}=\lambda$. Most electron transfer reactions lie within the normal Marcus regime, where $-\Delta G^{0}<\lambda$, as depicted in Figure 1.2. For $-\Delta G^{0}>\lambda$, this is the inverted regime. In this region, while the driving force becomes increasingly favorable, the wavefunction overlap between the considered states vanishes, and therefore reaction rate drops[8]. Evidence of this case was found 30 years later by Miller and coworkers[9].

While it is possible to compute $\Delta G, \lambda$, and $V$ in smaller or ordered systems, the task becomes much more formidable when considering large or non-rigid systems. Computation of $\Delta G^{0}$ and $\lambda$ require not only geometry optimization and energy calculations for the ground state, but also those for multiple excited states, which are significantly more involved. One can approximate such parameters from diabatic surfaces, but they are not uniquely defined. One can uniquely define the adiabatic


Reaction Coordinate / a.b.u.
Figure 1.2: Schematic representation of Marcus electron transfer theory. Parabolas represent the energy surfaces of the initial (blue) and final (orange) states with respect to an arbitrary reaction coordinate, where the minima correspond to an equilibrium geometry. Terms depicted are $\Delta G^{0}$, the free energy offset, and $\lambda$, the reorganization energy.


Figure 1.3: Schematic figure of adiabatic (blue) potentials surfaces (arbitrary energy unit) as a function of arbitrary coordinate $q$. These are one dimensional cross-sections of an otherwise high dimensional coordinate space. (Top) Adiabatic surfaces plotted with resulting diabatic surfaces (orange). (Bottom, left) Adibatic potentials under strong coupling regime. (Bottom, right) Adiabatic potentials in weak coupling regime.
potentials along a given nuclear coordinate via Born-Oppenheimer Approximation

$$
\begin{equation*}
V_{n}(R)=\left\langle\psi_{n}(q)\right| \mathcal{H}_{e l}(q)\left|\psi_{n}(q)\right\rangle \tag{1.2}
\end{equation*}
$$

giving rise to a series of potentials $V_{n}(q)$ visualized in Figure 1.3. Such potentials may come arbitrarily close but will not cross, unless allowed by symmetry.

Diabatization involves assuming that away from the avoided crossing, each adiabatic state can be written as a linear combination of some other states such that in this basis

$$
\mathcal{H}=\left(\begin{array}{cc}
E_{A}(q) & V_{A B}  \tag{1.3}\\
V_{A B} & E_{B}(q)
\end{array}\right)
$$

and the eigenvalues of $\mathcal{H}$ are the same as those of the Born-Oppenheimer Hamiltonian. $E_{A}(q)$ and $E_{B}(q)$ are the "diabatic" potentials. So long as $\left|E_{A}-E_{B}\right|>2 V_{A B}$, the diabatic potentials provide a robust and accurate description. In this limit, a perturbative expansion of the states in terms of $\frac{V_{A B}}{\left|E_{A}-E_{B}\right|}$ converges rapidly. However, close to the avoided crossing, the diabatic states become strongly mixed and perturbation theory is no longer valid.

Furthermore, free energy surfaces are not dependent on merely one dimension or normal coordinate as pictured; they are multivariate with respect to the system under study. Nevertheless, if these obstacles can be overcome, this theory remains not only viable for determining electron transfer rates for inorganic, organometallic, and organic molecules but stands as a comparison point for new models $[4,5,6,7]$. The reorganization energy encapsulates any nuclear dynamics that occur as a result of changes in the electronic state. As the term is a significant factor this description of electron transfer, identifying which normal coordinates of a given system are significant to the transition will not only give insight into better molecular construction but can also reduce the number of degrees of freedom considered in models.

### 1.1 Vibronic Transitions

Each electronic state contains numerous vibrational levels, which in turn contain rotational levels. Often, these rotational degrees of freedom are ignored as their energy scale is negligible in the context of electronic energies. A description of these vibrational states can be derived from first assuming the Born-Oppenheimer approximation (electronic and nuclear degrees of freedom can be separated).

$$
\begin{equation*}
\left|\Psi_{\text {total }}\right\rangle=\left|\Psi_{\text {elec }}\right\rangle \otimes\left|\Psi_{\text {nuc }}\right\rangle \tag{1.4}
\end{equation*}
$$

The Franck-Condon Principle then assumes nuclear motion is slow compared to electron motion and therefore photoexcitations are instantaneous relative to nuclear motion. Thus, a transition probability can be calculated:

$$
\begin{equation*}
\left.\left.P_{f \leftarrow i}=\left|\left\langle\Psi_{\text {total }}^{f}\right| \hat{\mu}\right| \Psi_{\text {total }}^{i}\right\rangle\left.\right|^{2}=\left|\left\langle\Psi_{\text {nuc }}^{f} \mid \Psi_{\text {nuc }}^{i}\right\rangle\right|^{2}\left|\left\langle\Psi_{\text {elec }}^{f}\right| \hat{\mu}\right| \Psi_{\text {elec }}^{i}\right\rangle\left.\right|^{2} \tag{1.5}
\end{equation*}
$$

where $\hat{\mu}$ is the dipole operator. The probability has dependence on the nuclear wavefunction and only with significant overlap can the transition occur.

Figure 1.4 plots a pair of displaced harmonic oscillators. In this example, the ground state vibrational mode has overlap with the fourth vibrational overtone of the excited state. The spectral amplitude for electronic transitions depends on this amplitude of the overlap. Note, that between the two electronic states, the energy minima are at two different normal mode coordinates. The final state resulting from the electronic transition begins at a nonequilibrium geometry with some vibrational energy, hence, the portmanteau "vibronic".

Following electronic excitation, the system can then vibrationally relax. When the wavefunction of a lower vibrational state has significant overlap with another in the electronic ground state, the system can emit a photon and electronically relax. The outgoing photon is of less energy than the initial excitation input energy (fluorescence). However, the system need not always electronically relax with photoemission. If there is significant wavefunction overlap with a different excited electronic state, the system can relax nonradiatively (Figure 1.2). The new excited state will likely have a different equilibrium nuclear configuration and electronic wavefunction distribution such that the electron density may be localized in a different spatial region (charge transfer), as discussed previously. This nonradiative transition is very much in line with the work of Marcus and an accurate description faces the same challenges. Where two electronic states coincide, electronic coupling becomes large and


Normal Coordinate / (a.b.u.)
Figure 1.4: Schematic diagram of a vertical transition between a ground state (blue) and excited state (orange). Parabolic curves represent the potential energy surface of the respective electronic states. Strata within the parabolic curves are the amplitudes of the vibrational wavefunctions.
the Born-Oppenheimer approximation breaks down.

The Fewest Switches Surface Hopping (FSSH) method approaches electronic transitions from a dynamics perspective[10]. Within this method, multiple adiabatic states are propagated via the time-dependent Shrödigner equation and the system is in exactly one of these states at any given time. The system can hop to another adiabatic state with a probability computed from the electronic coupling between its current state and some other adiabatic state. An ensemble of propagated trajectories averages out the random aspect of "choosing" to hop against a probability. Adjusting nuclear velocities following a hop conserves angular momenta and total energy. Nuclei are purely classical, responding to mean-field potential (Ehrenfest[11] dynamics), and therefore no vibrational wavefunction overlap is considered for the purposes of electronic transitions. The original proposition of this method accurately described a collision reaction between $\mathrm{H}^{+}$and $\mathrm{D}_{2}[12]$. Further developments apply more rigorous considerations, namely towards the ad hoc nuclear momentum rescaling and lack of quantum decoherence treatment $[13,14,15,16,17]$. FSSH and related methods have been applied to model electronic transitions in larger systems reproducing experimental results and, in some cases, with better accuracy than exact quantum mechanical calculations $[18,19]$. FSSH is not entirely without faults, however. Large coupling value relative to the energy difference between two electronic states drives up the switching probability. In systems where low-lying states are densely packed, trajectories will rapidly hop about these surfaces, leading to unphysical results.

### 1.2 Charge Transfer in Organic Semiconductors

As the looming threat of global warming and climate change begins to manifest, the need to undo global energy dependence on fossil fuels and non-renewable energy sources becomes increasingly apparent. Solar energy is a viable alternative as there is enough radiation to power human energy consumption many-fold[20]. It becomes a crucial task, then, to understand the optoelectronic properties of photoactive materials and optimize their construction. In particular, comprehensive knowledge of electron/energy transfer in such materials lays a strong foundation towards this end. As such, the charge transfer problem has been the subject of an enormous amount of effort in well over the last half-century, including the works of many Nobel laureates.

Figure 1.5 shows the progress towards high photoconversion efficiency for various kinds of photovoltaic materials. The current record holders are multi-junction inorganic photovoltaics that now boast up to $46 \%$ photoconversion efficiency. These materials, however, often require caustic components and are costly to produce. On the lower side of the efficiency chart, the organic semiconductors have enjoyed two decades of growth, reaching just over $16 \%$ efficiency[21]. Despite this difference in efficacy, organic photovoltaics (OPV's) have many desirable properties. Namely, they are significantly cheaper and easier to produce, and the amorphous nature of the active photovoltaic layer lends to flexible devices suitable for applications on even non-rigid surfaces. Furthermore, vast knowledge of synthetic organic chemistry affords polymer scientists an enormous variation in cell construction. The efficiency of OPV's relies on the successful transfer of photoexcited electrons across the active layer. Complex morphology of most OPV's and their low dielectric constants make this a non-trivial phenomenon.


Figure 1.5: Photovoltaic efficiencies by material class in time collected by National Renewable Energy Laboratory. Figure current as of June 2019. Image courtesy of NREL[22].

### 1.2.1 The Bulk Heterojunction

Figure 1.6 depicts the cross-section of an OPV cell. At the top sits a glass layer which allows light to travel in. Sandwiched between two electrode layers (gray) is the active layer consisting of separated donor and acceptor phases. In an OPV of this type, a photon will excite an electron in the donor or acceptor phase generally forming a Frenkel exciton (a tightly bound electron and hole pair on the same molecule) or charge transfer exciton (electron and hole are on different molecules, yet Coulombically bound). This exciton will either undergo recombination (radiative for singlet excitons, nonradiative for triplet) back to the ground state or dissociate into a loosely bound electron-hole pair wherein the electron finds itself in the acceptor phase and its positively charged vacancy in the donor phase. These separated charges eventually migrate to opposite electrodes generating current. Binding energies for these excitons range between $\sim 0-1 \mathrm{eV}[23]$. This interaction is particularly strong relative to inorganic semiconductors as a result of the low dielectric constant of organic media, making the separation process all the more difficult. This binding energy must be overcome by the combination of ambient thermal energy and energetic offset of the acceptor and donor materials.

Characterizing these electron dynamics provides insight into the photophysical properties of the semiconducting material and may lead to the design of improved or novel materials. However, it is exceptionally difficult to atomistically simulate the optoelectronic properties of a full-scale bulk heterojunction given that modern quantum computational techniques increase exponentially with system size ${ }^{1}$. The energetic offset between acceptor and donor materials constitutes the driving force for charge

[^0]

Figure 1.6: Depiction of an organic photovoltaic device. Blue and orange represent donor and acceptor phases of the bulk heterojunction.
separation and, therefore, one can simplify the problem by studying interactions at the interface between semiconductor phases.

Previous work by Kelley, Patel, and Bittner used a mixed quantum mechanical/molecular mechanics approach model a PPV:PCMB bulk heterojunction in which preselected interfacial molecules were determined to be "quantum active" leaving the remaining molecules treated as a classical solvent[24]. By "quantum active", we mean $\pi$ electrons of this subset of molecules are treated quantum mechanically and the rest treated with force fields. Our simulations describe that low lying excited states form a dense band spanning about 0.5 eV ; as previously discussed, FSSH under this scenario undergoes rapid switching between propagated surfaces producing unphysical results. We show, via Fourier Transform of bandgap time-series, that excitation energy is modulated by lower energy torsional modes, mid-range $\mathrm{C}=\mathrm{C}$ bond stretching, and, to a lesser extent, high energy C-H modes. Such vibrations, though perhaps only weakly coupled to electronic states, provide enough energetic overlap between electronic states such that rapid transitions occur between excitonic, charge transfer, and (long-range) charge-separated state.

In general, an excitation can occur in any molecular phase of the system. Photoexcitation of the donor requires subsequent migration of the excited electrons to the acceptor along LUMO orbitals to form the CT state. In contrast, photoexcitation of the acceptor should be followed by hole migration to the donor through HOMO orbitals. In certain model systems, charge transfer can be mediated by a bridge moiety. Large energetic offset decreases overlap between donor and acceptor states. However, bridge states provide both intermediate energetic and spatial pathways for much more efficient electron transfer. Distortions arising from vibrations, solvent effects, or other


Figure 1.7: Schematic representation of orbital energies for each moiety. Initial excitation is represented as a promotion of an electron from bridge HOMO to LUMO. Dark arrows represent subsequent electron transfer processes resulting in the final charge transfer state. Vibrational strata provide accessible higher energy states the energetic proximity helps facilitates electronic transitions.
noise fluctuate the energy differences between these states and alter the charge transfer rate as a consequence. Figure 1.7 depicts an alternative sequence of the charge transfer mechanism wherein a bridge electron is excited, followed by two localized transitions: bridge to acceptor along LUMO's and donor to bridge along HOMO's. We discussed such models in the proceeding subsection.

### 1.2.2 Artificial Photosynthesis

Additionally, one can look to nature for inspiration for another solar energy conversion method. For billions of years, phototrophic lifeforms have used light as the primary source of energy to drive anabolic processes. Photosynthesis is initiated by photoabsorption in the light-harvesting complex (LHC). Figure 1.8 depicts the structure of light-harvesting complex I (LH-I) and the reaction center (RC) of purple bacteria[25]. Within LH-I, 32 bacteriochlorophyll (BChl, green square with yellow carotenoid tail) absorb light and funnel the excitation energy to the RC encompassed within.


Figure 1.8: Structure of the LH-I-RC complex. (a) Side view of the LH-I-RC complex with three LH-I $\alpha \beta$-heterodimers on the front side removed to expose the RC in the interior. The $\alpha$-helices are represented as cylinders with the $\mathrm{L}, \mathrm{M}$, and H subunits of the RC in yellow, red, and gray, and the $\alpha$-apoprotein and the $\beta$-apoprotein of the LH-I in blue and magenta. BChls and bacteriopheophytins are represented as green and yellow squares, respectively. Carotenoids (spheroidenes) in a yellow licorice representation, and quinone $\mathrm{Q}_{B}$ is rendered by gray van der Waals spheres. $\mathrm{Q}_{B}$ shuttles in and out (as $\left.\mathrm{Q}_{B} \mathrm{H}_{2}\right)$ of the LH-I-RC complex. (b) Arrangement of BChls in the LH-I-RC complex. The BChls are represented as squares with B875 BChls of LH-I in green, and the special pair ( $\mathrm{P}_{A}$ and $\mathrm{P}_{B}$ ) and the accessory BChls ( $\mathrm{B}_{A}$ and $\mathrm{B}_{B}$ ) of the RC in red and blue, respectively; cyan bars represent the $\mathrm{Q}_{y}$ transition moments of BChls.[25] Image courtesy of National Academy of Sciences. Copyright (1998) National Academy of Sciences, U.S.A.

However, this complex does not sufficiently collect enough light alone and requires antennae in the form of light-harvesting complex II (LH-II) and, in some bacteria, light-harvesting complex III (LH-III)[26, 27, 28, 29]. LH-II and LH-III are structurally similar to LH-I but contain less BChl units and have no reaction center. Each LH-I complex can be surrounded by up to ten LH-II antennae with the exact ratio depending on the bacteria itself and growth conditions[30]. Absorption studies of these LH complexes have found that LH-III absorbs at higher energies than LH-II, which in turn absorbs at higher energy than LH-I. The succession of energies drives photoexcitation energy from LH-III through LH-II to LH-I[31] and finally ending at a pair of strongly interacting BChls (red squares in Figure 1.8(b)) in the RC. This final pair, termed the special pair, drives the high energy electron into quinone acceptors. In purple bacteria, the system recovers the lost electron from the oxidation of $\mathrm{H}_{2}$, elemental sulfur, or sulfur compounds, completing the electron processes in Photosystem II. In cyanobacteria and higher plants, the process concludes with the oxidation and splitting of water.

Scientists have long since attempted to understand and replicate the photophysical processes occurring within photosynthetic bacteria. Efficient splitting of water provides a viable means of hydrogen production for energy storage. Three key factors have been identified for developing artificial reaction centers. Systems must (1) have quantum yield near unity, (2) have slow recombination rates, and (3) store large amounts of energy[32].

The final electron transfer reaction in Photosystem II (special pair to quinone transfer) precedes the water-splitting step and is therefore an important precursor process to study. The photosynthetic complex fixes the special pair into optimal positions for electron transfer to bound quinones. For experimental study, porphyrin


Figure 1.9: Basic construction of the Donor-Bridge-Acceptor triad composed of a carotenoid donor (blue), porphyrin bridge (red), and fullerene (green) derivative acceptor (green). Alternative structures include addition of side groups to the porphyrin in $\beta$ or meso positions, increasing distance between subunits via methylene units, or a different fullerene derivative.
molecules are photophysically similar to Bchl, but have the added benefit of facile synthesis and stability. Thus, early models considered covalently bound porphyrin and quinone $[33,34]$.

Tom and Anna Moore and coworkers have experimentally investigated a wide array of dyads (donor/acceptor) and triads (donor/bridge/acceptor) that mimic the photosynthetic processes of bacterial light harvesters[35, 36, 37, 38, 39, 40, 41, 42, 43]. They have shown that porphyrin-quinone and porphyrin- $C_{60}$ dyad systems can maintain charge separation for time scales up to hundreds of picoseconds[37, 40]. The addition of a carotenoid polyene moiety increases lifetimes, in some cases by three orders of magnitude, by increasing the physical separation of the charges. A readily detectable transient absorption band of the carotenoid radical cation[44] and large detected dipole moment[42] support this claim.

Triadic systems of this design undergo a multistep electron transfer process (depicted in Figure 1.10). First, the porphyrin bridge, retaining its chromophoric function from BChls and the dyads, is photoexcited into a singlet excited state. Following this, the excited electron migrates to the acceptor moiety $\left(k_{2}\right)$, driven by the energetic offset between the exciton and first charge transfer state $\left(\mathrm{CP}^{+} \mathrm{C}_{60}^{-}\right)$. An electron from the donor then relaxes $\left(k_{4}\right)$ into the vacancy in the bridge forming the final CT state. This state can undergo a decay process into the carotenoid triplet state[45] ( $k_{6}$ ) and finally relax down to the ground state. Incidentally, this triplet state, which provides photoprotection from singlet oxygen, is not seen in many other biomimetic materials but is seen in natural photosynthetic systems[40].

Each charge transfer process competes with a corresponding recombination process (not shown) that relaxes the system to the ground state. By comparing the rate constants ( $k_{x}$ ) of each forward process to other competing relaxation processes, one can ascribe a quantum yield value to each step

$$
\begin{equation*}
\Phi=\frac{k_{\text {forward }}}{k_{\text {forward }}+k_{\text {others }}} \tag{1.6}
\end{equation*}
$$

Large $k_{\text {forward }}$ values (faster process) compared to competing processes push $\Phi$ towards unity. Experimental studies of the formation of first CT state in Carotenoid-Porphyrin-Fullerene (CPF) triads indicate the quantum yield for this process lies around $\Phi>0.85)$.

Rozzi and corkers have combined experimental and theoretical techniques on a study of one CPF triad[46]. Their experimental work studies the triad in Figure 1.9 with the addition of mesitylene molecules at the porphyrin meso positions. Their theoretical work considers only the basic construction of the triad. In this work, they claimed coherent ultrafast charge transfer occurs at the sub-100 femtosecond scale. Differential transmission spectra showed the rise of a few bands following


Figure 1.10: Energies of transient states for M1. Energies levels will vary with triads M2-4 but are relatively similar. Arrows indicate electronic transitions with even numbers labeling charge transfer processes and odd numbered rates labeling relaxation processes. Republished with permission from Wiley and Sons.
system photoexcitation in the neighborhood of 550 nm . Each of these bands exhibited oscillatory behavior in intensity with a period of about 30 fs .

Their theoretical study involved a Time-Dependent Density Functional Theory (TDDFT)[47] excited state dynamics simulation of a similarly structured triad. By spatially integrating the electron density around the fullerene moiety, they measured the charging of the acceptor in time. A full electron of charge migrated to the fullerene with the charging shape also having some oscillatory behavior (roughly 30 fs period). As this is close to the conjugated carbon-carbon bond stretching period, they concluded that such nuclear vibrations are fundamental to CT. They performed additional TDDFT simulations freezing various subsets of nuclei. Each of these dynamics simulations showed mitigated charge transfer at some level and freezing all nuclei suppressed CT entirely.

Note, Ref. [46] only considered the results of a single trajectory which may not represent the actual CT dynamics within these triads. Furthermore, the molecule presented in the supplementary media of simulations does not reflect the molecule presented for their experimental work. Differences include lack of pyrolle methyl group on fullerene derivative (which extends the $\pi$ conjugation towards acceptor), a reversal of the amide linker, and para versus ortho connectivity on an aryl linker, all of which have known effects on electronic current and charge transfer[48, 49].

Cheung et. al. have approached computation of CT rates of the basic CPF triad (Figure 1.9) via the Fermi Golden Rule expression[50]. They applied the linearized semiclassical (LSC) approximation, developed by Geva[51], which has been shown to reproduce rate constants so long as the donor and acceptor potential energy surfaces are sufficiently parabolic and otherwise identical save for some difference in equilibrium coordinate and energy. The FGR expression reduces to a form reminiscent of
the Marcus expression via second-order cumulant approximation. Here, the various parameters in the Marcus expression can be related to the dynamical statistics of the donor-acceptor energy bandgap. With this approach and parameterization from molecular dynamics simulations with explicit solvent, their results indicate the formation of the first CT state at the picosecond scale and second state at far longer times with little difference resulting from rigid or flexible triad nuclei. They further identify a fundamental amide mode $\left(1700 \mathrm{~cm}^{-1}, \mathrm{C}=\mathrm{O}\right.$ stretching $)$ that is highly sensitive to the electronic state and triad conformation. This mode exhibits a blue shift of about $25 \mathrm{~cm}^{-1}$ between the $\pi-\pi^{*}$ and first CT states. Despite this sensitivity, there seems no imminent correlation between the mode position and the local electric field. Thereby, this mode is more likely to be affected by changes in the conjugations over other effects. With the dramatic shift in frequency, they propose that this mode can be probed to visualize or monitor the CT process.

### 1.2.3 Charge Transfer Rate Dependence on Molecular Construction

Charge transfer rates depend on the molecular system. It is surprising, however, just how sensitive they are to seemingly minor changes in moiety linkers and even side substituent groups. For example, in triads with donor-bridge units linked by an amide group, reversal of the amide direction changes the rate of formation of the final CT state by a factor of $\sim 30[37]$. A number of studies on the rectification behavior of small molecules and linkers substantiate this directional bias[52, 48, 53] and primarily attribute this effect to asymmetry in electronic structure.

Choice of side groups on the bridge can affect the electronic coupling between
the bridge and the acceptor. Several studies of CPF triads consider the porphyrin bridge linked to fullerene acceptor via an aryl group. Fluctuations of the dihedral angle between this linker and porphyrin not only modulate the electronic coupling to the acceptor but also perhaps affect the energy difference between excited and charge transfer states. Large aliphatic side groups in the $\beta$ positions sterically hinder the accessible angles the linker can sample. Small dihedral angles increase the $p_{z}$ orbital overlap where angles closer to $\pi / 2$ close the overlap. Therefore bridges with smaller side groups should allow better electronic overlap and result in faster CT rates. However experimental measurements prove otherwise: triads with aliphatic groups proved an order of magnitude faster[39, 43]. The absorption spectrum of the triads is remarkably close to a linear combination of spectra of the individual moieties $[39,46]$ indicating that when covalently linked, the moieties are nearly electronically independent; covalent bonding in the triad form only weakly perturbs the electronic structure of each moiety. Bahr and coworkers argue, in the framework of Marcus theory, that the thermodynamic driving force, $\Delta G^{0}$, has a much more significant effect on the CT rate than the electronic coupling.

### 1.3 Dissertation Overview

We are interested in identifying the principle vibronic motions that couple and modulate electron transfer processes in a class of molecules that model photosynthetic reaction centers in biological systems. In agreement with the literature, the present work confirms the crucial role vibrational dynamics play in the process of electron transfer in Donor-Bridge-Acceptor triads. Specifically, we identify particular vibrational modes of various Carotenoid-Porphyrin-Fullerene (CPF) systems that strongly
correlate to charge transfer following photoexcitation. Our investigations employ a density matrix formalism in the time-dependent Hartree-Fock (TDHF) schema in conjunction with molecular dynamics simulations to analyze vibrational modes of the system and assess the dependence of charge transfer on the smallest details of molecular structure.

This dissertation is structured in the following way. Chapter 2 details the derivation of the methodology with which we perform our investigations, including the density matrix formalism and its connection to TDHF through the Liouville-von Neumann equation. Further, we explain structure preparation and simulation setup. Chapter 3 presents, first, the results of the electron dynamics and charge transfer rate approximation and, second, an in-depth vibrational mode analysis of the CPF triads and detailed discussions of what charge-transfer depends on in these systems. We conclude by outlining immediate areas of improvement as well as speculations on the possible directions this project can take. The reader can find in Appendix A a multitude of Fortran and Python codes used in the development and analysis of this work.

## Chapter 2

## Methods

### 2.1 Dynamical Simulations

In highly conjugated organic systems, the electronic properties of interest primarily happen within the closely packed $\pi$ and $\pi^{*}$ molecular orbitals. We suspect that treating $\pi$-electrons quantum mechanically should sufficiently reproduce the charge transfer dynamics while significantly reducing computational cost. Therefore we assume negligible orbital overlap between $\sigma$ - and $\pi$-states and separate their degrees of freedom. The semiempirical Pariser-Parr-Pople (PPP)[54, 55] model readily reflects this paradigm and is implemented in the TINKER software[56].

The TINKER code employs a modified version of the PPP Hamiltonian wherein a specified number of atoms (sites), predesignated in the input, contribute a $p_{z}$ orbital and an appropriate number of electrons to the quantum system depending on expected atomic orbital hybridization. These site localized orbitals form the basis set for the quantum calculations and $\pi$ molecular orbitals. All other electronic interactions ( $\sigma$ system) are then treated with molecular mechanics (force fields). The ground state
is calculated via self-consistent field (SCF) iterations of the restricted Hartree-Fock (HF) equations

$$
\begin{equation*}
\mathcal{F}_{i j}=H_{i j}+\sum_{k}^{N / 2} \sum_{l m}^{N} c_{l k} c_{m k}^{*}[2(i j \mid m l)-(i l \mid m j)] \tag{2.1}
\end{equation*}
$$

$H_{i j}$ is the Hartree-core (one particle) term which encapsulates the electron's kinetic energy and Coulombic interaction with the nuclei (in atomic units):

$$
\begin{equation*}
H_{i j}=\langle i|-\frac{1}{2} \nabla^{2}-\sum_{A} \frac{Z_{A}}{r_{1 A}}|j\rangle \tag{2.2}
\end{equation*}
$$

where $A$ iterates through the nuclei. The second term is the two particle matrix and corresponds to Coulomb and exchange terms[57]. Indices $i, j, l$, and $m$ iterate through the basis (site) orbitals centered on the nuclei; the matrix element $c_{l k}$ is the contribution of site orbital $l$ to molecular orbital $k$ (the eigenvector matrix). The form of Equation 2.1 can be simplified with two steps. First, define a density matrix in the usual sense under closed-shell restricted (all electrons are spin paired and molecular orbitals are doubly occupied) Hartree Fock

$$
\begin{equation*}
\rho_{i j}=\sum_{k}^{N / 2} \sum_{l m} 2 c_{l k} c_{m k}^{*} \tag{2.3}
\end{equation*}
$$

Here, the coefficient of 2 denotes doubly occupied molecular orbital $k$. We generalize this expression as

$$
\begin{equation*}
\rho_{i j}=\sum_{k}^{N} \sum_{l m} \eta_{k} c_{l k} c_{m k}^{*} \tag{2.4}
\end{equation*}
$$

where $\eta_{k}$ is some population count ( 2 for closed-shell, 1 for open-shell). In this form, the density matrix is simply a unitary transform of the state occupations (a diagonal matrix) into site basis.

$$
\begin{equation*}
\rho_{\text {site }}=C \cdot \rho_{\text {state }} \cdot C^{\dagger} \tag{2.5}
\end{equation*}
$$

Here, the matrix $C$ is the modal matrix (molecular orbital) of the Fock matrix. Second, apply Complete Neglect of Differential Overlap (CNDO) approximation to
the two-particle integrals.

$$
\begin{align*}
(i j \mid k l) & =\int d \mathbf{r}_{1} d \mathbf{r}_{2} \chi_{i}^{*}\left(\mathbf{r}_{1}\right) \chi_{j}\left(\mathbf{r}_{1}\right) r_{12}^{-1} \chi_{l}^{*}\left(\mathbf{r}_{2}\right) \chi_{l}\left(\mathbf{r}_{2}\right)  \tag{2.6}\\
& =J_{i k} \delta_{i j} \delta_{k l}
\end{align*}
$$

(for atomic orbitals $\chi$ ). This reduces the HF equations to

$$
\begin{equation*}
\mathcal{F}_{i j}=H_{i j}+\sum_{k}^{N / 2} \rho_{i j} J_{i m}\left[\delta_{i j} \delta_{m l}-\frac{1}{2} \delta_{i l} \delta_{m j}\right] \tag{2.7}
\end{equation*}
$$

In this expression, terms $H_{i j}$ and $J_{i m}$ are approximated using semi-empirical parameters and are also dependent on the geometry of the system.

### 2.1.1 Nuclear-Electron Coupling

Electronic degrees of freedom are coupled to the molecular dynamics calculation by adjusting equilibrium bond lengths, bond force constants, and torsional barriers as a function of the site representation density matrix. The density matrix here is interpreted as a bond-charge matrix where diagonal elements represent site populations, and off-diagonal terms represent the $\pi$-bond order between two sites. The equilibrium bond length is calculated using a linear interpolation between idealized single and double bond lengths. Thus, for bonded atoms $i$ and $j$, the equilibrium bond length is

$$
\begin{equation*}
l=l_{1}+\delta l\left(1-\rho_{i j}\right) \tag{2.8}
\end{equation*}
$$

where $l_{1}$ is the idealized bond length for the double bond $\rho_{i j}=1$. The bond force constant is similarly interpolated

$$
\begin{equation*}
k=k_{1}-\delta k\left(1-\rho_{i j}\right) \tag{2.9}
\end{equation*}
$$

as is the torsional barrier

$$
\begin{equation*}
t=\rho_{i j} t_{1} \tag{2.10}
\end{equation*}
$$

In general off-diagonal elements of the density matrix have non-zero imaginary value, but the matrix must remain Hermitian $\left(\rho_{i j}=\rho_{j i}^{*}\right)$. For molecular mechanics parameters, we drop the imaginary value and use only the real part. It is clear to see that increasing the bond order ( $\pi$-bond character), the equilibrium length decreases while bond force constant and torsional barrier increases.

At each time step, SCF iterations recalculate the ground state Fock matrix, generating a new density matrix, and the above parameters are adjusted accordingly. Nuclear integration follows the new forces and the process repeats. In the context of harmonic oscillators, the vibrational energy of a normal mode depends on the mode's reduced mass and the force constant. In units of wavenumbers $\left(\mathrm{cm}^{-1}\right)$ :

$$
\begin{equation*}
\tilde{\nu}=\frac{1}{2 \pi c} \sqrt{\frac{k}{\mu}} \tag{2.11}
\end{equation*}
$$

where $c$ is the speed of light, $\mu$ is the reduced mass, and $k$ is the force constant taking into account the above computation. As a system undergoes thermal fluctuation, the electronic structure, and therefore elements of the density matrix, should not fluctuate wildly. However, an impulsive excitation causes significant deviation from the ground state and the collective changes in these force constants will change the overall dynamical behavior of the nuclei. In short, as the electronic state undergoes any form of transition, there will be a corresponding change in the vibrational modes.

### 2.1.2 Excited States from Configuration Interaction-Singles

Our first modification to this framework comes in the form of implementing an electronically excited state using Configuration Interaction-Singles (CI-S). In general, the CI method uses the HF states as input and generates a wavefunction composed of a
large number of elementary excitation states.

$$
\begin{align*}
& |\Phi\rangle= \\
& \quad C_{0}\left|\Psi_{0}\right\rangle+\sum_{a r} C_{a}^{r}\left|\Psi_{a}^{r}\right\rangle+\sum_{\substack{a<b \\
r<s}} C_{a b}^{r s}\left|\Psi_{a b}^{r s}\right\rangle+\sum_{\substack{a<b<c \\
r<s<t}} C_{a b c}^{r s t}\left|\Psi_{a b c}^{r s t}\right\rangle+\ldots \\
& \text { Ground State } \tag{2.12}
\end{align*} \quad \text { Singles } \quad \text { Doubles } \quad \ldots .
$$

In this notation, coefficients $C$ represent the contribution of the particular elementary excitation and $\left|\Psi_{a}^{r}\right\rangle$ implies moving an electron from occupied HF state $a$ to unoccupied HF state $r$ ( $b$ to $s, c$ to $t, \ldots$ ).

Even for a reasonable number of electrons, the full formulation quickly becomes intractable. We, therefore, dismiss double excitations and higher as well as truncate the input to the highest 20 occupied HF states and lowest 20 unoccupied HF states (amounting to 400 single excitations considered). Then, diagonalizing the CI Hamiltonian produces the excitation energies and excited states. We only consider singlet excitations and therefore restrict the possible excitations to the promotion of an $\alpha$-spin electron to another $\alpha$-orbital.

### 2.1.3 Density Matrix Formalism

For increasingly larger systems, repeating the SCF iterations at each time-step becomes computationally cumbersome (despite already ignoring non- $\pi$ electrons). The same holds for diagonalizing the CI Hamiltonian. The next modification changes the method by which we propagate a system in time. We take a time-dependent Hartree-Fock (TDHF) approach choose to evolve the density matrix in time via the Liouville-von Neumann equation. We briefly revisit the derivation from Ref [58] here.

We define the time-dependent density matrix by the outer product:

$$
\begin{equation*}
\rho(t)=|\psi(t)\rangle\langle\psi(t)| \tag{2.13}
\end{equation*}
$$

The time derivative of this expression gives:

$$
\begin{equation*}
i \hbar \frac{\partial}{\partial t} \rho(t)=\left(i \hbar \frac{\partial|\psi(t)\rangle}{\partial t}\right)\langle\psi(t)|+|\psi(t)\rangle\left(i \hbar \frac{\partial\langle\psi(t)|}{\partial t}\right) \tag{2.14}
\end{equation*}
$$

We apply the time-dependent Schrödinger equation and its adjoint

$$
\begin{align*}
i \hbar \frac{\partial}{\partial t}|\psi(t)\rangle & =\hat{\mathcal{H}}|\psi(t)\rangle  \tag{2.15}\\
i \hbar \frac{\partial}{\partial t}\langle\psi(t)| & =-\langle\psi(t)| \hat{\mathcal{H}}
\end{align*}
$$

to equation 2.14, giving:

$$
\begin{align*}
i \hbar \frac{\partial}{\partial t} \rho(t) & =\hat{\mathcal{H}}|\psi(t)\rangle\langle\psi(t)|-|\psi(t)\rangle\langle\psi(t)| \hat{\mathcal{H}}  \tag{2.16}\\
& =[\hat{\mathcal{H}}, \rho]
\end{align*}
$$

The above equation is often compactly written as:

$$
\begin{equation*}
\frac{\partial}{\partial t} \rho(t)=-\frac{i}{\hbar} \mathcal{L} \rho(t) \tag{2.17}
\end{equation*}
$$

where $\mathcal{L}$ is the Liouvillian super-operator that commutates the Hamiltonian and density matrices. In the time-dependent Hartree-Fock schema, we replace the Hamiltonian operator with the Fock operator

$$
\begin{equation*}
i \hbar \frac{\partial \rho}{\partial t}=[\mathcal{F}, \rho]=i \mathcal{L}_{\mathcal{F}} \rho \tag{2.18}
\end{equation*}
$$

We choose to expand the time propagator as a series of imaginary Chebyshev polynomials:

$$
\begin{equation*}
\left(e^{-i \mathcal{L} d t}\right) \rho(t)=\left(\sum_{k=0}^{N} a_{k} T_{k}(-i \mathcal{L} d t / R)\right) \rho(t) \tag{2.19}
\end{equation*}
$$

where $T_{k}$ is the $k^{t h}$ Chebyshev polynomial of the first kind. The value

$$
\begin{equation*}
R=d t\left(E_{\max }-E_{\min }\right) / 2 \tag{2.20}
\end{equation*}
$$

normalizes the super-operator eigenspectrum to range $[-1,1]$ as this is the region where the Chebyshev polynomials are defined. The coefficient $a_{k}$ is defined as such:

$$
\begin{equation*}
a_{k}=e^{i(R+G)} C_{k} J_{k}(R) \tag{2.21}
\end{equation*}
$$

where $C_{k}=1$ for $k=1$ and $C_{k}=2$ for $k>1 . J_{k}$ are the Bessel functions of the first kind of order $k$.

We use the Chebyshev expansion of the exponential is generally considered to be stable and converges rapidly. More importantly, this expansion scheme is norm preserving [59, 60]: the total magnitude of $\rho$ is conserved. This property ensures that the trace of the density matrix $(\operatorname{Tr}[\rho]=$ number of electrons) is also preserved. All of these traits are highly beneficial for maintaining accuracy and stability during longtime propagation. Finally, the recursive definition of the polynomials makes their computation trivial, even for a large number of expansion terms. For a normalized operator $\hat{X}$, the Chebychev polynomials are generated using the recursion relation

$$
\begin{align*}
& T_{0}(\hat{X})=\hat{1} \\
& T_{1}(\hat{X})=\hat{X}  \tag{2.22}\\
& T_{k}(\hat{X})=2 \hat{X} T_{k-1}(\hat{X})+T_{k-2}(\hat{X})
\end{align*}
$$

Within our implementation of this scheme, we truncated the recursion at 9th order giving a typical numerical error of $1: 10^{-10}$ (unitless) which we consider sufficiently accurate.

The Fock matrix (Eq. 2.7) is calculated at each time-step based on the current nuclear geometry and the previous electronic density matrix.

$$
\begin{equation*}
\mathcal{F}=\mathcal{F}(\mathbf{R}(t+d t), \rho(t)) \tag{2.23}
\end{equation*}
$$

The density matrix is propagated with the new Fock matrix, force field parameters are adjusted based on new bond orders, nuclei are iterated according to classical
mechanics, and the iteration process repeats. At time $t=0$, the ground state SCF computation and CI excited states must still be computed; implementing the time evolution removes the need for subsequent diagonalizations. However, it is perhaps wise to occasionally diagonalize the Fock matrix and collect the eigenspectrum to ensure the Liouvillain remains within the limit where the Chebychev polynomials are well behaved.

### 2.1.4 Hartree Core Coupling Term

The implementation of the PPP Hamiltonian is a nearest neighbors model: for the calculation of the Hartree core term, only matrix elements of bonded $\pi$-active atoms are non-zero. Then for systems with multiple molecules (e.g., stacked benzene rings) or $s p^{3}$ hybridized atoms between $\pi$-systems (e.g., diphenylmethane), the matrix is block diagonal. Despite the two-particle matrix, $J_{i m}$, being densely populated, the shape of $H_{i j}$ dominates in the SCF procedure. As a result, the final Fock matrix is block diagonal leading to localized molecular orbitals, and therefore, a block diagonal density matrix, as shown in figure 2.1. What this implies is that there is no electronic communication between these separated systems and, during the time evolution described previously, no charge can migrate between these systems.

We remedy this by lifting the nearest neighbors restriction and allow interaction between non-bonded sites. However, the original formulation of the one-particle term is calculated by the Whitehead and Lo formula[61]:

$$
\begin{equation*}
H_{i j}=\frac{3}{2}\left(E_{b}-E_{e}\right)-\frac{3}{8} \gamma_{11}+\frac{5}{12} \gamma_{12}-\frac{1}{24} \gamma_{14} \tag{2.24}
\end{equation*}
$$

where $E_{b}\left(E_{e}\right)$ is the bond energy of carbon-carbon bond in benzene (ethylene) calculated using a semiempirically parameterized Morse potential, $\gamma_{11}$ is the average of the


Figure 2.1: Matrix plots of the Fock (left, units in eV ) and density (right, unitless) matrices for a ground state calculation of stacked benzene and naphthalene. Indices 16 correspond to benzene carbons and indices 7-16 correspond to naphthalene carbons. Here, interactions are limited to nearest neighbors.
atomic repulsion energies of atomic orbitals $i$ and $j, \gamma_{12}=\left(r_{i j}^{2}+\gamma_{11}^{2}\right)^{-1 / 2}$ (for atomic orbital center distance $r_{i j}$ ), and $\gamma_{14}=\left(4 r_{i j}^{2}+\gamma_{11}^{2}\right)^{-1 / 2}$. The formula does not decay to zero at long distances due to the $\gamma_{11}$ term being distance independent. In the nearest neighbors approximation, this is acceptable as interaction distances between bonded sites are expected to remain within normal covalent bond lengths (1-2 $\AA$ ). Therefore, we introduce a Yukawa-like screening factor to the one particle calculation between non-bonded sites:

$$
H_{i j}^{\prime}= \begin{cases}H_{i j} & i, j \text { bonded }  \tag{2.25}\\ H_{i j} \times \exp \left[-\frac{r_{i j}}{r_{c r}}\right] \frac{a_{0}}{r_{i j}} & i, j \text { non-bonded }\end{cases}
$$

where $r_{c r}$ is an adjustable coupling radius and $a_{0}$ is the Bohr radius. At large $r_{i j}$, the interaction energy between sites $i$ and $j$ vanish and the SCF-minimized Fock matrix, and consequently density matrix, are no longer block diagonal (as seen in figure 2.2). As a result, discrete $\pi$-systems now interact. Coupling values are between non-bonded atoms are small relative to that of bonded atoms, but importantly non-zero. As a consequence of enabling this interaction, the $\pi$ orbitals now overlap and the electronic


Figure 2.2: Matrix plots of the Fock (left, units in eV) and density (right, unitless) matrices for a ground state calculation of stacked benzene and naphthalene. Indices 16 correspond to benzene carbons and indices 7-16 correspond to naphthalene carbons. Here the adjustable coupling parameter is turned on $\left(r_{c r}=2.0 \AA\right)$.
energy is lowered in the given example.

### 2.1.5 Excited State Density Matrix

Thus far, our formulation is exact, but in principle does not provide a means for propagating the system in an excited state. We now formulate an expression for the density matrix in the excited state. First, consider the population matrix in equation 2.5. Naïvely, we might simply move some population from a lower orbital into a higher one. For example, in the following six state system, we can create an excitation by promoting an electron from occupied orbital $\# 3$ into unoccupied orbital \#4.

$$
\begin{gather*}
\rho_{\text {state }}^{(e x)}=\left(\begin{array}{cccccc}
2 & & & & & \\
& 2 & & & & \\
& & 1 & & & \\
& & & 1 & & \\
& & & & & 0
\end{array}\right)  \tag{2.26}\\
\rho_{\text {site }}^{(e x)}=C \tag{2.27}
\end{gather*} \rho_{\text {state }}^{(e x)} C^{\dagger} .
$$

where we transform $\rho_{\text {state }}^{(e x)}$ to the site basis via unitary transform $C$. Note, in the state basis, both the Fock and density matrices are diagonal (all off-diagonal elements are
zero). This construction proves problematic in the context of equation 2.19. Recalling that the $C$ diagonalizes the Fock matrix and $C C^{\dagger}=C^{\dagger} C=\hat{1}$ :

$$
\begin{align*}
i \hbar \frac{\partial \rho_{\text {site }}}{\partial t} & =\left[\mathcal{F}_{\text {site }}, \rho_{\text {site }}^{(e x)}\right] \\
& =\mathcal{F}_{\text {site }} \rho_{\text {site }}^{(e x)}-\rho_{\text {site }}^{(e x)} \mathcal{F}_{\text {site }} \\
& =C \mathcal{F}_{\text {state }} C^{\dagger} C \rho_{\text {state }}^{(e x)} C^{\dagger}-C \rho_{\text {state }}^{(e x)} C^{\dagger} C \mathcal{F}_{\text {state }} C^{\dagger} \\
& =C \mathcal{F}_{\text {state }} \rho_{\text {state }}^{(\text {ex }} C^{\dagger}-C \rho_{\text {state }}^{(e x)} \mathcal{F}_{\text {state }} C^{\dagger}  \tag{2.28}\\
& =C\left(\mathcal{F}_{\text {state }} \rho_{\text {state }}^{(e x)}-\rho_{\text {state }}^{(e x)} \mathcal{F}_{\text {state }}\right) C^{\dagger} \\
& =C\left[\mathcal{F}_{\text {state }}, \rho_{\text {state }}^{(\text {ex })}\right] C^{\dagger} \\
& =0
\end{align*}
$$

where, in the final step, two diagonal matrices necessarily commute. Since the time derivative of the density matrix is zero, the matrix is stationary, will not evolve, and no electrodynamics will occur.

We, instead, define an excitation operator

$$
\begin{equation*}
A_{N}^{\dagger}=\sum_{p, h} z_{p h}^{*} \phi_{p}^{\dagger} \phi_{h} \tag{2.29}
\end{equation*}
$$

where $z$ is the contribution of the elementary excitation from $h \rightarrow p$ for excitation $N$. The operators $\phi$ are state operators which are further broken down as a linear combination of site operators, $a$

$$
\begin{equation*}
\phi_{n}^{\dagger}=\sum_{j} C_{j n}^{*} a_{j}^{\dagger} \tag{2.30}
\end{equation*}
$$

Again, matrix $C$ is the unitary transform that changes from state to site basis. Operator $A_{N}^{\dagger}$ acts on the HF ground state to produce the $N^{t h}$ excited state.

$$
\begin{equation*}
A_{N}^{\dagger}|H F\rangle=|N\rangle \tag{2.31}
\end{equation*}
$$

The ground state reduced density matrix is given by

$$
\begin{equation*}
\rho_{r s}=\left\langle a_{s}^{\dagger} a_{r}\right\rangle=\langle H F| a_{s}^{\dagger} a_{r}|H F\rangle \tag{2.32}
\end{equation*}
$$

where the HF ground state is generated by populating the lowest energy states from the vacuum state

$$
\begin{equation*}
|H F\rangle=\phi_{1}^{\dagger} \ldots \phi_{n}^{\dagger}|0\rangle \tag{2.33}
\end{equation*}
$$

for $n$ number of electrons. Using equation 2.30,

$$
\begin{align*}
\rho_{r s} & =\sum_{i j}\langle H F| \phi_{i}^{\dagger} \phi_{j}|H F\rangle c_{s i}^{*} c_{r j} \\
& =\sum_{i j} \delta_{i j}\langle H F| \phi_{i}^{\dagger} \phi_{i}|H F\rangle c_{s i}^{*} c_{r i}  \tag{2.34}\\
& =\sum_{i \leq n} c_{s i}^{*} c_{r i}
\end{align*}
$$

where we have now restricted $i$ to only the occupied orbitals. We now write the density matrix for singly excited state $N$ in the same fashion.

$$
\begin{align*}
\gamma_{r s}^{N} & =\langle N| a_{s}^{\dagger} a_{r}|N\rangle \\
& =\sum_{n m}\langle N| \phi_{n}^{\dagger} \phi_{m}|N\rangle c_{s n}^{*} c_{r m}  \tag{2.35}\\
& =\sum_{n m} \sum_{p^{\prime} h^{\prime}} \sum_{p h} c_{s n}^{*} c_{r m} z_{p^{\prime} h^{\prime}}^{*} z_{p h}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{p^{\prime}} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle
\end{align*}
$$

Indices $p$ and $p^{\prime}$ span over unoccupied orbitals; indices $h$ and $h^{\prime}$ span over occupied orbitals in the ground state; and indices $m$ and $n$ span all state orbitals, occupied and unoccupied. We now turn our efforts to simplifying the integral

$$
\begin{equation*}
I=\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{p^{\prime}} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \tag{2.36}
\end{equation*}
$$

Note, fermion orbitals operators must anti-commute

$$
\begin{equation*}
\left\{\phi_{n}, \phi_{m}^{\dagger}\right\}=\phi_{n} \phi_{m}^{\dagger}+\phi_{m}^{\dagger} \phi_{n}=\delta_{n m} \tag{2.37}
\end{equation*}
$$

Rearrangement gives

$$
\begin{equation*}
\phi_{n} \phi_{m}^{\dagger}=\delta_{n m}-\phi_{m}^{\dagger} \phi_{n} \tag{2.38}
\end{equation*}
$$

Furthermore, we can use the properties of $|H F\rangle$. Namely, a creation on an occupied orbital and annihilation on an unoccupied orbital both destroy the ket.

We start by moving $\phi_{p^{\prime}}$ to the right.

$$
\begin{align*}
I & =\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{p^{\prime}} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{n p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle-\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{p^{\prime}} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{n p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{p^{\prime}} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{n p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\delta_{p p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{h}|H F\rangle-\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{p^{\prime}} \phi_{h}|H F\rangle \\
& =\delta_{n p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\delta_{p p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{h}|H F\rangle+\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h} \phi_{p^{\prime}}|H F\rangle \\
& =\delta_{n p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\delta_{p p^{\prime}}\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{h}|H F\rangle \\
& =\delta_{n p^{\prime}} I_{1}+\delta_{p p^{\prime}} I_{2} \tag{2.39}
\end{align*}
$$

In $I_{1}$ move $\phi_{h^{\prime}}$ to the right.

$$
\begin{align*}
I_{1} & =\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{h^{\prime} m}\langle H F| \phi_{p}^{\dagger} \phi_{h}|H F\rangle-\langle H F| \phi_{m} \phi_{h^{\prime}}^{\dagger} \phi_{p}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{h^{\prime} m}\langle H F| \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\langle H F| \phi_{m} \phi_{p}^{\dagger} \phi_{h^{\prime}}^{\dagger} \phi_{h}|H F\rangle  \tag{2.40}\\
& =\delta_{h^{\prime} m}\langle H F| \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\delta_{h^{\prime} h}\langle H F| \phi_{m} \phi_{p}^{\dagger}|H F\rangle-\langle H F| \phi_{m} \phi_{p}^{\dagger} \phi_{h} \phi_{h^{\prime}}^{\dagger}|H F\rangle \\
& =\delta_{h^{\prime} m}\langle H F| \phi_{p}^{\dagger} \phi_{h}|H F\rangle+\delta_{h^{\prime} h}\langle H F| \phi_{m} \phi_{p}^{\dagger}|H F\rangle
\end{align*}
$$

$\phi_{p}^{\dagger}$ can be interpreted as annihilating to the left. Therefore the first term vanishes and $I_{1}$ reduces to

$$
\begin{equation*}
I_{1}=\delta_{h^{\prime} h} \delta_{m p} \tag{2.41}
\end{equation*}
$$

$I_{2}$ follows similarly.

$$
\begin{align*}
I_{2} & =\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{n}^{\dagger} \phi_{m} \phi_{h}|H F\rangle \\
& =-\langle H F| \phi_{n}^{\dagger} \phi_{h^{\prime}}^{\dagger} \phi_{m} \phi_{h}|H F\rangle \\
& =\langle H F| \phi_{n}^{\dagger} \phi_{m} \phi_{h^{\prime}}^{\dagger} \phi_{h}|H F\rangle-\delta_{h^{\prime} m}\langle H F| \phi_{n}^{\dagger} \phi_{h}|H F\rangle  \tag{2.42}\\
& =\delta_{h^{\prime} h}\langle H F| \phi_{n}^{\dagger} \phi_{m}|H F\rangle-\langle H F| \phi_{n}^{\dagger} \phi_{m} \phi_{h} \phi_{h^{\prime}}^{\dagger}|H F\rangle-\delta_{h^{\prime} m}\langle H F| \phi_{n}^{\dagger} \phi_{h}|H F\rangle \\
& =\delta_{h^{\prime} h}\langle H F| \phi_{n}^{\dagger} \phi_{m}|H F\rangle-\delta_{h^{\prime} m}\langle H F| \phi_{n}^{\dagger} \phi_{h}|H F\rangle
\end{align*}
$$

Take $\phi_{h}$ to create to the left. Then $I_{2}$ reduces to

$$
\begin{equation*}
I_{2}=\delta_{h^{\prime} h}\langle H F| \phi_{n}^{\dagger} \phi_{m}|H F\rangle-\delta_{h^{\prime} m} \delta_{n h} \tag{2.43}
\end{equation*}
$$

Since the HF ground state only has the lowest orbitals occupied, the remaining integral reduces to

$$
\begin{equation*}
\langle H F| \phi_{n}^{\dagger} \phi_{m}|H F\rangle=\delta_{n_{o c c}, m_{o c c}} \tag{2.44}
\end{equation*}
$$

where $n$ and $m$ here span only the occupied orbitals. Finally, the integral simplifies to

$$
\begin{align*}
I & =\langle H F| \phi_{h^{\prime}}^{\dagger} \phi_{p^{\prime}} \phi_{n}^{\dagger} \phi_{m} \phi_{p}^{\dagger} \phi_{h}|H F\rangle  \tag{2.45}\\
& =\delta_{h h^{\prime}} \delta_{n p^{\prime}} \delta_{m p}-\delta_{p p^{\prime}} \delta_{m h^{\prime}} \delta_{n h}+\delta_{p p^{\prime}} \delta_{h h^{\prime}} \delta_{n_{o c c}, m_{o c c}}
\end{align*}
$$

As expressed in the above equation, the density matrix is in the state space. That is, $h, h^{\prime}, p, p^{\prime}, m$, and $n$ iterate through the system's molecular orbitals. We examine these terms independently to interpret their physical meaning. The first term iterates $m$ and $n$ through the unoccupied orbitals and adds magnitude to the population and coherence terms. The second term iterates $m$ and $n$ through the occupied orbitals and subtracts magnitude. The third term accounts for the otherwise unaffected populations of the ground state.

Figure 2.3 plots these three terms for a six-state system (for which the first three


Figure 2.3: Matrix plots of each term in equation 2.45 for a sample six state system in the HF state basis. Plots are normalized to unity where orange represents an added quantity and blue represents a subtracted quantity. Values are unitless.
states are occupied in the ground state). The third term resembles the state population matrix of the naïve approach. The former two terms, however, not only shift populations to the excited states but also introduce coherences in the form of offdiagonal matrix elements. The final excited density matrix is not diagonal in this formulation but represents a pure state. The commutation of the generating Fock matrix and this excited state matrix is non-zero and, therefore, electron dynamics can occur.

### 2.1.6 Simulation Parameters

We are interested in studying the charge transfer properties of four DBA triad systems studied by Moore and coworkers[40, 43]. Figure 2.4 shows the breakdown of each molecule. Each molecule has the same acceptor ( $\mathrm{C}_{60}$ derivative) and polymeric donor (carotenoid) is are differentiated by their side groups on porphyrin bridges. In Molecule 1 (M1), the porphyrin ring is dressed by tri-substituted aryl groups. Molecule 2 (M2) is identical to M1 except for the two methyl substitutions on the aryl groups. Molecule 3 (M3) has methyl and $n$-butyl groups on the pyrrole sites.

Molecule 4 (M4), similar to M3, replaces the longer chain with ethyl groups. Additionally, the amide group is reversed on M4 relative to those of M1-3.

The four molecules are constructed and pre-optimized using external software, AVOGADRO[62]. Note, one can easily convert a standard PDB file to TINKER's version of XYZ via the provided routine PDBXYZ. Each optimized structure thermalized with a Nosé-Hoover thermostat set to $T=300 \mathrm{~K}$ in vacuum for 10 ps at a time step of $0.01 \mathrm{fs}\left(10^{6}\right.$ time steps). This temperature was chosen as an expected operating temperature for these systems in a real environment. The time-step must be chosen to capture electron dynamics adequately and should be shorter than the oscillation period of the time evolution operator. We therefore want $\delta t<\hbar / E$ or $E<\hbar / \delta t$, and our choice allows for the Liouvillian eigenspectrum to range between $\pm 1.2$ Hartrees. The adjustable coupling parameter was set to $1.5 \AA$ as it is slightly larger than the carbon-carbon bond distance of benzene. Figure 2.5 shows the molecules quickly achieve the target temperature and stay within a range of 20 K . From the last 5 ps , we sample 50 geometries (every 100 fs ) as the basis for the ensemble. (Note, we retain the coordinates and velocities of each sample.) We parameterize the molecular mechanics and semiemperical quantum mechanics with the MM3 parameter set[63].

We perform a single point calculation on each of these samples to determine the correct excited state to choose. For these triads, the excitation should resemble an exciton localized to the porphyrin bridge. We determine the correct excitation using the eigenvectors of the Fock and CI matrices in the following way. Let $C_{i, j}$ be the contribution of atomic orbital $i$ to molecular orbital $j$ and $z_{h p}^{N}$ be the contribution of elementary excitation (from molecular orbital $h$ to $p$ ) to the $N^{t h}$ excited state. Then, for any CI excitation, $N$, we calculate the percentage of the hole density localized to





Figure 2.4: Breakdowns of the four molecules simulated in this study. Each molecule have a common acceptor (Fullerene derivative, top left) and donor (carotenoid, top right) moiety. The bridging moieties differentiate the molecules (labeled 1-4).


Figure 2.5: Temperature vs time plot of the thermalization of each molecule.
the bridge as

$$
\begin{equation*}
P_{\text {hole }}(N)=\sum_{i \in \operatorname{Brg}} \sum_{h \in \mathrm{occ}}\left|C_{i, h}\right|^{2}\left|z_{h}^{N}\right|^{2} \tag{2.46}
\end{equation*}
$$

where $i$ sums over atoms in the bridge moiety and $h$ over the occupied molecular orbitals. Correspondingly, the percentage of electron density can be calculated as

$$
\begin{equation*}
P_{\text {elec }}(N)=\sum_{i \in \operatorname{Brg}} \sum_{p \in \text { unocc }}\left|C_{i, p}\right|^{2}\left|z_{p}^{N}\right|^{2} \tag{2.47}
\end{equation*}
$$

for $p$ over the unoccupied molecular orbitals. We choose the lowest energy excitation which has $P_{\text {hole }}$ and $P_{\text {elec }}$ larger than 0.75 (at least $75 \%$ of the exciton density is localized to the bridge). For most configurations, this corresponds to the first excited state $(\approx 2.0 \mathrm{eV})$. Each geometry is excited at $t=0$ and then freely relaxes given an energy kick for 10 ps . The thermostat and time step are retained at 300 K and 0.01 fs respectively.

This procedure essentially recreates the scenario of a molecule undergoing thermal fluctuations at operational temperatures, becoming photoexcited, and then undergoing electronic and nuclear relaxation.


Figure 2.6: Overlay of starting geometries for molecules M1-M4.

### 2.2 Analysis

### 2.2.1 Rate Approximation

The diagonal terms of the density matrix (bond-charge matrix) give the occupation number for an orbital. Thus in the site-basis, $\rho_{i i}$ represents an electron count on orbital $i$ centered on some $\pi$-active nucleus. Then, a partial trace of the density matrix, choosing for atoms assigned to a particular moiety, accounts for the total number of electrons localized to that moiety; the full trace of the density matrix reflects the total electron count of the system. The effective charge (population gain) is this partial trace of the density matrix at time $t$ subtracted by the ground state charge. For the acceptor moiety,

$$
\begin{equation*}
q_{\mathrm{Acc}}(t)=\sum_{i \in \mathrm{Acc}}\left(\rho_{i i}(t)-\rho_{i i}^{g s}\right) \tag{2.48}
\end{equation*}
$$

For multi-molecular systems, this calculation can be extended to consider the charging of whole molecules. We measure charge transfer by following the excess population in acceptor moiety in time for each trajectory. Fitting the charge transfer plots from each trajectory to a logistic growth function provides an approximate form:

$$
\begin{equation*}
q(t)=\frac{q_{\max }}{1+\exp \left[-k\left(t-t_{c}\right)\right]}+q_{0} \tag{2.49}
\end{equation*}
$$

where $q_{\max }$ is the long-time maximal charge transferred, $k$ is a steepness factor, $t_{c}$ is the function center ( $50 \%$ completion time), and $q_{0}$ is an initial charge amount. Nonzero $q_{0}$ represents some partial charge transfer character in the initial excited state. From these regressions, the fractional completion time can be computed as

$$
\begin{equation*}
t_{f}=t_{0}+\frac{1}{k} \ln \left[\frac{f}{1-f}\right] \tag{2.50}
\end{equation*}
$$

We take the $95 \% ~(f=0.95)$ completion time to represent a charge transfer time-scale; the inverse of this is interpreted as the reaction rate.

### 2.2.2 Time-Frequency Analysis

We are interested in evaluating the nuclear dynamics that occur during the charge transfer process. For this, we use the velocity autocorrelation function

$$
\begin{equation*}
C_{v v}(\tau)=\sum_{t=0}^{T-\tau} \sum_{i=1}^{N} \vec{v}_{i}(t) \cdot \vec{v}_{i}(t+\tau) \tag{2.51}
\end{equation*}
$$

where, $\tau$ is the lag time, $T$ is the total time, $N$ is the number of particles considered, and $\vec{v}_{i}(t)$ is the velocity of particle $i$ at time $t$. Fourier transform of the correlation function will give a power spectrum, a distribution of energy across frequencies which here is analogous to a vibrational spectrum. However, this only provides a time-averaged description and is only well suited for a stationary signal; it does not decode information about transient signals. We suspect that certain nuclear modes activate and deactivate during the charge transfer process. A time-frequency spectrogram of a nonstationary time-series will resolve evolution of the vibrational power spectrum[64]. We apply the Short-Time Fourier Transform (STFT) method on the velocity autocorrelation function to visualize the evolution of the nuclear dynamics in time:

$$
\begin{gather*}
S(\tau, \omega)=\int_{-\infty}^{\infty} f(t) g(t-\tau) \mathrm{e}^{-\mathrm{i} 2 \pi \omega t} d t  \tag{2.52}\\
g(t-\tau)= \begin{cases}\frac{1}{2}-\frac{1}{2} \cos \left(\frac{\pi(\tau-t+\mathcal{T})}{\mathcal{T}}\right) & |\tau-t| \leq \mathcal{T} \\
0 & |\tau-t|>\mathcal{T}\end{cases} \tag{2.53}
\end{gather*}
$$

where $\mathcal{T}$ is the window radius of the Hanning window function $g(t)$, defined in equation 2.53. Nakai and coworkers have used this technique for the analysis of ab initio dynamics simulations of collision reactions on small molecules[65, 66, 67, 68, 69, 70]. STFT resolution is restricted to the Heisenberg-Gabor limit such that wider window functions resolve frequencies better, but sacrifice time resolution whereas thinner windows give better time resolution but sacrifice frequency resolution[71, 72]. For a given
window radius, uncertainty in frequency can be computed as $\Delta \omega \approx(2 c T)^{-1}$. STFT was performed with a Hanning window of width $\mathcal{T}=600 f s\left(\Delta \omega \approx 28 \mathrm{~cm}^{-1}\right)$. At this resolution, we may not be able resolve finer details of the vibrational spectrograph, but it sufficiently suitable for our needs. Edge effects occur as a result of this analysis on finite time-series. At the temporal extrema, less information is available resulting in an overall smoothing and diminishing of the spectral intensity. To mitigate this, we include dynamics from 2 ps prior to the photoexcitation.

### 2.2.3 Screening Vibrational Modes

The discrete STFT process returns a 2-dimensional array in time and frequency. By plotting the spectrogram, we can visually inspect for and pick out modes that seem to correspond to the charge transfer time. Figure 2.7 follows the time-series of three modes $\left(\omega_{1}, \omega_{2}, \omega_{3}\right)$ from an example spectrogram where the vertical axis is the power spectrum intensity of a particular mode. In this example, we say the system undergoes charge transfer between $t=1 p s$ and $t=5 p s$ (gray region). The first mode (blue) has intensity only during the CT period, but no intensity before or after. The second mode (orange) behaves exactly opposite. It has intensity (activity) before and after CT, but not during CT. The third mode (green) is relatively active during the entire example simulation.

We find a correlation value between the spectral intensity of a mode and the charge transfer regime through the following steps. First, shift the intensities down for a mode's $\left(\omega_{k}\right)$ spectral time series such that its average lies at 0 ,

$$
\begin{equation*}
\tilde{S}\left(\tau, \omega_{k}\right)=S\left(\tau, \omega_{k}\right)-s_{k} \tag{2.54}
\end{equation*}
$$



Figure 2.7: (Left) Spectral Intensity vs Time of three example modes. The gray region represents the time span where charge actively migrates to the acceptor. (Right) Down shifted intensities with shifted rectangle function.
for some $s_{k}$

$$
\begin{equation*}
\int_{t_{1}}^{t_{2}} \tilde{S}\left(\tau, \omega_{k}\right) d \tau=0 \tag{2.55}
\end{equation*}
$$

where $t_{1}$ and $t_{2}$ are the temporal limits of the vibrational time considered. Then define a rectangle function that is unity in the gray region and zero otherwise and again shift it down so that its average value is 0 (fig 2.7 (right)).

$$
\begin{equation*}
\int_{t_{1}}^{t_{2}} \operatorname{Rect}(\tau) d \tau=0 \tag{2.56}
\end{equation*}
$$

The result of these shifts is plotted in Figure 2.7 (right). The inner product of the shifted spectral time-series, $\tilde{S}$, and the shifted rectangle function

$$
\begin{equation*}
C\left(\omega_{k}\right)=\int_{t_{1}}^{t_{2}} \tilde{S}\left(\tau, \omega_{k}\right) \operatorname{Rect}(\tau) d \tau \tag{2.57}
\end{equation*}
$$

gives a correlation strength between the mode and the charge transfer process. A large positive value indicates direct correlation: the mode is specifically active during the charge transfer. A large negative value indicates the mode is inactive during charge transfer and it is active otherwise. Small correlation values indicate either poor correlation or low spectral amplitude, either of which implies the mode is of no interest. Thus, this analysis gives a compact value that relates the activity of a mode to the charge transfer process.

## Chapter 3

## Charge Transfer Dynamics in Model Triad Systems

### 3.1 Ensemble Configurations

Given the non-trivial construction of the molecules of interest and their high number of vibrational degrees of freedom, we must introduce a statistical component to our investigations. Generally, a large selection of random configurations will result in a distribution around an average case. However, given constraints in time and resources, we are limited to a finite number of configurations to simulate. To produce these initial configurations, we uniformly sample ground state thermal fluctuations. Despite this uniform sampling, we can show the configurations are sufficiently random. The time correlation function, $C_{q q}(t)=\langle q(t) q(0)\rangle$, of the geometries shows the correlation strength between two configurations separated in time. We plot in Figure 3.1 both the correlation function and exponential decay fit. The correlation time can be found


Figure 3.1: Geometry correlation plot (light) and exponential decay fit (dark) of the ground state dynamics for each molecule. Correlation functions are normalized to the initial value: $\tilde{C}_{q q}(t)=C_{q q}(t) / C_{q q}(0)$.
from the integral

$$
\begin{equation*}
\tau_{c}=\int_{0}^{\infty} \frac{C_{q q}(t)}{C_{q q}(0)} d t \tag{3.1}
\end{equation*}
$$

The results from these ground state dynamics reveal a correlation time of about 3 fs. Consequently, the system does not retain memory from a previous configuration and samplings separated in time by the correlation time, $\tau_{c}$, or longer can be considered uncorrelated. Our sampling time is $t_{\text {samp }} \sim 30 \tau_{c}$ and we can consider the initial geometries to represent random thermal configurations.

Thermal fluctuations in the molecular configuration modulate the excitation energy and we need to check that the distribution of excitation energies of our initial geometries match that of the full configurational space. We assume in the last 5


Figure 3.2: Energy distributions for the first excited singlet state for each molecule. Smooth distributions represent the distribution of excitation energies from 5000 ground state samplings each. Discrete histograms represent the 50 initial configurations chosen for the ensemble.
ps of the ground state dynamics, each system samples operational temperature configurations and that a selection of 5000 geometries adequately represents the full configurational space. Figure 3.2 compares the energy distributions of the selected initial geometries and subset of 5000 geometries. We find that not only the excitation energies not only match the distribution of the broader configuration space, but the average excitation energies also are in excellent agreement with experimental absorption spectra of the lowest excitation energy for the porphyrin moieties ( $\sim 1.9$ $\mathrm{eV})[40,43]$ as well as spectra computed using higher theory levels[73, 74].

### 3.2 Approximated Charge Transfer Rates

Recently, coherent dynamics have been used to explain charge transfer at the subpicosecond time scale[75, 76, 77]. In this strong electronic coupling regime, constructive interference of CT pathways opens up the possibility of rapid transfer despite large physical separation between chromophores in photosynthetic proteins[78, 79, 80]. Conversely, low electronic coupling typically entails electron hopping from site to site and results in a much slower transfer process. Figure 3.3 shows the excess electron population in (charge transferred to) the $C_{60}$ moieties for each trajectory. In most cases, CT does not begin until after 2 ps and completes at various times. The simulations indicate longer than picosecond timescales and therefore low electronic coupling between bridge and acceptor.

Following excitation at $t=0$, most trajectories do not immediately begin the CT process. Some excited state dynamics almost always ensues as the system responds to the impulsive vertical excitation before the initiating charge transfer. Once CT has completed, the charge separation is stable and long lived. We have not evolved the trajectories passed 10 ps ; formation of the second charge transfer state $\left(\mathrm{C}^{+}-\mathrm{P}-\mathrm{C}_{60}^{-}\right)$is expected to be on the order of tens to hundreds of picoseconds with a lifetime into the nanosecond scale.

All four molecules successfully undergo some amount of charge transfer within 10 ps. This implies that charge transfer itself is determined by the offset between HOMO and LUMO energy levels of the donor and acceptor moieties. Additionally, this agrees with experimentally observed quantum yield of unity. However, the amount and rate of CT depend on the finer details of the molecular structure. We see the range of total charge transferred, between $0.05-0.35 q$ is consistent through all molecules, while the


Figure 3.3: Charge accumulation plots for each trajectory in M1-4. Plots generally follow a logistic growth regression excluding one anomalous trajectory in M1.
distributions of the CT curves differ among them.

Charge accumulation follows a logistic growth function quite well ( $R^{2}>0.99$ ), excluding one errant trajectory in M1. Further investigation of this simulation shows the lowest energy porphyrin excitation $\sim 3 \mathrm{eV}$ producing an extremely "hot" exciton. This excitation is anomalously high compared to the 1.9 eV for all other trajectories. Therefore, we deem this a significant outlier and exclude it from further analysis. We approximate the CT rate constant as the inverse of the $95 \%$ completion time (using the logistic fits) which are plotted. Figure 3.4 adds crucial information about the CT rates, which are difficult to assess from the multitude of trajectories in Figure 3.3. From Figure 3.4, we can clearly see that difference in chemical structure, even subtle ones, alter CT rates and their distribution. While our approach overestimates rates for M1 and M2 as compared to experiment, the rates for M3 and M4 are in good agreement with experimental results[42, 43] (dashed lines). However, the overestimation is systematic between the pair of molecules and we are able to reproduce their relative similarity of rates seen in experiment. Furthermore, our results differ from the LSC approach by less than a factor of $10[6,50]$.

Interestingly, trajectories that take the longest to initiate the charge transfer process tend to have a proportionately lower total amount of charge transferred. M2-4 have prominent examples of such where CT does not begin until about 4 ps after excitation and ultimately settles at 0.1 q of charge transferred. In these instances, the system undergoes vibrational relaxation during the delay time. In the frame work of the potential energy surfaces, the system relaxes into an energy well and cannot make the transition into a charge transfer state. Such trajectories may be examples of cold excitons. Here, excess excitation energy is lost and dissociation occurs along low energy paths resulting in slower CT[81].


Figure 3.4: Histogram of the charge transfer rates of each ensemble. Averaged rates for M1-4 are $0.28 \pm 0.04 \mathrm{ps}^{-1}, 0.28 \pm 0.07 \mathrm{ps}^{-1}, 0.26 \pm 0.06 \mathrm{ps}^{-1}$, and, $0.23 \pm 0.06$ $\mathrm{ps}^{-1}$ respectively. Dashed lines indicate experimentally reported values with rate for M4 reported as a maximum[43].


Figure 3.5: Charge accumulation plots for select trajectories in M1 (M1, blue), trajectories with frozen side groups (M1-Frz, purple), and trajectories with no $\pi$ contribution from side groups (M1-No $\pi$, pale green).

We further explore the electronic effect of the aryl side groups in M1. We take the subset of 10 initial configurations that were chosen for vibrational analysis (discussed in the next chapter) and resimulate the excitation and relaxation dynamics with two variations. In the first, we freeze the aryl group atoms while maintaining their electronic contribution to the $\pi$-system ("quantum active"). In the second, side group atoms are free to move but provide no quantum contribution ("quantum inactive"). Figure 3.5 plots the charge accumulation in the acceptor for these trajectories, including the original ten.

Within each sub-ensemble, CT behavior remained similar to one another, however, imposing these exclusions mitigates CT. Computed as previously, CT rate constants are $0.29 \mathrm{ps}^{-1}, 0.20 \mathrm{ps}^{-1}$, and $0.16 \mathrm{ps}^{-1}$ for M1, M1-Frz, and M1-No $\pi$ sub-ensembles, respectively. Freezing side aryl group nuclei causes nearly a $30 \%$ reduction in CT rate and slightly diminishes the quantity of charge transferred, qualitatively agreeing with results from simulations of similar motifs in Ref [46]. Disabling the $\pi$ contribution
from the side aryl groups further reduces the CT rate and quantity. Notably, the CT curves this sub-ensemble are smooth relative to the other two. Very little excited state electronic dynamics occurs until the actual CT process is initiated. This is also seen in the CT plots for M3 and M4. The aryl groups modulate the electronic structure of the bridge at a small level. Furthermore, including the side groups into the conjugated system provides a relaxation pathway where the system can funnel excess electronic energy until energetic overlap becomes suitable for CT. This is consistent with M3 and M4 as their bridge side groups are not conjugated and overall these systems have slower CT according to our simulations. However, this does not agree with experimental results which indicate that formation of the initial CT state in M1 and M2 be much slower than that of M3 and M4. As a final remark, these results indicate bridge side groups provide electronic and vibrational relaxation pathways that improve the charge transfer rate in such DBA triads.

## Chapter 4

## Transient Vibrational Dynamics <br> Related to Charge Transfer in

## Model Triads

The compact form of the Marcus expression suggests that only few degrees of freedom are involved in the CT process. However, it is not altogether obvious how to determine these motions. Here, we propose the Short Time Fourier Transform (STFT) of the velocity autocorrelation function to resolve vibrational modes in both frequency and time, visualizing how the nuclear modes evolve over the course of the charge transfer process. By examining at each trajectory individually, some noise will be inherent. Examining the entire ensemble collectively will reduce the noise and amplify common modes in the wavenumber dimension. However, trajectories within an ensemble are not all temporally similar. Even if two trajectories exhibit similar vibrational information independently, the dissimilarities in charge transfer time-frame may dilute spectral intensity in the time dimension.

To avoid this, we choose a sub-ensemble of trajectories for each molecule that exhibit similar temporal charge transfer character. To choose these, we compute a pairwise difference squared integral to calculate the "distance" between two trajectories. Let $q_{i}(t)$ and $q_{j}(t)$ be two logistic regressions (per Equation 2.49) for trajectories indexed $i$ and $j$ of the same molecule. We define a quantitative measure as the "distance" between trajectories $i$ and $j$,

$$
\begin{equation*}
\epsilon_{i j}=\int_{t_{1}}^{t_{2}}\left(q_{1}(t)-q_{2}(t)\right)^{2} d t \tag{4.1}
\end{equation*}
$$

for $t_{1}$ and $t_{2}$ defining a given time window considered. Identical functions result in a vanishing integral and deviations results in increasingly larger $\epsilon$. We choose the set of 10 trajectories which mutually give the smallest collective difference integral. Since the Fourier Transform and STFT are linear operations, the average spectrogram can be achieved by averaging the autocorrelations of the trajectories chosen and then performing the transform.

Each molecule simulated contains between 238-272 atoms which leads to over $700(3 N-6)$ vibrational modes. The entire triad is a highly conjugated system whose moieties themselves are conjugated subsystems. Naturally, these subsystems have overlapping vibrational spectra wherein spectral intensity from some modes of one moiety could be washed out by that of another moiety. While this indicates such modes are weaker relative to the total system, they still may be relevant to the CT process. Analysis of the entire molecule as a whole may obscure crucial results. By considering where the differences in construction between molecules lie or crucial points in the molecule (linkers), we can isolate the necessary atomic subsets, perform an autocorrelation of their velocities, and then perform the STFT to reveal the underlying dynamics. We then screen the resulting spectrograms for modes with temporal behavior aligned to the charge transfer process. The temporal limits for
screening, $t_{1}$ and $t_{2}$, are defined by the $5 \%$ and $95 \%$ CT completion times, respectively, to sufficiently encapsulate the region of interest.

### 4.1 M1 and M2 Bridge Aryl Substituent Groups

We first consider molecules M1 and M2. Here, the major difference between the two is the number of methyl groups on the meso aryl side groups attached to the porphyrin. In Figure 4.1 we present the STFT spectrograms for these two. Immediately noticeable, modes of energies higher than $700 \mathrm{~cm}^{-1}$ are of low intensity or absent altogether. Typical vibrational spectra for mesitylene and toluene consist of out-of-plane ring distortions at $700-800 \mathrm{~cm}^{-1}$ and $\mathrm{C}=\mathrm{C}$ stretches at $1500 \mathrm{~cm}^{-1}$. The low energy vibrations in Figure 4.1 are torsional modes with the side aryl rings rotating across the bond linking them to the porphyrin bridge. We confirm this by computing the time series of the dihedral angle of these groups to the porphyrin. Fourier Transform of these time-series reveals spectral intensities centered at the same frequency in the STFT spectrograms (Figure 4.2, top).

Regarding M1, two modes at 190 and $425 \mathrm{~cm}^{-1}$ appear in all three visualizations, confirming both the torsional dynamics and relevance to the CT process. The dihedral angle here modulates the amount of $p_{z}$ orbital overlap and therefore has an effect on the local electronic structure of the bridge. A previous calculation gives the first excitation energy dependence on the dihedral angle of an idealized configuration of an isolated diaryl porphyrin, plotted in Figure 4.3. This calculation was performed at the PPP theory level rotating the side benzene rings maintaining $D_{2}$ symmetry. The computation reveals only a 0.1 eV difference in excitation energy for dihedral angles between $0^{\circ}$ (full $p_{z}$ overlap) and $90^{\circ}$ (no $p_{z}$ overlap). However, given the amount


Figure 4.1: STFT spectrograms for M1 (top) and M2 (bottom) aryl side groups on the bridge.


Figure 4.2: (Top) Fourier Transform of the dihedral angle time-series between the bridge and its aryl side groups for M1 and M2. (Bottom) Screened STFT modes for the same subunits in M1 and M2. Both figures here are featureless over $800 \mathrm{~cm}^{-1}$.
of steric hindrance experienced, the accessible angle space is constrained between $72^{\circ}\left( \pm 4^{\circ}\right)$ and the excitation energy accordingly differs by about 6 meV . Thus, for practical purposes, the dihedral angle of these conjugated side groups has little effect on the bridge electronic structure and therefore CT. Despite this, we can conclude there is still some interplay between the CT process and this particular mode: in the context of vibronic transitions, excitation of this mode certainly accompanies the $\pi-\pi^{*}$ electronic excitation.

With less steric hindrance, M2 has a much stronger response from the $360 \mathrm{~cm}^{-1}$ torsional mode; however, this mode is generally active throughout the simulation time and therefore does not pass screening. Conversely, the strong $600 \mathrm{~cm}^{-1}$ mode correlates to CT but is not prominent in the dihedral spectrum and therefore this is likely to be some low energy ring distortion. Charge transfer in M2, then, seems unaffected by torsional motions of the aryl side groups. We make the same arguments as with M1; these modes are activated during the initial excitation but do not play an essential role in electronic relaxation of the system into a charge transfer state.

### 4.2 M3 and M4 Bridge/Acceptor Aryl Linker

We next consider M3 and M4. The bridge side groups here are not $\pi$ active and, similar to the previous molecules, do not have a significant impact on the electronic structure of the bridge directly. From an experimental standpoint, aliphatic substituents like these are included to control the solubility of the molecule. However, as pointed out by Bahr, the longer chains in the $\beta$ positions sterically interfere with and force the linker aryl groups into perpendicular orientations[39]. Recent DFT computations on these triads showed that optimized structures have dihedral angles


Figure 4.3: First excitation energy of isolated diaryl meso substituted porphyrin dependence on dihedral angle, $\phi$. Inset is a rendering of a planar porphyrin with one meso aryl substituent. Hydrogens have been removed for clarity. $\phi$ indicates dihedral (small) angle between porphyrin and benzene planes. Points correspond to calculated energies. Gray curve corresponds to a curve fit. Fit: $\Delta E(\phi)=E_{\max }-\delta E * \cos ^{2}(\phi+\gamma)$, $\mathrm{E}_{\max }=1.35 \mathrm{eV}, \delta E=0.12 \mathrm{eV}, \gamma=0.12$ (radians).


Figure 4.4: Distribution of dihedral angles sampled by the aryl linker between the bridge and acceptor moieties during dynamics for M1-4.
that agree with this notion[82]. The dihedral angle of these linkers to the porphyrin should have a much larger impact on CT the side aryl groups. Increased orbital overlap between porphyrin and these linkers extends the molecular $\pi$ orbital towards the fullerene acceptor and therefore increases the electronic interaction between the two subsystems. Figure 4.4 plots a smooth histogram distribution of the dihedral angles sampled by these linkers (for molecules M1-4). Curiously, our dynamics results show a contrary trend. The linker in M3 is constrained to a smaller angle space, but does not sample angles perpendicular to the porphyrin and instead stays in the region of just over $60^{\circ}$. The linker in M4 accesses a wider angle space and, although sterically allowed to have a more planar angle, tends to remain closer to perpendicular to the porphyrin plane. However, our dynamics indicate aryl linkers in M1 and M2 oscillate around $61^{\circ}$, the ground state orientation observed in DFT calculations[82].

STFT spectrograms for these subunits are found in Figures 4.5. The low frequency modes ( 390 and $600 \mathrm{~cm}^{-1}$ ) are muted in M3. These frequencies appear in the dihedral angle times-series analysis (Figure 4.6, top) and we define both torsional
modes. When screened, the former mode is of no interest, but the latter mode shows as strongly anticorrelated. Low spectral intensity in STFT is consistent with the narrow distribution of angles sampled. We argue here that as electron density travels through the linker, the angle with the bridge plane is relatively locked in place. The mode at $950 \mathrm{~cm}^{-1}$ has strong response at early time then slowly decays. This mode accompanies the initial photoexcitation but diminishes once CT begins. Furthermore, it does not appear in the dihedral analysis and therefore we define this as a ring distortion mode. Of lower overall intensity, the $1010 \mathrm{~cm}^{-1}$ mode shows some response following excitation, then increased activity during CT, and finally decaying after that. Weaker still, the $1570 \mathrm{~cm}^{-1}$ mode shows as highly correlated. We determine these last two modes as ring vibrations as they do not appear in the dihedral angle analysis.

Spectra for the aryl linker in M4 reveal the presence of similar modes to that of M3. The $390 \mathrm{~cm}^{-1}$ mode appears anticorrelated but has a far too weak intensity to have significance. Contrary to M3, the $600 \mathrm{~cm}^{-1}$ mode is not only highly active, strengthens the anticorrelation. Intense activity of this mode before CT corroborates with large angle space the wide range of angles sampled; however, torsion is restricted once current flows through the linker. Temporal shape of the $950 \mathrm{~cm}^{-1}$ mode in largely mimics that of the $600 \mathrm{~cm}^{-1}$ mode in M3 but with larger intensity: this mode is active at photoexcitation, but absent after that. Two final vibrational modes at 1120 and $1600 \mathrm{~cm}^{-1}$ are relatively weak in the STFT spectrogram, however, still correlated to CT.


Figure 4.5: STFT spectrograms for aryl linker between bridge and acceptor in M3 (top) and M4 (bottom).


Figure 4.6: (Top) Fourier Transform of the dihedral angle time-series between the bridge and the aryl ring which links bridge and acceptor moieties for M3 and M4. Figure is featureless above $1500 \mathrm{~cm}^{-1}$. (Bottom) Screened STFT modes for the same subunits in M3 and M4.

### 4.3 Donor/Bridge Amide Linker

Amide linker STFT spectrograms are plotted in Figures 4.7 and 4.8. Prevalent for all four molecules are intense features at $700,1000,1200$, and $1300-1400 \mathrm{~cm}^{-1}$. Upon screening these modes in time, only the 700 and $1200 \mathrm{~cm}^{-1}$ appear to play significant roles. Vibrational computation on formamide suggests the $700 \mathrm{~cm}^{-1}$ mode corresponds to a twisting motion along the C-N bond. In M1 and M2, this mode is sporadically activated and deactivated. However, there is a stark difference with M3 and M4, recalling that direction of this linker is reversed between the two. According to rectification studies, the amide favors current travelling from the nitrogen side to the carbon side[48]. Thus, the linker in M3 has favorable orientation to allow electron density to pass from the donor to the bridge. In our studies, this mode correlates extremely well with CT to the acceptor. Naturally, the net positive charge in the bridge will begin to attract electron density from the donor. In M4, the amide is in the unfavorable orientation and we show here that the $700 \mathrm{~cm}^{-1}$ mode is deactivated during CT from bridge to acceptor. It is reasonable to believe that this particular mode is highly sensitive to the direction of current passing through the amide. The mode in the region of $1200 \mathrm{~cm}^{-1}$ (Amide III: C-N stretch, C-N-H bend) is universally deactivated during CT in all four molecules indicating this mode is not conducive to CT. In contrast to the findings published in Ref. [50], we see no activity in amide modes above $1500 \mathrm{~cm}^{-1}$.

### 4.4 Bridge and Acceptor

We turn our attention now to the porphyrin bridge moiety. STFT spectrograms are found in Figures 4.10 and 4.11. Mode screening for the four bridges are found


Figure 4.7: STFT spectrograms for the amide linker in M1 (top) and M2 (bottom).


Figure 4.8: STFT spectrograms for the amide linker in M3 (top) and M4 (bottom).


Figure 4.9: Screened vibrational modes for the amide linker in M1-4.
in Figure 4.12. What is immediately obvious between the four spectrograms is the general absence of features under $500 \mathrm{~cm}^{-1}$ and above $1500 \mathrm{~cm}^{-1}$. This featureless region is line with ground state experimental and computational vibrational studies of water solvated free base (and select derivatives of) porphryrin[83, 74]. M1 and M2 exhibit some low energy modes at 500 and $600 \mathrm{~cm}^{-1}$, respectively, that strongly correlate with CT. These macromolecular modes are note present in M3 or in M4, thus we can speculate these modes resemble macro-ring twisting with nodes at the meso position. Such modes would alter the aromaticity of ring (breaking planarity, and therefore having a marked impact on electronic structure) but would be far more restricted by the heavier alkyl $\beta$ substitutions in M3 and M4. The $720 \mathrm{~cm}^{-1}$ mode, likely some alternative ring deformation, is active in all four molecules and is anticorrelated with CT, excluding M3 where it is uncorrelated. The intensity of this mode is oscillatory throughout the dynamics, activated universally at the time
of excitation then progressing with seemingly inconsistent behavior.

In the 950-1050 $\mathrm{cm}^{-1}$ vibrational region, M1 and M4 show CT correlation while M2 and M3 show anticorrelation with spectral intensities differing between all four molecules. M1 solely sees a strongly anticorrelated mode at $1110 \mathrm{~cm}^{-1}$. This mode in both M1 and M2 is activated at excitation then decays in time; however, the mode reemerges after CT in M1. The same frequency in M3 and M4 is almost entirely nonexistent lending to the idea this mode is ring torsion with nodes at meso carbonds. Most nuclear displacement would occur at the pyrolle rings which would be inhibited by heavy $\beta$ substituents. Finally, a mode in the mid $1400 \mathrm{~cm}^{-1}$ range shows as correlated in M2, anticorrelated in M3, and decorrelated in M1 and M4. These modes are of low intensity overall and temporal behavior is universally noisy, perhaps only coincidentally aligned (misaligned) with CT in M2 (M3).

We finish here with examination of the acceptor moiety. STFT spectrograms for the fullerene dynamics can be found in Figures 4.13 and 4.14. The mode screening for the acceptors can be found in Figure 4.15. Contrary to the bridge counterparts, the acceptors have much more activity in the low-frequency range and relatively subdued activity at higher frequencies. In general, the spectrograms reveal that most of the dynamical activity is in breathing or other macromolecular modes as opposed to local carbon-carbon stretches. Density Functional Theory (B3LYP level) studies of $\mathrm{C}_{60}$ and $\mathrm{C}_{60}^{-}$indicate ionic forms have larger overall radii and distortion of the spherical geometry versus the neutral molecule[84]. We expect to see breathing modes accompany electronic charging of this moiety. Indeed, all four molecules show some level of correlation to CT with a mode between $200-250 \mathrm{~cm}^{-1}$ with M4 having a strong correlation. A multitude of other modes show strong correlation in either direction (e.g., $500,700,1000-1200,1500 \mathrm{~cm}^{-1}$ ) but are not consistent between systems.


Figure 4.10: STFT spectrograms for the porphryin bridge in M1 (top) and M2 (bottom).


Figure 4.11: STFT spectrograms for the porphryin bridge in M3 (top) and M4 (bottom).


Figure 4.12: Screened vibrational modes for the porphyrin moiety in M1-4.

Vibrational energy within the porphyrin is primarily distributed amongst higher frequency modes, which is likely associated with the large electronic excitation energy pumped into a localized region. The fullerene, conversely, has most of its vibrational energy distributed among low energy modes. Outside of the modes mentioned above, no other modes seem to behave consistently across these triads, at least temporally. The inconsistency in vibrational behavior could be due to a few reasons. Our subset for STFT analysis chooses only 10 trajectories, which may be an insufficient number for analyzing larger structures. Analysis of linker and bridge side groups involved at most 12 atoms, limiting the total number of normal coordinates, whereas the same analysis of full moieties requires the consideration of 30 atoms and upwards. A large number of degrees of freedom gives rise to more vibrational modes that are both energetically similar (possibly degenerate) and energetically accessible. Alternatively, the dynamics of the triads depends heavily on the initial conditions, and this is easily


Figure 4.13: STFT spectrograms for the fullerene acceptor in M1 (top) and M2 (bottom).
seen in Figures 3.3 and 3.4. Variations in the geometries necessarily result in varying excitation energies and excited electronic structures which in turn give diverse charge transfer characteristics. Therefore, averaging more trajectories would either reduce the vibrational noise resulting from the increase in accessible modes or, if noise is not reduced, give further credence to the sensitivity to initial conditions.

An additional effect of the dynamical evolution of force constants with the electronic structure is the blue- or red-shifting of the vibrational modes, most prominently in the amide STFT spectrograms. Within the harmonic oscillator approximation, the frequency of a mode is proportional to the square root of the force constant which is modulated by the $\pi$ bond order (off-diagonal elements of the site basis density matrix). The most extreme case of this shift is around $50 \mathrm{~cm}^{-1}$ seen in the 1000 $\mathrm{cm}^{-1}$ mode in Figure 4.1 (bottom) whereas this effect is less pronounced in other spectrograms. While this shift should be an indicator of fluctuating electronic state, our choice of time-frequency analysis and window function width in this work gives a frequency uncertainty of about $28 \mathrm{~cm}^{-1}$ and, consequently, we reserve detailed discussion of the effect in the present results. The trade-off between uncertainty in temporal or frequency resolution is unavoidable. However, the wavelet transform technique of time-frequency analysis does provide better resolution than STFT and future analyses will benefit from this approach $[71,68,85]$.


Figure 4.14: STFT spectrograms for the fullerene acceptor in M3 (top) and M4 (bottom).


Figure 4.15: Screened vibrational modes for the acceptor moiety in M1-4.

## Chapter 5

## Conclusion

We have presented here the results of mixed quantum mechanical/molecular mechanics simulations modeling electron and nuclear dynamics in four Donor-BridgeAcceptor triads, each with slightly differing bridge constructions. By taking a statistical approach, we ensure our simulations are representative of the average charge transfer behavior of these systems. Our model can reproduce experimentally accurate excitation energies for a localized excitation on the porphyrin bridge. Electron population analysis indicates initial charge transfer from porphyrin bridge to fullerene acceptor occurs at the picosecond scale. While we systematically overestimate charge transfer rates in M1 and M2, we reasonably reproduces rates in M3 and M4 when compared to experimental findings[43].

We further provide a time-resolved vibrational power spectrum which characterizes the nuclear vibrations occurring in our simulations. Our mode filtering technique provides a qualitative correlation of vibrational modes to the initial charge transfer process. By considering a subset of atoms from each triad, we can pinpoint which
nuclear motions have the strongest coupling to the electronic states. We find that conjugated aryl side groups on the porphyrin undergo dihedral rotations (lower energy) over ring breathing and ring distortions (higher energy). Despite a strong response to CT, we show these motions have very little effect on the electronic structure of the porphyrin at large. Conversely, aryl rings which link the bridge and acceptor units are shown to have little torsional behavior, and instead, nuclear motions take the form of ring distortions. Although this work focuses on charge migration from the bridge to acceptor, we still analyze the vibrations of the amide linking bridge and donor units. Here we find with M3 and M4 a torsional mode that is sensitive to the direction of electron flow. Finally, our analysis of bridge and acceptor moieties sees very little commonalities in nuclear dynamics between triads specific to the CT, despite the level of similarity in chemical structure. Nuclear energy is broadly distributed among high energy ring distortion modes in the bridge and low energy breathing modes in the acceptor.

Within our considerations in this work, we limit discussion to a qualitative relationship between vibrational modes and the electron transfer process without necessarily indicating dependency. Exploration via full quantum mechanical models would give detailed insight into the interplay between electronic and nuclear dynamics. Modes which show strong correlation may drive the CT process. We interpret anticorrelated modes here as having no activity during CT (perhaps even deactivated by CT). Recent experiments show the reverse occurring in systems with acetylide bridges. Selective vibrational excitation effectively disables CT in these DBA systems entirely[86].

Several quantum models implemented by Bittner et. al. study OPV's and charge transfer properties[87, 81]. Such models consider electronic states accompanied by
a small set of vibrational modes for acceptor, bridge (if included), and donor units and can reasonably recreate certain photophysical phenomena seen in experiment. With the vibrational analysis presented here, we begin the work to parameterize these models in a more robust sense, expanding the number of modes considered and differentiating the modes for each molecular unit. Furthermore, we can separate modes which have a marked effect on the electronic structure of the system versus modes which can be relegated to a phonon bath. What remains missing is the electronvibration coupling parameter which is certainly a non-trivial computation.

## Future Work

Marcus postulated that for larger ions, the change in electric field associated with charge transfer is smaller as the new charges are distributed over a larger volume of space[3]. As a result, there is less energy associated with the reorganization of solvent molecules, but the local system must undergo a more extensive rearrangement in response to new charges. For this work, we assumed solvent response would be minimal with respect to this charge transfer process and therefore excluded them. This not only eases computation but allows us to observe the vibrational response of the triads without interference.

We do, however, recognize the importance of inclusion of solvents. The addition of nuclear degrees of freedom provides an energy sink that can pull vibrational energy out of the system. This will either reduce some vibrational noise (modes associating with CT will remain active) or restrict the system from specific modes (torsional and breathing, for example) due to crowding. Polar molecules would stabilize any charge that emerges and the associated drop in energy may provoke more charge transfer
than the $0.35 q$ that we see. Inclusion of this interaction proves to be a non-trivial task in the TINKER software, however, as there is no explicit interaction term in the PPP Hamiltonian with solvent dipoles or external electric fields. Such interactions are currently only indirect: MM force fields of the solvent interact with those of the system. Direct interaction of the electronic structure with solvent molecules can be done if the choice of solvent has $\pi$ conjugation. This would entail quantum mechanical treatment of $\pi$ electrons in explicit solvent molecules and while this will increase computational cost, it is still a feasible computation in the TINKER software.

In the previous chapter, we briefly discuss an increase in ensemble size for the purpose of reducing vibrational noise and producing more consistent mode correlation from STFT. In our limited sample size here, choosing temporally similar trajectories required that we poll around the average case (the most populous region in the rate distribution). Vibrational analysis of this set allows us to qualitatively discuss modes which are relevant to CT. However, an increase in the ensemble size would give rise to even more trajectories which exhibit slow or fast CT. We can then analyze the extreme case sub-ensembles and investigate vibrational mode involvement in the retardation or hastening of CT.

The overall CT behavior for each trajectory is highly sensitive to initial configuration, and an exhaustive examination over every degree of freedom would require enormous computation effort. A large enough ensemble size would also present a sufficient training data set for the development of a machine learning model. Such a model could determine whether the charge transfer behavior in these triads is predictable and if so, identify key features (initial geometries, dihedral angles, excitation energies, and vibrational modes) that lead to optimal charge transfer properties.

## Appendix A

## Codes

## A. 1 Added Keywords

EXCITES [int] - Perform CI-S singlet excitations. Integer indicates the excitation number.

EXCITET [int] - Perform CI-S triplet excitations. Integer indicates the excitation number. (Experimental)

TDHF

- Use Time-Dependent Hartree-Fock and density matrix evolution.

TDHFCR [real] - Sets the screening radius for Yukawa-like interaction in Hartree-Core calculation.

TDHFDEBUG

- Increase verbosity of TDHF output.

USEURHF - Use unrestricted Hartree-Fock method. By default, THDF will use restricted HF. (Experimental)

PRINTEVERY [int] - Output frequency of TDHF. Integer defines number of iterations between TDHF data outputs.

PROBCURR

RESUME

- Compute the probability current at each quantum-active site. (Experimental)
- Import data from previous calculation and resume from there. (Experimental)


## A. 2 cicalc.f

1
!

subroutine cicalc

16

21

```
use sizes
    use atoms
        use bndstr
        use civars
        use iounit
        use piorbs
        use units
```

```
    to see if TDHF is requested
    use tdhfvars
    !----------------------------------------
    implicit none
! cicalc variables
! index variables
    integer i,j,k,l,m,ma,iip,iorb,jorb,iir
    integer ih,ie
    integer nv,nc,nci,nci_max,nl,nu
            nv - num valence orbitals
            nc - num condunting orbitals
            nci - total CI interactions
            nci_max - maximum calculated CI interactions
            nl - lower limit (for systems w/ <10 oribtals)
            nu - upper limit (for systems w/ <10 orbitals)
    parameter(nv = 20, nc = 20, nci_max = nv*nc)
    integer iconfig(nci_max,2)
        keeps track of configurations
            (n-9,n+1)
            (n-9,n+2)
                . . .
            (n-9,n+10)
            (n-8,n+1)
                ...
            (n,n+10)
    real*8 hfoc(norbit)
    real*8 exciton(norbit),tranvect(norbit)
    real*8 hodens(norbit), eldens(norbit)
```

```
!
! real*8 nco3(norbit,norbit),nco4(norbit,norbit)
real*8 nhf(norbit),nh(norbit), ne(norbit)
real*8 dens(norbit,norbit)
real*8 cibcm(norbit,norbit)
real*8 hcst(norbit,norbit),gst(norbit,norbit)
```

61
real*8, allocatable : d (:)
real*8, allocatable : work(:)
real*8, allocatable : : evec (:,:)
integer lwork,info
d - eigenvalues of CI hamiltonian
work - work variable
Density matrix (State Rep)
real *8 stds(norbit, norbit)

```
! New Coherences variables
    integer r,s,o,kd
        nl = max(ci_nfill - nv + 1, 1)
        nu = min(ci_nfill + nc, norbit)
        nci = (ci_nfill - nl + 1)*(nu - ci_nfill)
        lwork = 32*nci
    307 format(X,A9, I3)
    write(ciout,307) 'ci_nfill:\sqcup', ci_nfill
    write(ciout,307) 'nl:பபபபபபப', nl
    write(ciout,307) 'nu:பபபபபபப', nu
    write(ciout, 307) 'norbit: பபப', norbit
    write(ciout,307) 'nci: பபபபபப', nci
    write(ciout,307) 'iex:பபபபபப', iex
    write(ciout,*)
    if(iex.lt.1 .or. iex.gt.nci) then
    write(ciout,*) 'Invalid\sqcupexcitation \number'
    call fatal
    end if
! Allocate orbitals according to the CI interactions
    allocate (sing(nci,nci))
    allocate (trip(nci,nci))
    allocate (d(nci))
    allocate (work(lwork))
    allocate (evec(nci,nci))
!-----Test Print 10/8/16----------
```


do $i=1$, norbit
write(ciout,*) i, ci_en(i)
end do
!-----End Test Print---------------

121 !

126

131
sum over molecular orbitals
$m=0$
do $i=n l, \quad c i \_n f i l l$
do j=ci_nfill+1, nu
$m=m+1$
iconfig(m,1) = i
iconfig(m,2) $=j$
qxsum $=0.0 \mathrm{dO}$
qysum $=0.0 \mathrm{do}$
qzsum $=0.0 \mathrm{dO}$
! transitions before CI
$q x(m)=0.0 d 0$
$q y(m)=0.0 d 0$
$q z(m)=0.0 d 0$

136
do iip = 1, norbit
iorb = iorbit(iip)
qxsum $=q x s u m+c i_{\_} v(i i p, i) * c i \_v(i i p, j) * x(i o r b)$
qysum $=$ qysum $+c i_{-} v(i i p, i) * c i_{-} v(i i p, j) * y(i o r b)$
qzsum $=q z s u m+c i_{\_} v(i i p, i) * c i \_v(i i p, j) * z(i o r b)$
end do
$q x(m)=q x s u m$
qy $(\mathrm{m})=$ qysum
$q z(m)=q z s u m$

146

```
        ma = 0
```

```
construct CI Hamiltonian for singlet and triplet
```

construct CI Hamiltonian for singlet and triplet
do k = nl,ci_nfill
do k = nl,ci_nfill
do l = ci_nfill+1,nu
do l = ci_nfill+1,nu
ma}=ma+
ma}=ma+
Jint = 0.0d0
Jint = 0.0d0
Kint = 0.0d0
Kint = 0.0d0
do iip=1,norbit
do iip=1,norbit
s1 = 0.0d0
s1 = 0.0d0
s2 = 0.0d0
s2 = 0.0d0
do iir = 1, norbit
do iir = 1, norbit
s1 = s1 + ci_gamma(iip,iir)*ci_v(iir,j)*
s1 = s1 + ci_gamma(iip,iir)*ci_v(iir,j)*
>
>
>
>
Original
Original
sing(m,ma) = - Jint + 2.0dO*Kint
sing(m,ma) = - Jint + 2.0dO*Kint
sing(ma,m) = sing(m,ma)
sing(ma,m) = sing(m,ma)
trip(m,ma)=-Jint
trip(m,ma)=-Jint
trip(ma,m) = - Jint
trip(ma,m) = - Jint
end do
end do
end do
end do
sing(m,m)=sing(m,m) + (ci_en(j)-ci_en(i))
sing(m,m)=sing(m,m) + (ci_en(j)-ci_en(i))
trip(m,m) = trip(m,m) + (ci_en(j)-ci_en(i))
trip(m,m) = trip(m,m) + (ci_en(j)-ci_en(i))
end do

```
    end do
```

```
            end do
    !-----Test Print--------
    ! Need to see what all the values in iconfig mean
    write(ciout,*) "ப\sqcupm\sqcupபபபபiபபபj"
    999 format(i5,i5, 'ப->>'',i5)
            do i=1,m
                write(ciout, 999) i, iconfig(i,1), iconfig(i,2)
            end do
    write(ciout,*) ,'
    !-----End Test Print----
        !
    Print the CI Hamiltonians
    !
    302 format(E13.5)
    if(usesinglet) then
        write(ciout,*) "CI}S\mathrm{ SingletьHamiltonian"
        do i=1,nci
                do j=1,nci
                    write(ciout, 302, advance='no') sing(i,j)
                end do
                write(ciout,*) ,'
        end do
            end if
            if(usetriplet) then
            write(ciout,*) "CI吕ripletьHamiltonian"
            do i=1,nci
                do j=1,nci
                write(ciout, 302, advance='no') trip(i,j)
            end do
```

```
            write(ciout,*) ,'
            end do
end if
write(ciout,*)
Get the eigensystem, print
if(usesinglet) then
    call dsyev('V','U',nci,sing,nci,d,work,lwork,info)
At this point 'sing' holds the eigenvectors
Copy them to 'evec'
    do i=1,nci
        do j=1,nci
                evec(i,j) = sing(i,j)
            end do
    end do
    write(ciout,*) 'CI
end if
if(usetriplet) then
    call dsyev('V','U',nci,trip,nci,d,work,lwork,info)
At this point 'trip' holds the eigenvectors
Copy them to 'evec'
    do i=1,nci
        do j=1,nci
                evec(i,j)=trip(i,j)
        end do
    end do
    write(ciout,*) 'CI
end if
```

241

```
Print out the energies
format(i5,2f12.6)
do i=1,min(20,nci)
    write(ciout,303) i,d(i)*evolt
    end do
    write(ciout,*)
    Analyse CI states
    if(usesinglet) then
    write(ciout,*) 'Analysis\sqcupof Singlet\sqcupStates'
    else if(usetriplet) then
    write(ciout,*) 'Analysis\sqcupof \sqcupTriplet\sqcupStates'
    end if
    do i=1,min(20,nci)
    do i=1,nci
        qxsum = 0.0d0
        qysum = 0.0d0
        qzsum = 0.0d0
```

        do \(j=1, n c i\)
            \(q x s u m=q x s u m+\operatorname{evec}(j, i) * q x(j)\)
            qysum \(=\) qysum \(+\operatorname{evec}(j, i) * q y(j)\)
            qzsum \(=q z s u m+\operatorname{evec}(j, i) * q z(j)\)
        end do
        qtot \(=\) qxsum*qxsum \(+q y s u m * q y s u m ~+~ q z s u m * q z s u m ~\)
        fosci \(=0.0875161 * q t o t * d(i)\)
        if(fosci.lt.10.0d0**(-90)) fosci \(=0.0 \mathrm{dO}\)
    !
    !
write(ciout, 304) i,d(i)*evolt,fosci

write(ciout, 305) qxsum, qysum, qzsum, sqrt(qtot)

2 x, ' $\mathrm{qtot}_{\sqcup}={ }_{\sqcup}$ ', e12.6)

do $j=1, n c i$
if (evec(j,i)**2.gt.0.1) then
write(ciout,'(i3," - $^{->", i 3,3 x, f 12.6,3 x, f 12.6) ') ~}$
$>$
$>$
$>$
end if
end do
write(ciout,*)
end do
Modify electron densitites for excitations.
He were use the assumption that the CI(S)
state add and subtract single electron
density from the ci_ed(i,j) matrix
May need iex here.
! First construct the density matrix using
! the CI coefficients for iex in MO basis

```
    do i=1,norbit
        do j=1,norbit
        dens(i,j) = 0.0d0
        end do
    end do
    do m=1,nci
    i = iconfig(m,1)
    j = iconfig(m,2)
    dens(i,j) = evec(m,iex)
    end do
    write(ciout,*) 'CI\sqcupEigenvectors'
    do i=1,nci
        write(ciout,306) (evec(i,j),j=1,nci)
        end do
        write(ciout,*)
        306 format(8f12.6)
    write(ciout,*) 'CI
    do i=1,norbit
        write(ciout, 306) (dens(i,j),j=1,norbit)
        end do
    write(ciout,*)
    At this point, we have the CI density matrix in the local orbital basis.
    Now we need to write the populations in the orbital basis. For this, we
    first determine the orbital population changes
    do i=1,norbit
    nhf(i) = 0.0d0
```

```
    nh(i) = 0.0d0
    ne(i) = 0.0d0
    if(i.le.ci_nfill) then
        if(usetdhf) then
            nhf(i) = 1.0d0
        else
            nhf(i) = 2.0d0
        end if
    end if
end do
do ih = nl,ci_nfill
    sum = 0.0d0
    do ie = ci_nfill+1,nu
        sum = sum + dens(ih,ie)**2
    end do
    nh(ih) = sum
end do
do ie=ci_nfill+1,nu
    sum = 0.0d0
    do ih=nl,ci_nfill
        sum = sum + dens(ih,ie)**2
    end do
    ne(ie) = sum
end do
! Check: write the occupations over the range nl->nu
    308 format(I3,4F13.5)
write(ciout,*) "State}\sqcup\mathrm{ Populations 
```



```
do k=nl,nu
```

```
            write(ciout,308) k,nhf(k),nh(k),ne(k),nhf(k)+ne(k)-nh(k)
end do
```


The state populations might be inherently included
in the CI eigenvectors. So lets take the eigenvector
and use that to populate coherences and diagonals.
start with the state representation
do o=1, norbit ! state
do m=1, norbit ! state
sum1 $=0.0 \mathrm{~d} 0$
$\operatorname{stds}(o, m)=0.0 d 0$
do i=nl,ci_nfill ! hole 1
do j=ci_nfill+1,nu ! elec 1
do k=nl,ci_nfill ! hole 2
do l=ci_nfill+1,nu ! elec 2
$\mathrm{kd}=0$
if(l.eq.o .and. i.eq.k . and. m.eq.j) then
$\mathrm{kd}=\mathrm{kd}+1$
end if
if(l.eq.j . and. k.eq.m.and. o.eq.i) then
$k d=k d-1$
end if
if(l.eq.j .and. i.eq.k. and. o.eq.m) then
if(o.le.ci_nfill) kd = kd+1
end if
sum1= sum1 + float(kd)*dens (i,j)*dens(k,l)
end do
end do

```
            end do
        end do
        stds(o,m) = sum1
        end do
end do
```

401 !
unitary transform into site represenation
do $r=1$, norbit
do $s=1$, norbit
sum $=0.0 \mathrm{~d} 0$
do $o=1$, norbit
do $m=1$, norbit
sum $=\operatorname{sum}+\operatorname{stds}(o, m) * c i_{\_} v(r, o) * c i_{-} v(s, m)$
end do
end do
cibcm (r,s) = sum
end do
end do

do $i=1$, norbit
do j=1, norbit
write (ciout, 309, advance='no') stds (i, j)
end do
write(ciout, *) , '
end do
write (ciout, *) , '

```
    Print out the CI density/bond-charge matrix
    309 format(F13.5)
    write(ciout,*) 'Density/Bond-Charge
    do i=1,norbit
        do j=1,norbit
                write(ciout,309, advance='no') cibcm(i,j)
        end do
        write(ciout,*) ,'
    end do
    write(ciout,*) ',
```

    ! As a check, take a look at the changes in the bond-orders.
    ! These will go in to the forcefield calculation next.
    
do k=1, nbpi
$\mathrm{p}=\mathrm{pnpl}(\mathrm{k})$
$\mathrm{i}=\mathrm{ibpi}(2, k)$
j $=$ ibpi (3,k)
if(usetdhf) then
if(useurhf) then
pnpl(k) = realpart(cibcm(i,j) + tdhfedb(i,j))
else
pnpl(k) = realpart(cibcm(i,j) + 0.5d0*tdhfed(i,j))
end if
!-----Test 03.20.17----
pbpl(k) $=$ pnpl(k)*ci_hc(i,j)/(-0.0757d0)
!--------------------------
else
pnpl(k) = cibcm(i,j)
!-----Test 03.20.17----
pbpl(k) $=$ cibcm(i,j)*ci_hc(i,j)/(-0.0757d0)

```
    !-------------------------
    end if
    i = ibnd(1,ibpi(1,k))
    j = ibnd(2,ibpi (1,k))
```

```
            write(ciout,'(5i5,2f12.2)') k,ibpi(2,k),ibpi(3,k),i,j,p,pnpl(k)
        end do
write(ciout,*)
If needed, update the TDHF electron density matrix
    if(usetdhf) then
            write(ciout,*)
            write(ciout,*) 'Updating}\mp@subsup{|}{\bulletDHF}{\sqcup
            write(ciout,*)
            do i=1, norbit
                do j=1, norbit
                    if(useurhf) then
                        tdhfeda(i,j) = cibcm(i,j)
            call flush(ciout)
            end subroutine
```


## A. 3 ciinnit.f

! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
$!$
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
\#\# \#\#
\#\# subroutine ciinit -- checks for keyword "EXCITES" or \#\#
\#\# "EXCITET" for single or triplet \#\#
\#\# calculations respectively, then \#\#
\#\# initializes necessary values \#\#
\#\# \#\#
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
"ciinit" checks for the keyword "EXCITES" or "EXCITET" which
decides whether to do excited state calculations
'EXCITES' - singlet
'EXCITET' - triplet
subroutine ciinit
use sizes
use keys
use civars
logical exist
integer i, next, freeunit
character*20 keyword
character*120 record, string
character $* 120$ cifile

```
usesinglet = .false.
usetriplet = .false.
do i=1,nkey
    next = 1
    record = keyline(i)
    call gettext (record,keyword,next)
    call upcase (keyword)
    if(keyword(1:8) .eq. 'EXCITES\sqcup') then
        usesinglet = .true.
        usetriplet = .false.
        ciout = freeunit()
        cifile = 'ci.sing.debug'
        string = record(next:120)
        iex = 0
        read(string,*,err=10, end=10) iex
        continue
    else if(keyword(1:8) .eq. 'EXCITET\sqcup') then
        usesinglet = .false.
        usetriplet = .true.
        ciout = freeunit()
        cifile = 'ci.trip.debug'
        string = record(next:120)
        iex = 0
        read(string,*,err=11, end=11) iex
        continue
    end if
end do
open the CI debug file
if(usesinglet.or.usetriplet) then
    inquire(file=cifile,exist=exist)
```

```
! ## ##
! #############################################################
    !
    ! \#\# \#\#
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
\(!\)
\(!\)
\(!\)
```

```
! maxkey maximum number of lines in the keyword file
```

! maxkey maximum number of lines in the keyword file
! nkey number of nonblank lines in the keyword file
! nkey number of nonblank lines in the keyword file
! keyline contents of each individual keyword file line
! keyline contents of each individual keyword file line
! maxkey maximum number of lines in the keyword file
! nkey number of nonblank lines in the keyword file
! keyline contents of each individual keyword file line

```
```

- 

```




1 !
!
 \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# \#\# \#\# module civars -- contents of the CI singlet and \#\# \#\# triplet calculations \#\#
\(!\)

```

            open(unit=ciout, file=cifile,status='old')
    ```
            rewind (ciout)
            else
            open(unit=ciout, file=cifile, status='new')
            end if
end if
write(ciout, *) 'ciபsing: ', usesinglet
write(ciout, *) 'ciчtrip: \(\quad\) ', usetriplet
return
end

\section*{A. 4 civars.f}
if(exist) then

\section*{A. 5 fullpi.f}

1 !
\(!\)
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# \# \# \#\#
! \#\# subroutine fullpi -- replaces subroutine pical! \#\#
! \#\# because the given routine does not \#\#
! \#\# include the whole pi system \#\#
! \#\# together in one calculation \#\#
! \# \# \#\#
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

11 !
\(!\)
! "picalc" performs a modified Pariser-Parr-Pople molecular
```

! orbital calculation for each conjugated pi-system. The
! implication here is that the pi-systems, then, do not
! interact with each other except by force fields (MM). As a
! result, there are no population dynamics between pi-systems.
!
! "fullpi" does the same calculation, but treats all pi orbitals
! as a single large pi-system
21
! for tdhf calculations
use tdhfvars
! for CI calculations
use civars
implicit none
integer i,j,k,m,ib,i!
integer ii,jj,kk
integer iorb,jorb
integer ncalls
data ncalls / 0 /

```
```

! only needs to be done if pisystem is present

```
    !
    if (norbit.eq. 0) return
56
    ! compute MOs for full pisystem
    \(!\)
        norbit \(=0\)
        do \(\mathrm{i}=1, \mathrm{nconj}\)
        do \(j=i \operatorname{conj}(1, i), i \operatorname{conj}(2, i)\)
            norbit = norbit + 1
            iorbit(norbit) \(=k \operatorname{conj}(j)\)
            end do
        end do
    66
        ! find and store the pisystem bonds for this pisystem
        !

    nbpi \(=0\)
        \(k k=i \operatorname{conj}(2, i)-i \operatorname{conj}(1, i)+1\)
        do ii \(=1\), norbit-1
        iorb = iorbit(ii)
        do jj = ii+1, norbit
```

            jorb = iorbit(jj)
                do k = 1, n12(iorb)
                if (i12(k,iorb) .eq. jorb) then
                    nbpi = nbpi + 1
                    do m = 1, nbond
                    if (iorb.eq.ibnd(1,m) . and.
                    jorb.eq.ibnd(2,m)) then
                        ibpi(1,nbpi) = m
                            ibpi(2,nbpi) = ii
                                    ibpi(3,nbpi) = jj
                                    goto 10
                end if
                    end do
                        continue
            end if
        end do
            end do
            end do
    !--------------------------------------------------------------------------
!--------------new code------------------------------------------------
Point of this code is to find pi-atoms within a certain
distance of each other and consider them pi-bonded.
This will allow for inter-pisystem coupling and therefore
population dynamics therewithin. This should hold for
molecular systems with unconnected pisystems and
pairs of molecules that are within proximity.
nbpi = 0
do i = 1, norbit-1
iorb = iorbit(i)
do j = i+1, norbit

```
```

        jorb = iorbit(j)
                nbpi = nbpi + 1
                do m = 1, nbond
                        ibpi(1,nbpi) = m
                        ibpi(2,nbpi) = i
            ibpi(3,nbpi) = j
                end do
                end do
        end do
        Notes:
        bohr - ratio of Bohr/Angstrom
    !------------------------------------------------------------------------
121 C
! find and store the pisystem torsions for this pisystem
c
ntpi $=0$
do ii $=1$, ntors
ib $=$ itors(2,ii)
ic $=$ itors (3,ii)
if (listpi(ib) .and. listpi(ic)) then
do $j \mathrm{j}=1, \mathrm{nbpi}$
$\mathrm{k}=\mathrm{ibpi}(1, \mathrm{j} j)$
if (ib.eq.ibnd (1,k).and.ic.eq.ibnd (2,k) .or.
\& ib.eq.ibnd (2,k).and.ic.eq.ibnd(1,k)) then
ntpi = ntpi + 1
itpi(1,ntpi) = ii
itpi(2,ntpi) = jj
goto 20
end if

```
```

                    end do
    20
continue
end if
end do
!
! print a header for the molecular orbital calculation
30
\& '\sqcupOrbitals员')
else
write (iout, 40) i
40 format (/,'ьModified\sqcupPariser-Parr-Pople\sqcupMOs\sqcupfor',
\& '\sqcupPi-System',i4,'ь:')
end if
end if
156 !
! get SCF-MOs, then scale bond and torsional parameters
need to see if TDHF is requested
if(usetdhf . and. .not. tdhffirst) then
if(useurhf) then
call pitduhf
else
call pitdrhf
end if
else
call fullpiscf

```
```

if CI calculations are requested
if(usesinglet.or.usetriplet) call cical!

```

171

176

181 !
!
\(!\) ! \# subroutine fullpiscf -- SCF molecular orbital \#\# \#\# calculation \#\# \#\# \#\#
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# "piscf" performs an SCF molecular orbital calculation for a pisystem to determine bond orders used in parameter scaling "fullpiscf" is a modificaion of "piscf" that fills in off diagonal terms that allow for intermolecular/interpisystem interactions
subroutine fullpiscf
!-------------------------------------------------
! for the initialization of tdhf variables
            use tdhfvars
            use civars
```

use sizes
use atomid
use atoms
use bndstr
use couple
use inform
use iounit
use orbits
use piorbs
use pistuf
use units

```
implicit none
integer i,j,k,m
    integer iter,maxiter
    integer iatn,jatn
    integer iorb,jorb,nfill
    real*8 delta, converge
    real*8 xij,yij,zij,p
    real*8 hcii,gii,gij
    real*8 g11,g11sq,g12,g14
    real*8 rij, erij,brij
    real*8 ovlap, covlap
    real*8 cionize
    real*8 iionize, jionize
251
    real*8 rijsq,hcij,qi
    real*8 total, totold
    real*8 ebeta, aeth, abnz
    real*8 ebe, ebb,ble,blb
    real*8 eebond,bebond
    real*8 s1,s2,gjk
    real*8 vij, vik, vmj, vmk
    real*8 xi, xj, xk, xg
    real*8, allocatable :: povlap(:,:)
    real*8, allocatable : en (:)
    real*8, allocatable :: ip(:)
    real*8, allocatable : : fock(:,:)
    real*8, allocatable : : hc (:,:)
    real*8, allocatable :: v(:,:)
    real*8, allocatable : gamma(:,:)
    real*8, allocatable :: ed(:,:)
    character*6 mode
!-----Testing Variables----------------------------
    real*8, allocatable :: FR(:,:)
    real*8, allocatable : : RF(:,:)
    integer testout
        allocate (FR(norbit, norbit))
        allocate (RF(norbit, norbit))

```

maxiter maximum number of SCF iterations
converge criterion for SCF convergence
ebeta value of resonance integral for ethylene
cionize ionization potential of carbon (Hartree)
266 !
! ebb equilibrium bond energy in benzene
aeth the P-P-P constant "a" in ethylene
abnz the P-P-P constant "a" in benzene
ble equilibrium bond length in ethylene
blb equilibrium bond length in benzene
ebe = 129.37d0
ebb = 117.58d0
aeth = 2.309d0
abnz=2.142d0
ble = 1.338d0
blb=1.397d0
!
! perform dynamic allocation of some local arrays
291 !
allocate (povlap(norbit,norbit))

```
```

    allocate (en(norbit))
    allocate (ip(norbit))
    allocate (fock(norbit,norbit))
    allocate (hc(norbit,norbit))
    allocate (v(norbit,norbit))
    allocate (gamma(norbit,norbit))
    allocate (ed(norbit,norbit))
    assign empirical one-center Coulomb integrals, and
    first or second ionization potential depending on
    whether the orbital contributes one or two electrons
    nfill = 0
    do i = 1, norbit
    iorb = iorbit(i)
    gamma(i,i) = emorb(iorb)
    ip(i) = worb(iorb) + (1.0d0-qorb(iorb))*emorb(iorb)
    nfill = nfill + nint(qorb(iorb))
    end do
nfill = nfill / 2
calculate two-center repulsion integrals
according to Ohno's semi-empirical formula
do i = 1, norbit-1
iorb = iorbit(i)
gii = gamma(i,i)
do j = i+1, norbit
jorb = iorbit(j)
g11 = 0.5d0 * (gii+ gamma(j,j))
g11sq = 1.0d0 / g11**2

```
```

xij = x(iorb) - x(jorb)
yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rijsq = (xij**2 + yij**2 + zij**2) / bohr**2
g12 = 1.0d0 / sqrt(rijsq+g11sq)
gamma(i,j) = g12
gamma(j,i) = g12

```
! the first term in the sum to find alpha is the first
or second ionization potential, then the two-center
repulsion integrals are added
do \(i=1\), norbit
    hcii \(=i p(i)\)
    do \(j=1\), norbit
        if (i .ne. j) then
            jorb \(=\) iorbit(j)
            hcii \(=\) hcii - qorb (jorb) \(* \operatorname{gamma}(i, j)\)
        end if
    end do
    hc(i,i) = hcii
end do
```

356 !
! ----Original Code--------------
!
! get two-center repulsion integrals via Ohno's formula
361 ! do k = 1, nbpi
i = ibpi(2,k)
j = ibpi(3,k)
do i = 1, norbit-1
do j = i+1, norbit
iorb = iorbit(i)
jorb = iorbit(j)
iatn = atomic(iorb)
jatn = atomic(jorb)
xij = x(iorb) - x(jorb)
yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rij = sqrt(xij**2 + yij**2 + zij**2)
rijsq = rij**2 / bohr**2
g11=0.5d0*(gamma(i,i)+gamma(j,j))
g11sq}=1.0d0/g11**
g12= gamma(i,j)
compute the bond energy using a Morse potential
erij = aeth * (ble-rij)
brij = abnz * (blb-rij)
eebond = (2.0d0*exp(erij)-exp(2.0dO*erij)) * ebe / hartree
bebond = (2.0dO*exp(brij)-exp(2.0dO*brij)) * ebb / hartree

```

```

! hc(i,j) = hcij
! hc(j,i) = hcij
! end do
! end do

```
!-----Test Code 11.04.16---------------------------------------------
! Check if a particular pair is bonded. If so, do hc calcs
! as normal. If not, apply the calculation and scale it
    by Yukawa.

    do \(k=1, \mathrm{nbpi}\)
            \(i=i b p i(2, k)\)
            j = ibpi(3,k)
    do i = 1, norbit-1
    do \(j=i+1\), norbit
        iorb \(=\) iorbit(i)
        jorb \(=\) iorbit(j)
        iatn \(=\) atomic(iorb)
        jatn \(=\) atomic(jorb)
        xij \(=x(i o r b)-x(j o r b)\)
        yij \(=y(i o r b)-y(j o r b)\)
        zij \(=z(i o r b)-z(j o r b)\)
        rij \(=\operatorname{sqrt(xij**2+yij**2+zij**2)~}\)
        rijsq \(=\) rij**2 / bohr**2
        \(\operatorname{g11}=0.5 \mathrm{~d} 0 *(\operatorname{gamma}(\mathrm{i}, \mathrm{i})+\operatorname{gamma}(j, j))\)
            \(\mathrm{g} 11 \mathrm{sq}=1.0 \mathrm{~d} 0 / \mathrm{g} 11 * * 2\)
            \(\mathrm{g} 12=\operatorname{gamma}(\mathrm{i}, \mathrm{j})\)
        !
    ! compute the bond energy using a Morse potential
!
```

            erij = aeth * (ble-rij)
            brij = abnz * (blb-rij)
            eebond = (2.0d0*exp(erij)-exp(2.0d0*erij)) * ebe / hartree
            bebond = (2.0d0*exp(brij)-exp(2.0d0*brij)) * ebb / hartree
    ```
```

    g14 = 1.0d0 / sqrt(4.0d0*rijsq+g11sq)
    hcij = 1.5d0*(bebond-eebond) - 0.375d0*g11
    \&
+(5.0d0/12.0d0)*g12 - g14/24.0d0
if either atom is non-carbon, then factor the resonance
integral by overlap ratio and ionization potential ratio
if (iatn.ne.6 .or. jatn.ne.6) then
call overlap (iatn,jatn,rij,ovlap)
call overlap (6,6,rij,covlap)
hcij = hcij * (ovlap/covlap)
iionize = ip(i)
if (qorb(iorb) .ne. 1.0d0) then
if (iatn .eq. 7) iionize = 0.595d0 * iionize
if (iatn .eq. 8) iionize = 0.525d0 * iionize
if (iatn .eq. 16) iionize = 0.89d0 * iionize
end if
jionize = ip(j)
if (qorb(jorb) .ne. 1.0d0) then
if (jatn .eq. 7) jionize = 0.595d0 * jionize
if (jatn .eq. 8) jionize = 0.525d0 * jionize
if (jatn .eq. 16) jionize = 0.89d0 * jionize
end if

```
```

                hcij = hcij * (iionize+jionize)/(2.0dO*cionize)
            end if
    481 !
! See if this pair of orbitals is bonded.
bonded = .false.
do k=1, nbpi
iorb = ibpi(2,k)
jorb = ibpi(3,k)
bonded = (iorb.eq.i . and. jorb.eq.j) .or. bonded
end do
if(.not.bonded) then
4 9 1
900
hcij = hcij*(exp(-1.0d0*rij/tdhfcr))/rij
format(2i3,L5,E12.5)
end if
!---------------------------------------------------------
!
! set symmetric elements to the same value
!
hc(i,j) = hcij
hc(j,i) = hcij
end do
end do
!---------------------------------------------------------------------
!
506 !
construct an initial guess to the Fock matrix
!
do i = 1, norbit
do j = 1, norbit

```
```

            fock(j,i) = hc(j,i)
    ! sets. Print out iteration number, energy, and delta
    testout=99
    open(unit=testout,file='SCF.out')
    do while (mode.eq.'PLANAR' .or. mode.eq.'NONPLN')
    if (mode .eq. 'NONPLN') then
                        call fulltilt (povlap)
                do k = 1, nbpi
                    i = ibpi(2,k)
                    j = ibpi(3,k)
                do i = 1, norbit-1
                do j = i+1, norbit
                    hc(i,j) = hc(i,j) * povlap(i,j)
                    hc(j,i) = hc(i,j)
            end do
                end do
            end if
        perform SCF iterations until convergence is reached; diagonalize
    ```
```

5 4 1
! next "f" matrix assuming zero differential overlap except for
! one-center exchange repulsions
!
!-----Test Code 31-Mar-18----------------------------------------------
write(testout,*) mode

```

```

    910 format(I4,E12.5,F17.5)
    ```

551
```

iter $=0$
delta $=2.0 \mathrm{dO} *$ converge
do while (delta.gt.converge .and. iter.lt.maxiter) iter = iter + 1 call jacobi (norbit,fock,en,v) do i = 1, norbit do j = i, norbit $s 1=0.0 \mathrm{~d} 0$ $\mathrm{s} 2=0.0 \mathrm{~d} 0$
gij = gamma(i,j)
do k = 1, nfill
s2 = s2 - v(i,k)*v(j,k)*gij
if (i .eq. j) then
do m = 1, norbit
s1 = s1 + 2.0d0*gamma(i,m)*v(m,k)**2
end do
end if
end do
fock(i,j) = s1 + s2 + hc(i,j)
fock(j,i) = fock(i,j)

```
```

            end do
            end do
    !
    576 !
! repulsion integrals, "xk" sums the molecular exchange
repulsion integrals, and "xg" sums the nuclear repulsion
xi = 0.0d0
xj = 0.0d0
xk = 0.0d0
xg = 0.0d0
do i = 1, nfill
do j = 1, norbit
vij = v(j,i)
do k = 1, norbit
vik = v(k,i)
gjk = gamma(j,k)
xi = xi + 2.0dO*vij*vik*hc(j,k)
do m = 1, nfill
vmj = v(j,m)
vmk = v(k,m)
xj = xj + 2.0dO*vij*vij*vmk*vmk*gjk
xk = xk - vij*vmj*vik*vmk*gjk
end do
end do
end do
end do
do i = 1, norbit-1
iorb = iorbit(i)
qi = qorb(iorb)

```
```

do j = i+1, norbit
jorb = iorbit(j)
xg = xg + qi*qorb(jorb)*gamma(i,j)

```

606
end do
end do
total \(=x i+x j+x k+x g\)
if (iter .ne. 1) delta = abs (total-totold)
totold \(=\) total

write(testout, 910) iter, total, delta

end do

616 !
! print warning if \(S C F-M O\) iteration did not converge
!
if (delta .gt. converge) then
write (iout, 10)

621

\&
call fatal
end if

626 !
! calculate electron densities from filled MO's
\(!\)

631
```

            do i = 1, norbit
            do j = 1, norbit
                ed(i,j) = 0.0d0
                        do k = 1, nfill
                        ed(i,j) = ed(i,j) + 2.0d0*v(i,k)*v(j,k)
                    end do
    ```
```

            end do
            end do
    ```

636
```

        print out results for the SCF computation
        if (verbose) then
    if (mode .eq. 'PLANAR') then
        write (iout,20)
    ```

```

        else
            write (iout,30)
                            3 0
                            &
        end if
        write (iout,40) total,norbit,delta,iter
    40 format (/,'ьTotalьEnergy',11x,f12.4,

```
\&
\&
```

            format (/,', SCF-MO\sqcupCalculation ffor\sqcupNon-Planar',
                                    'ьSystem
        /,'ьNumberьof чOrbitals',5x,i12,
        /,'ьConvergence', 12x,d12.4,
                /,'\sqcupIterations', 13x,i12)
        write (iout,50) xi,xj,xk,xg
        format (/,'ьCoreчIntegrals',9x,f12.4,
        /,'ьCoulomb\sqcupRepulsion',6x,f12.4,
        /,'\sqcupExchange\sqcupRepulsion',5x,f12.4,
        /,'\sqcupNuclearьRepulsion',6x,f12.4)
        write (iout,60)
        format (/,'ьOrbitalьEnergies')
        write (iout,70) (en(i),i=1,norbit)
        format (8f9.4)
        write (iout,80)
        format (/,'\sqcupMolecularOrbitals') ! Intentionally removed
    ```
do i = 1, norbit write (iout, 90) (v(i,j), j=1, norbit)
format (8f9.4)
end do
write (iout, 100)
format (/,'பFock \({ }_{\sqcup}\) Matrix')
do \(i=1\), norbit
write (iout, 110) (fock(i,j), j=1, norbit)
format (8f9.4)
end do
write (iout, 120)
format (/,'๖DensityபMatrix')
do \(i=1\), norbit
write (iout, 130) (ed(i,j), j=1, norbit)
format (8f9.4)
end do
write (iout, 140)
format (/,'๖H-Core \({ }_{\sqcup}\) Matrix')
do \(\mathrm{i}=1\), norbit
write (iout, 150) (hc(i,j), j=1, norbit)
format (8f9.4)
end do
write (iout, 160)
format (/,'பGammaபMatrix')
do \(i=1\), norbit
write (iout, 170) (gamma(i, j), \(j=1\), norbit)
format (8f9.4)
end do
end if
```

    now, get the bond orders (compute p and p*b)
            if (verbose) then
                            write (iout,180)
    format (/,'\sqcupPisystem\sqcupBond\sqcupOrders')
        end if
        do k = 1, nbpi
            i = ibpi(2,k)
            j = ibpi(3,k)
            p = 0.0d0
            do m = 1, nfill
                p = p + 2.0d0*v(i,m)*v(j,m)
            end do
            if (mode .eq. 'PLANAR') then
                    pbpl(k) = p * hc(i,j)/ebeta
            else if (mode .eq. 'NONPLN') then
                pnpl(k) = p
            end if
            if (verbose) then
                i = ibnd(1,ibpi (1,k))
                j = ibnd(2,ibpi(1,k))
                write (iout,190) i,j,p
                format (3x,2i6,2x,f10.4)
            end if
        end do
            !
    ! if we have done planar calculation, do the nonplanar;
when both are complete, alter the pisystem constants
if (mode .eq. 'PLANAR') then

```
```

            mode = 'NONPLN'
        else if (mode .eq. 'NONPLN') then
        mode = ',பபபபபப'
            end if
    ```
```

end do
!-----------------------------------------------
close(unit=testout)
!-------------------------------------------------
!------------------------------------------------------
If using tdhf, we need to allocate and copy
over the matrices for propagation
write(iout,*) "usetdhf: ", usetdhf
if(usetdhf) then
tdhf_nfill = nfill
if(.not.allocated(tdhfhc)) then
allocate (tdhfhc (norbit, norbit))
end if
if(.not.allocated(tdhfgamma)) then
allocate (tdhfgamma(norbit,norbit))
end if
if(useurhf) then
if(.not.allocated(tdhfeda)) then
allocate (tdhfeda(norbit, norbit))
end if
if(.not.allocated(tdhfedb)) then
allocate (tdhfedb(norbit, norbit))
end if
if(.not.allocated(tdhffocka)) then

```
```

        allocate (tdhffocka(norbit,norbit))
        end if
    if(.not.allocated(tdhffockb)) then
        allocate (tdhffockb(norbit,norbit))
        end if
    else
    if(.not.allocated(tdhffock)) then
        allocate(tdhffock(norbit,norbit))
    end if
    if(.not.allocated(tdhfed)) then
        allocate(tdhfed(norbit,norbit))
    end if
    end if
    do i=1,norbit
    do j=1,norbit
        tdhfhc(i,j) = hc(i,j)
        tdhfgamma(i,j) = gamma(i,j)
        if(useurhf) then
            tdhfeda(i,j) = ed(i,j)*0.5d0
            tdhfedb(i,j) = ed(i,j)*0.5d0
            tdhffocka(i,j) = fock(i,j)
            tdhffockb(i,j) = fock(i,j)
        else
            tdhfed(i,j) = ed(i,j)
            tdhffock(i,j) = fock(i,j)
        end if
    end do
    end do
    end if

```
```

    !------------------------------------------------------------
    ! If using CI theory, we need to allocate and
    ```
```

copy over matrices: \{gamma, v, en\} to use
if (usesinglet. or. usetriplet) then
if (usetriplet) then
write(iout,*) 'Sorry, ¢CI-triplets\sqcupnot\sqcupavailable\sqcupright\sqcupnow.''
call fatal
end if

```

```

            write(ciout,*) "Allocating\sqcupCI\sqcupmatrices"
            if(.not.allocated(ci_gamma)) allocate (ci_gamma(norbit,norbit))
            if(.not.allocated(ci_v)) allocate (ci_v(norbit,norbit))
            if(.not.allocated(ci_en)) allocate (ci_en(norbit))
            if(.not.allocated(ci_ed)) allocate (ci_ed(norbit,norbit))
            if(.not.allocated(ci_hc)) allocate (ci_hc(norbit,norbit))
            ci_nfill = nfill
            write(ciout,*) "Populating\sqcupCI\sqcupmatrices"
            do i=1,norbit
                ci_en(i) = en(i)
                do j=1,norbit
            ci_v(i,j) = v(i,j)
            ci_gamma(i,j) = gamma(i,j)
            ci_ed(i,j) = ed(i,j)
            ci_hc(i,j) = hc(i,j)
            end do
            end do
            write(ciout,*) ,'
    end if
!------------------------------------------------------

```
```

821
! perform deallocation of some local arrays
deallocate (povlap)
deallocate (en)
deallocate (ip)
deallocate (fock)
deallocate (hc)
deallocate (v)
deallocate (gamma)
deallocate (ed)
return
end
836 !
!
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
! \#\# \#\#
! \#\# subroutine fulltilt -- direction cosines for pisystem \#\#
8 4 1
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
!
!
"fulltilt" calculates for each pibond the ratio of the
actual p-orbital overlap integral to the ideal overlap
if the same orbitals were perfectly parallel
performs the exact same calculation as PiTilt, but applies it
for all pi-atom pairs.

```
```

subroutine fulltilt (povlap)
use sizes
use atomid
use atoms
use couple
use piorbs
implicit none
integer i,j,k,m
integer iorb,jorb
integer list(8)
real*8 ideal,cosine,rnorm
real*8 xij,yij,zij,rij
real*8 a1,b1,c1,a2,b2,c2
real*8 x2,y2,z2,x3,y3,z3
real*8 xr(8),yr(8),zr(8)
real*8 povlap(norbit,norbit)
planes defining each p-orbital are in "piperp"; transform
coordinates of "iorb", "jorb" and their associated planes
to put "iorb" at origin and "jorb" along the x-axis
do k = 1, nbpi
i = ibpi(2,k)
j = ibpi(3,k)
do i=1, norbit-1
do j=i+1, norbit
iorb = iorbit(i)
jorb = iorbit(j)

```
```

            list(1) = iorb
            list(2) = jorb
            do m = 1, 3
            list(m+2) = piperp(m,iorb)
            list (m+5) = piperp(m,jorb)
            end do
            call pimove (list,xr,yr,zr)
                check for sp-hybridized carbon in current bond;
                    assume perfect overlap for any such pibond
            if ((atomic(iorb).eq.6 . and. n12(iorb).eq.2) .or.
                    & (atomic(jorb).eq.6 .and. n12(jorb).eq.2)) then
            povlap(i,j)=1.0d0
    896 !
! find and normalize a vector parallel to first p-orbital
else
x2 = xr (4) - xr (3)
y2=yr(4) - yr (3)
z2 = zr (4) - zr(3)
x3 = xr (5) - xr(3)
y3 = yr (5) - yr(3)
z3 = zr(5) - zr(3)
a1=y2*z3-y3*z2
b1 = x3*z2 - x2*z3
c1 = x2*y3 - x3*y2
rnorm = sqrt(a1*a1+b1*b1+c1*c1)
a1 = a1 / rnorm
b1 = b1 / rnorm
c1 = c1 / rnorm

```
```

now find vector parallel to the second p-orbital,
"a2" changes sign to correspond to internuclear axis
9 1 6

```

921

931
```

                    x2 = xr (7) - xr (6)
                    y2 = yr(7) - yr (6)
                    z2 = zr(7) - zr(6)
                    x3 = xr(8) - xr(6)
                    y3 = yr(8) - yr(6)
                    z3 = zr(8) - zr(6)
                    a2 = y2*z3 - y3*z2
                    b2 = x3*z2 - x2*z3
                    c2 = x2*y3 - x3*y2
            rnorm = sqrt(a2*a2+b2*b2+c2*c2)
            a2 = -a2 / rnorm
            b2 = b2 / rnorm
            c2 = c2 / rnorm
            osine = a1*a2 + b1*b2 + c1*c2
            if (cosine .lt. 0.0dO) then
            a2 = -a2
            b2 = -b2
            c2 = -c2
            end if
    find overlap if the orbitals were perfectly parallel
    xij = x(iorb) - x(jorb)
    ```
```

yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rij = sqrt(xij**2 + yij**2 + zij**2)
call overlap (atomic(iorb), atomic(jorb),rij,ideal)

```

\section*{A. 6 pitdrhf.f}
\begin{tabular}{|c|c|c|}
\hline \#\# & This code is written by Kush Patel. & \#\# \\
\hline \#\# & & \#\# \\
\hline \#\# & Prints various matrices and calls the TDHF & \#\# \\
\hline \# \# & iterator to update rho according to the & \#\# \\
\hline \# \# & equation: & \#\# \\
\hline \#\# & & \#\# \\
\hline \#\# & \((\mathrm{ih})(\mathrm{d}\) rho/dt) \(=\langle[\mathrm{F}(\mathrm{rho}), \mathrm{rho}]\rangle=\mathrm{i}\) L rho & \#\# \\
\hline \#\# & & \#\# \\
\hline \# \# & \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# & \\
\hline
\end{tabular}
subroutine pitdrhf
use sizes
use atoms
use atomid
```

use files
use iounit

```
    Dipole calculation
    real*8 hcom (3)
    real*8 ecom (3)
    real*8 qii
    real*8 dipl (3)
!-------Testing-------------
! Seeing if original method of calculating energy
! results in regular fluctuations
    complex*16 xi, xj, xk, xg, xcor
    complex*16 pii,pjj,pij
    ! Electron current
            real*8 currax, curray, curraz
            real*8 currbx, currby, currbz
            real*8 cc1, cc2, cc3
    68
        300 format (2E17.6, 3X)
        301 format (8E16.5)
        ! open an output file
        outiter \(=\) outiter +1
    printq \(=\bmod (o u t i t e r, o u t f r e q) \cdot e q \cdot 0\)
    printq \(=\) printq.or.(outiter.eq.1)
    lext \(=6\)
    if (printq) then
            call numeral (outiter, ext, lext)
            tdhfout \(=\) freeunit ()
            inquire(file=filename//'.tdhf.'//ext(1:lext), exist=exist)
            if (exist) then
            open(unit=tdhfout,
\&
            rewind(unit=tdhfout)
        else
        open (unit=tdhfout,
    \&
        file=filename(1:leng)//'.tdhf.'//ext(1:lext), status='new')
        end if
309
    format (A18, E16.5)


    write(tdhfout,*) ,
        write(tdhfout, 309) ' \(\sqcup\) Coupling \(\quad\) radius: \(\sqcup\) ', tdhfcr
        write(tdhfout, 309) 'பTimeபStep: பபபபபபப', tdhfdt
        write(tdhfout,*) ,'
    end if

! Following code develops the gamma matrix as well
! as the hc matrix. These are the various integrals
! and the Hatree Core matrix
    Taken straight from the piscf subroutine
    of picalc.f

    initialize some constants and parameters
    cionize \(=-11.16 d 0 /\) evolt
```

set the bond energies, alpha values and ideal bond length
parameter for carbon-carbon pibond type parameters
ebe = 129.37d0
ebb = 117.58d0
aeth = 2.309d0
abnz = 2.142d0
ble = 1.338d0
blb= = 1.397d0
assign empirical one-center Coulomb integrals, and
first or second ionization potential depending on
whether the orbital contribures one or two electrons
do i = 1, norbit
iorb = iorbit(i)
tdhfgamma(i,i) = emorb(iorb)
ip(i) = worb(iorb) + (1.0d0-qorb(iorb))*emorb(iorb)
end do
calculate two-center repulsion integrals
according to Ohno's semi-empirical formula
do i = 1, norbit
iorb = iorbit(i)
gii = tdhfgamma(i,i)
do j = i+1, norbit
jorb = iorbit(j)
g11 = 0.5d0 * (gii+tdhfgamma(j,j))
g11sq = 1.0d0 / g11**2
xij = x(iorb) - x(jorb)
yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rijsq = (xij**2 + yij**2 + zij**2) / bohr**2

```
```

g12 = 1.0d0 / sqrt(rijsq + g11sq)
tdhfgamma(i,j) = g12
tdhfgamma(j,i) = g12

```
end do
end do
the first term in the sum to find alpha is the first
or second ionization potential, then the two-center
repulsion integrals are added
do i = 1, norbit
hcii \(=i p(i)\)
do \(j=1\), norbit
if (i.ne.j) then
jorb \(=\) iorbit(j)
hcii \(=\) hcii - qorb(jorb)*tdhfgamma(i,j)
end if
end do
tdhfhc(i,i) = hcii
end do
get two-center repulsion integrals via Ohno's formula
do \(k=1, n b p i\)
i \(=\) ibpi \((2, k)\)
\(j=i b p i(3, k)\)
do i = 1, norbit-1
do \(j=i+1\), norbit
iorb \(=\) iorbit(i)
jorb \(=\) iorbit(j)
iatn \(=\) atomic(iorb)
jatn \(=\) atomic(jorb)
xij \(=x(i o r b)-x(j o r b)\)
```

    yij = y(iorb) - y(jorb)
    zij = z(iorb) - z(jorb)
    rij = sqrt(xij**2 + yij**2 + zij**2)
    rijsq = rij**2 / bohr**2
    g11 = 0.5d0 * (tdhfgamma(i,i) + tdhfgamma(j,j))
    g11sq=1.0d0 / g11**2
    g12 = tdhfgamma(i,j)
    ```
    178
! compute the bond energy using a Morse potential
    erij \(=\) aeth \(*(b l e-r i j)\)
    brij = abnz * (blb-rij)
    eebond \(=(2.0 d 0 * \exp (\operatorname{erij})-\exp (2.0 d 0 * e r i j)) *\) ebe / hartree
    bebond \(=(2.0 d 0 * \exp (b r i j)-\exp (2.0 d 0 * b r i j)) * e b b /\) hartree
    compute the carbon-carbon resonance integral using
the Whitehead and Lo formula
    \(\mathrm{g} 14=1.0 \mathrm{~d} 0 / \operatorname{sqrt}(4.0 \mathrm{~d} 0 * r i j s q+\mathrm{g} 11 \mathrm{sq})\)
    hcij \(=1.5 \mathrm{~d} 0 *(\) bebond-eebond) \(-0.375 \mathrm{~d} 0 * \mathrm{~g} 11\)
\&
                        \(+(5.0 \mathrm{~d} 0 / 12.0 \mathrm{~d} 0) * \mathrm{~g} 12-\mathrm{g} 14 / 24.0 \mathrm{~d} 0\)
if either atom is non-carbon, then factor the resonance
    integral by overlap ratio and ionization potential ratio
    if (iatn.ne. 6 .or. jatn.ne.6) then
        call overlap(iatn, jatn, rij, ovlap)
        call overlap (6, \(6, r i j\), covlap)
        hcij \(=\) hcij \(*(o v l a p / c o v l a p)\)
        iionize \(=\) ip(i)
        if (qorb(iorb) .ne. 1.0d0) then
            if (iatn .eq. 7) iionize \(=0.595 \mathrm{dO} *\) iionize
            if (iatn .eq. 8) iionize \(=0.525 d 0 *\) iionize
            if (iatn .eq. 16) iionize \(=0.890\) d0 * iionize

228
            end if
            jionize = ip(j)
                if (qorb (jorb) .ne. 1.0d0) then
                    if (jatn .eq. 7) jionize \(=0.595 d 0 *\) jionize
                    if (jatn .eq. 8) jionize \(=0.525 d 0 *\) jionize
                    if (jatn .eq. 16) jionize \(=0.890\) d0 * jionize
                    end if
                    hcij \(=\) hcij * (iionize+jionize)/(2.0d0*cionize)
                            end if
!-----Test Code 11.04.16----------------------------------------------
! This code is the pitdhf copy of the similar thing in fullpi.f.
! Applies Yukowa scaling to hcij terms of nonbonded atoms
    bonded = .false.
    do \(k=1\), nbpi
            iorb \(=\) ibpi (2,k)
            jorb \(=i b p i(3, k)\)
            bonded \(=\) (iorb.eq.i .and. jorb.eq.j) .or. bonded
                        end do
                        if (.not.bonded) then
                        hcij \(=\) hcij*(exp(-1.0d0*rij/tdhfcr))/rij
        end if

! set symmetric elements to the same value
            tdhfhc(i,j) = hcij
            tdhfhc(j,i) \(=\) hcij
        end do
        end do
c! reconstruct the Fock matrix

233
!

C
! reconstruct the Fock Matrix
do i=1, norbit
    do \(j=1\), norbit
            \(\mathrm{s} 1=0.0 \mathrm{~d} 0\)
            if(i.eq.j) then
            do \(k=1\), norbit
                \(s 1=s 1+\operatorname{tdhfed}(k, k) * t d h f g a m m a(i, k)\)
            end do
            end if
            \(s 2=0.5 d 0 * t d h f e d(i, j) * t d h f g a m m a(i, j)\)
            tdhffock(i,j) \(=\operatorname{tdhfhc}(i, j)+s 1-s 2\)
        end do
end do

263
```

do i=1, norbit
do j=1, norbit
gij = tdhfgamma(i,j)
s1 = (0.0d0,0.0d0)
s2 = -1.0d0*tdhfed(i,j)*gij
if(i.eq.j) then
do k=1, norbit
s1 = s1 + 2.0d0*tdhfgamma(i,k)*tdhfed(k,k) original
s1 = s1 + 1.0d0*tdhfgamma(i,k)*tdhfed(k,k)
end do
end if
tdhffock(i,j) = tdhfhc(i,j) + s1 + s2
end do
end do

```
            248
diagonalize the fock matrices to obtain eigenvalues

C

C
if(printq) then

    do i=1, norbit
        do \(j=1\), norbit
            write(tdhfout, 300, advance='no') tdhfed(i, j)
        end do
        write(tdhfout,*) ',
    end do
    write(tdhfout,*) ,
Print the diagonal elements
    format (2E20.9, 3X)
    write(tdhfout,*) 'TDHF」Density Matrix \({ }_{\sqcup}\) Diagonal'
    \(s 1=(0.0 d 0,0.0 d 0)\)
    do \(j=1\), norbit
        \(s 1=s 1+\operatorname{tdhfed}(j, j)\)
        if (printq) write(tdhfout, 307) tdhfed(j, j)
    end do
    format (A12, 2F17.6)
    write(tdhfout,*) ,
    write(tdhfout, 302) 'Trace: \({ }^{\prime}\), s1
    write(tdhfout,*) ,'
end if

C
! copy fock matrix to tdhfcopy

C
! occasionally recalculate the eigenvalues
c

318

C
! tridiagonalize
\(!\)

323
```

if(printq) write(tdhfout,*) 'Fock\sqcupmatrix'
do i=1, norbit
do j=1, norbit
fockcopy(i,j) = tdhffock(i,j)
if(printq) then
write(tdhfout, 300, advance='no') tdhffock(i,j)
end if
end do
if(printq) write(tdhfout,*) ,'
end do
if(printq) write(tdhfout,*) ',

```

```

if(mod(outiter,100).eq.1 .or. res1) then
res1 = .false.
if(tdhfdebug) then
write(debugout,*) 'Recalculating\sqcupSuper\sqcupEigenvalues'
end if

```
c
    call zhetrd('U', norbit, fockcopy, norbit,d,e,tau,
\&
                                work, \(8 *\) norbit, info)
    if(tdhfdebug) then
        write(debugout,*) 'Info:, , info
get the eigenvalues
    superevmax \(=0.0 \mathrm{~d} 0\)
    superevmin \(=0.0 \mathrm{~d} 0\)
    call zsteqr('N', norbit, d,e,'null', norbit,'null', info)
        write(tdhfout,*) 'Fock Eigenvalues: \({ }^{\prime}\) '
        write(tdhfout, 301) (d(i), i=1, norbit)

C
```

calculate total electronic energy

```
if (printq) then
    energy \(=(0.0 \mathrm{~d} 0,0.0 \mathrm{~d} 0)\)
    do i=1, norbit
        do \(j=1\), norbit
            pij \(=\) tdhfed(i,j)
            energy \(=\) energy \(+0.5 d 0 * p i j *(t d h f h c(j, i)+t d h f f o c k(j, i))\)
        end do
    end do
    format(A25,2E16.5)
    write (tdhfout, 305) 'TotalபElectronic Energy: \({ }_{\sqcup}\) ', energy
    write(tdhfout,*) ,
end if
            end do
        format (9E16.5)
                        write(tdhfout, 306) \(x(i o r b), y(i o r b), z(i o r b), c u r r a x, c u r r a y\),
            \&
                        curraz, currbx, currby, currbz
            end do
        end if
    408
    ! call tdhfiterate and update rho
        call tdhfiterate (tdhfed, tdhffock, superevmax,
        \& \(\quad\) superevmin, tdhfdt, norbit, 9)
        \& \(\quad\) superevmin, tdhfdt, norbit, 9)
        if (probcurr .and. printq) then
            write(tdhfout,*) 'Probability Current'

            do i=1 , norbit
                        iorb \(=\) iorbit(i)
        currax \(=0.0 \mathrm{~d} 0\)
        curray \(=0.0 \mathrm{~d} 0\)
        curraz \(=0.0 \mathrm{~d} 0\)
        do \(j=1\), norbit
                jorb \(=\) iorbit(j)
                cc1 \(=2.0 \mathrm{~d} 0 * \operatorname{tdhfhc(j,i)*\operatorname {aimag}(tdhfed(j,i))~}\)
                currax \(=\) currax \(+c c 1 *(x(j o r b)-x(i o r b))\)
                curray \(=\) curray \(+c c 1 *(y(j o r b)-y(i o r b))\)
                curraz \(=\) curraz \(+c c 1 *(z(j o r b)-z(i o r b))\)
!-----Test Code 13 Jan 18---------------------------------------------
    ! Test fock and density matrices for Hermiteness
    ! \(\quad \mathrm{s} 1=0.0 \mathrm{dO}\) ! Density
! \(\quad s 2=0.0 \mathrm{dO}\) ! Fock
! do i=1,norbit
            do \(j=1\), norbit
```

                s3 = abs(realpart( tdhfed(i,j) - tdhfed(j,i) ))
                s3 = abs(aimag( tdhfed(i,j) + tdhfed(j,i) ))
                s1 = s1 + s3 + s4
                s3 = abs(realpart( tdhffock(i,j) - tdhffock(j,i) ))
                    s4 = abs(aimag( tdhffock(i,j) + tdhffock(j,i) ))
                s2 = s2 + s3 + s4
            end do
        end do
        format(A4,2X,2E16.5)
        write(tdhfout,*) 'Hermiteness: '
        write(tdhfout, 308) 'Dens',s1
        write(tdhfout, 308) 'Fock',s2
        write(tdhfout,*) ,'
    !--------------------------------------------------------------------
! Impose zero for imaginary parts on diagonal
do i=1,norbit
tdhfed(i,i) = realpart(tdhfed(i,i))
end do
438
! update the nonplanar pi bond orders (pnpl) this is the same code that's at the end of picalc
401 format (5i5,2f12.2)
402 format(3A5,2A15)
if(printq) write(tdhfout,402) 'Bond','i','j','old','new'
do k=1, nbpi
i = ibpi(2,k)
j = ibpi(3,k)
p = pnpl(k)

```
```

take just the real part of electron density
pnpl(k) = realpart( tdhfed(i,j) )
take the real part of the electron density
pnpl(k) = zabs( tdhfeda(i,j) + tdhfedb(i,j))
pnpl(k) = realpart( tdhfed(i,j) )
pbpl(k) = pnpl(k) * tdhfhc(i,j)/(-0.0757d0)
i = ibnd(1,ibpi(1,k))
j = ibnd(2,ibpi(1,k))
if(printq)
\&
write(tdhfout, 401) k,ibpi (2,k),ibpi(3,k),i,j,p,pnpl(k)
end do
if(printq) write(tdhfout,*)',

```
        if(printq) then
```

        if(printq) then
            xi = 0.0d0
            xi = 0.0d0
        xj = 0.0d0
        xj = 0.0d0
        xk = 0.0d0
        xk = 0.0d0
        xg = 0.0d0
        xg = 0.0d0
        xcor = 0.0d0
        xcor = 0.0d0
    ```
!----------------------------
```

!----------------------------
write(tdhfout,*) 'Original\sqcupType}\sqcup\mathrm{ Energy Calculation'
write(tdhfout,*) 'Original\sqcupType}\sqcup\mathrm{ Energy Calculation'
do i=1, norbit
do i=1, norbit
do j=1, norbit
do j=1, norbit
pii = tdhfed(i,i)
pii = tdhfed(i,i)
pjj = tdhfed(j,j)
pjj = tdhfed(j,j)
pij = tdhfed(i,j)
pij = tdhfed(i,j)
xi = xi + pij*tdhfhc(i,j)
xi = xi + pij*tdhfhc(i,j)
xj = xj + 0.50d0*pij*tdhfgamma(i,j)

```
            xj = xj + 0.50d0*pij*tdhfgamma(i,j)
```

```
xk = xk - 0. 25d0*pij*tdhfgamma(i,j)
xcor = xcor - 0.5d0*(pij*pij - pii*pjj)*tdhfgamma(i,j)
```

        end do
    end do
    do \(i=1\), norbit-1
        do j=i+1, norbit
            \(\mathrm{xg}=\mathrm{xg}+\mathrm{tdh} f \mathrm{gamma}(\mathrm{i}, \mathrm{j})\)
    !----------------------------
    write(tdhfout,*)
    
write(tdhfout,*)',
write(tdhfout,*)',
Close the output file
flush(tdhfout)
close(unit=tdhfout)
! Write restart information
call writerestart()
end if
! oper - complex*16, input, matrix size m*m
Fock Matrix
operator $\operatorname{Exp}(-i \quad 0$ dt)
emax - real*8, input
largest eigenvalue of oper
! m - integer, input dimension of rhoo and oper
emin - real*8, input
smallest eigenvalue of oper
dt - real*8, input
time step
Np - integer, input
Chebyshev polynomial expansion limit
use sizes
use tdhfvars
implicit none

```
            integer i,j,k,m,Np,c(Np+1)
            real*8 dt,emin,emax,R,G,hToEvPS,dta
            complex*16 ii,sum,a(Np+1)
            complex*16 oper(m,m),X(m,m)
            complex*16 phi(Np+1,m,m),rho0(m,m)
            complex*16 FR(m,m),RF(m,m),temp(m,m)
            real*8 v1,v2
```

            code will expand to polynomials J_O to J_Np
            \(\mathrm{dta}=\mathrm{dt} * 41341.48 \mathrm{dO}\) ! dt in atomic units
        tdhfdebug = .false.
    Debugging prints
    format (2E17.6, 3X)
if(printq.and.tdhfdebug) then

write(tdhfout,*) 'emax ${ }_{\sqcup}={ }_{\sqcup}$, $\quad$ emax
write(tdhfout,*) 'emin ${ }_{\sqcup}=$ ', emin
write(tdhfout,*) 'dtபபப=ப', dt
write(tdhfout,*) 'dtaபப= ${ }^{\prime}$ ', dta

write(tdhfout,*) 'Np
write(tdhfout,*) "operator"
do $i=1, m$
do $j=1, m$
write(tdhfout, 111, advance='no') oper(i,j)
end do
write(tdhfout,*) ,'
end do
write(tdhfout,*) 'rho0பin'
do $i=1, m$
do $j=1, m$
write(tdhfout, 111, advance='no') rho0(i,j)
end do
write(tdhfout,*) ',
end do
end if
! initialize some values
ii $=(0 . d 0,1 . d 0)$
$\mathrm{R}=0.5 * \operatorname{dta} *($ emax-emin)
$\mathrm{G}=\mathrm{dta*emin}$
! define $X$ matrix

```
    write(tdhfout,*) 'X(i, j)'
do i=1,m
    do j=1,m
            X(i,j)= -1*ii*dta*oper(i,j)/R
                write(tdhfout,111, advance='no') X(i, j)
    end do
        write(tdhfout,*) ,'
end do
    write(tdhfout,*) , ,
phi is a 3 index array that acts as a temporary
container for values. Better visualized as a list
of matrices.
these values will be summed up
phi is indexed as:
    phi(expansion_number,density_matrix_row,
                                    density_matrix_column)
6 2 3 ~ ! ~ t h e ~ n e x t ~ 2 ~ d o ~ l o o p s ~ p o p u l a t e ~ p h i ( 1 ) ~ a n d ~ p h i ( 2 ) ~
phi(1)=rho0, phi(2)=[oper,rho]=oper.rho-rho.oper
note: phi(k) refers to the (k-1)th expansion
    write(tdhfout,*) 'phi(1,i,j)'
c
628
! Therefore, index (k) refers to the (k-1)th
! expansion. This is applicable to phi,a, and c
        do i=1,m
        do j=1,m
            phi(1,i,j)= rho0(i,j)
            write(tdhfout,*, advance='no') phi(1,i,j)
```

```
        end do
    !
6 3 8
    !
    ! matrix dot product of }X\mathrm{ and rho0
    FR = matmul(X,rho0)
    RF = matmul(rho0,X)
        do i=1,m
            do j=1,m
            print *, FR(i,j)
            print *, RF(i,j)
            end do
            print *,""
        end do
            do i=1,m
        do j=1,m
        phi(2,i,j)=FR(i,j)-RF(i,j)
    assign values to temp to be used as phi(k-1)
            temp(i,j)= phi(2,i,j)
            print *, phi(2,i,j)
            end do
        print *,""
            end do
663 !
    C(k) coefficients
    c(0) = 1,
    c(k>1) = 2
    c(1)=1
```

```
do k=2,Np+1
    c(k)=2
    print *, c(k)
end do
if(printq.and.tdhfdebug) then
        write(tdhfout,*) '!-coeffs'
    do k=1,Np+1
        write(tdhfout,*) c(k)
    end do
end if
```

use the recursion relation to populate phi
do $k=3, N p+1$
$\mathrm{FR}=$ matmul (X,temp)
$R F=$ matmul (temp, X)
do $i=1, m$
do $j=1, m$
phi (k,i,j) $=2 * F R(i, j)-2 * R F(i, j)+p h i(k-2, i, j)$
temp(i,j) $=$ phi(k,i,j)
end do
end do
end do
if(printq.and.tdhfdebug) then
do $k=1, N p+1$
write(tdhfout,'("phi(",i3,")")') k
do $i=1, m$
do $j=1, m$
write(tdhfout, 111, advance='no') phi(k,i,j)
end do
write(tdhfout,*) ',
end do
end do
end if
! populate a(k) integrals
do $k=1, N p+1$
703
!d print *, a(k)
end do
if (printq.and.tdhfdebug) then write(tdhfout,*) 'alpha $\operatorname{coeffs}^{\prime}$
do $k=1, N p+1$ write(tdhfout, 111) a(k)
end do
end if

713 ! perform final multiplication, sum up the expansions
! and store values in rhoo
do $i=1, m$
do $j=1, m$
sum $=(0 . d 0,0 . d 0)$
do $k=1, N p+1$
sum $=\operatorname{sum}+a(k) * p h i(k, i, j)$
end do
rhoo(i,j) = sum
end do

723 ! d print *,rho0(i,j)
end do
!-----Test Code 20 Mar 18----------------
! Long-time iterations accrue lots of error and we start

728
getting non-Hermitian matrices.

```
Here we'll just average transposed elements (and make
    sure imaginary sign is preserved).
    do i=1,m
    do j=1,m
        v1 = 0.5d0*(realpart( rho0(i,j)+rhoo(j,i) ))
        v2 = 0.5d0*(imagpart( rho0(i,j)-rho0(j,i) ))
        rho0(i,j) = v1 + ii*v2
        rho0(j,i) = v1 - ii*v2
    end do
    end do
if(printq.and.tdhfdebug) then
    write(tdhfout,*) "rhoO\sqcupout"
    do i=1, m
        do j=1, m
            write(tdhfout, 111, advance='no') rho0(i,j)
        end do
        write(tdhfout,*) ,'
    end do
end if
if(printq.and.tdhfdebug) then
    write(tdhfout,*) "#####}\sqcupTDHFITERATE END EN####"
    write(tdhfout,*) ,'
    write(tdhfout,*) ,'
    write(tdhfout,*) , ,
end if
```

return
end

763

| \#\# |  | \#\# |
| :---: | :---: | :---: |
| \#\# | This code is written by Kush Patel based off of the | \#\# |
| \#\# | methods described in the following reference | \#\# |
| \#\# |  | \#\# |
| \#\# | Population Analysis (Mulliken, Lowdin) | \#\# |
| \#\# | Modern Quantum Chemistry | \#\# |
| \#\# | Attila Szabo, Neil S. Ostlund | \#\# |
| \#\# |  | \#\# |
| \# \# | \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# | \# \# |

subroutine popanal(ml,N, rho, S, pop)

```
! N - integer, input
```

! rho - complex*16, input, matrix size $N * N$
Electron Density Matrix
788 !
!
ml - character, input, length 1
'M' for Mulliken Poplation Analysis
'L' for Lowdin Population Analysis
!
$!$
!

```
    pop - real*16, output, vector size N
    will contain the electron populations on exit
793
        end if
!----------------------------------------------------------------------------
    At this point, Mulliken was not chosen, default to Lowdin
    Diagonalize the overlap matrix to get its Eigensystem
        lwrk = 34*N
        call dsyev('V','U',N,S,N,evals,wrk,lwrk,info)
        write(tdhfout,*) 'dsyevьcalled'
```

```
write(tdhfout,*) 'info: பபப', info
write(tdhfout,*) 'wrk(1): '', wrk(1)
write(tdhfout,*) ',
```

401 format (E12.5, 'பப')
write(tdhfout,*) 'Overlap Eigenvalues'
do $i=1, N$
write(tdhfout, 401) evals(i)
end do
write(tdhfout,*) ',
write(tdhfout,*) 'Overlap Eigenvectors'
do $i=1, N$
do $j=1, N$
write(tdhfout, 401, advance='no') $S(i, j)$
end do
write(tdhfout,*) ,
end do
write(tdhfout,*) ,'
$S$ is now the eigenvector matrix.
Populate the diagonal elements of Ssqrt with the square roots
of the eigenvalues. Simultaneously populate SevecsT as the
transpose of the eigenvector Matrix.
do $i=1, N$
do $j=1, N$
SevecsT $(i, j)=S(j, i)$
$\operatorname{Ssqrt}(i, j)=0.0 d 0$
end do
Ssqrt(i,i) = sqrt(evals(i))
end do

```
    write(tdhfout,*) 'Overlap}\mp@subsup{\mp@code{Root}}{\bullet}{\prime}Eigenvalues'
    do i=1,N
        do j=1,N
            write(tdhfout,401, advance='no') Ssqrt(i,j)
        end do
    end do
    write(tdhfout,*) ,'
    Recover the overlap matrix root
    S^(1/2) = V.s^(1/2).V^T
    Ssqrt = matmul(Ssqrt,SevecsT)
    Ssqrt = matmul(S,Ssqrt)
    write(tdhfout,*) 'Overlap\sqcupRoot\sqcupMatrix'
    do i=1,N
        do j=1,N
        write(tdhfout,401, advance='no') Ssqrt(i,j)
    end do
    write(tdhfout,*) ,'
end do
write(tdhfout,*) ',
Perform final matrix multiplication according to
Lowdin Population Analysis
P'}=\mp@subsup{S}{}{\wedge}(1/2)\cdotP\cdot\mp@subsup{S}{}{\wedge}(1/2
    rho2 = matmul(rho,Ssqrt)
    rho2 = matmul(Ssqrt,rho2)
    do i=1, N
    pop(i) = zabs(rho2(i,i))
```

end do
return

## subroutine writerestart

908

```
integer rout, freeunit
integer i,j
logical exist
character*20 fname
```

913
end subroutine
$!$

```
use iounit
use orbits
use piorbs
use tdhfvars
implicit none
```

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
\# \# \#\# \#
\#\# writerestart - subroutine to save information for \#\#
\#\# resuming an old dynamics simulation \#\#
\#\# \#\#
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
fname $=$ 'restart/restart.data'

```
rout = freeunit()
inquire(file=fname, exist=exist)
```

if (exist) then
open(unit=rout,file=fname, status='old')
rewind (rout)
else
call system('mkdirurestart')
open(unit=rout,file=fname, status='new')
end if
501 format (A10, 2X, I8)
502 format (A10, 2X,L1)
write(rout, 501) "Iter: $\quad$ ", outiter
write(rout, 502) "Usé URHF: $"$, useurhf
write (rout,*) ""
503 format (8E17.6)
if (useurhf) then

do i=1, norbit
write(rout, 503) (realpart(tdhfeda(i,j)), $=1$, norbit)
end do
write(rout,*) 'Density Matrix ${ }_{\sqcup}(a l p h a, \sqcup I M)$ '
do i=1, norbit
write(rout, 503) (aimag(tdhfeda(i,j)), j=1, norbit)
end do
write(rout,*) 'Density ${ }^{\prime}$ Matrix $\sqcup($ beta, $\sqcup$ RE) '
do i=1, norbit

```
            write(rout, 503) (realpart(tdhfedb(i,j)), j=1, norbit)
    end do
    write(rout,*) 'Density\sqcupMatrix
    do i=1,norbit
        write(rout, 503) (aimag(tdhfedb(i,j)), j=1, norbit)
    end do
else
    write(rout,*) 'Density Matrix
    do i=1,norbit
        write(rout,503) (realpart(tdhfed(i,j)),j=1, norbit)
    end do
    write(rout,*) 'Density\sqcupMatrix
    do i=1,norbit
        write(rout, 503) (aimag(tdhfed(i,j)), j=1, norbit)
    end do
end if
```

```
flush(rout)
```

flush(rout)
close(unit=rout)
close(unit=rout)
end subroutine writerestart

```
973
\(\begin{array}{ll}\text { ! } & \text { \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# } \\ ! & \# \# \\ ! & \# \# \\ ! & \text { tdhfloadold - subroutine to load old information }\end{array}\)
```

! \#\# from previous dynamics simulation \#\#
subroutine tdhfload

```
```

check if *.dyn exists. If not do not resume
fname = filename(1:leng) // '.dyn'
inquire(file=fname, exist=exist)
if(.not.exist) then
write(iout,*) ', Could
return
end if
II=(0.0d0,1.0d0)
fname = "restart/restart.data"

```

1008
```

io=freeunit()
open(unit=io,file=fname,action='read')

```
    501 format (A10, 2X, I8)
    502 format(A10, 2X,L1)
    read (io, 501) line, outiter
    read (io, 502) line, useurhf
    if(useurhf) print \(*\), 'Use unrestricted'
if(.not. useurhf) print \(*\), 'Use restricted'
    read (io,*) line
allocate(temp1 (norbit, norbit))
allocate(temp2(norbit, norbit))
if(.not.allocated(tdhfhc)) then
    allocate (tdhfhc(norbit, norbit))
end if
if(.not.allocated(tdhfgamma)) then
    allocate (tdhfgamma(norbit, norbit))
    end if
503 format (8E17.6)
    if (useurhf) then
    if(.not.allocated(tdhffocka)) then
    allocate(tdhffocka(norbit, norbit))
    end if
    if(.not.allocated(tdhffockb)) then
    allocate(tdhffockb(norbit, norbit))
    end if
    if(.not.allocated(tdhfeda)) allocate(tdhfeda(norbit, norbit))
```

    if(.not.allocated(tdhfedb)) allocate(tdhfedb(norbit,norbit))
    do i=1, norbit
        read(io,503) (temp1(i,j),j=1,norbit)
    end do
    read(io,*) line
    do i=1, norbit
        read(io,503) (temp2(i,j),j=1,norbit)
    end do
    do i=1,norbit
        do j=1,norbit
            tdhfeda(i,j)= temp1(i,j)+II*temp2(i,j)
        end do
    end do
    1053
    ```
```

    read(io,*) line
    do i=1,norbit
        read(io,503) (temp1(i,j),j=1,norbit)
    end do
    read(io,*) line
    do i=1,norbit
        read(io,503) (temp2(i,j),j=1,norbit)
    end do
    do i=1,norbit
        do j=1,norbit
        tdhfedb(i,j) = temp1(i,j)+II*temp2(i,j)
        end do
    end do
    else
if(.not.allocated(tdhfed)) allocate(tdhfed (norbit,norbit))
if(.not.allocated(tdhffock)) allocate(tdhffock(norbit,norbit))

```
```

    do i=1,norbit
        read(io,503) (temp1(i,j),j=1,norbit)
    end do
    read(io,*) line
    do i=1,norbit
        read(io,503) (temp2(i,j),j=1,norbit)
        end do
        do i=1,norbit
        do j=1,norbit
            tdhfed(i,j) = temp1(i,j)+II*temp2(i,j)
        end do
        end do
    end if
tdhffirst = .false.
deallocate(temp1)
deallocate(temp2)
close(io)
end subroutine

```

\section*{A. 7 pitduhf.f}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline 1 ! & \multicolumn{8}{|l|}{\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#} \\
\hline ! & \#\# & This & code is w & written by & Kush & Patel & & \#\# \\
\hline \(!\) & \#\# & & & & & & & \#\# \\
\hline ! & \#\# & Prints & s various & s matrices & and & calls the & TDHF & \#\# \\
\hline
\end{tabular}
```

! \#\# iterator to update rho according to the \#\#
| \#\# equation: \#\#
! \#\# \#\#
! \#\# (ih)(d rho/dt) = <[F(rho),rho]> = i L rho \#\#
\#\# \#\#
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
11
pitdhf variables
integer i,j,k,m
integer info
complex*16 tau(norbit),work(8*norbit),fockcopy(norbit,norbit)
real*8 d(norbit),e(norbit-1), p
variables for reconstructing fock
integer iorb,jorb
integer iatn,jatn
complex*16 s1a,s2a,s1b,s2b
real*8 hcii, hcij

```
```

    real*8 brij,erij
    real*8 bebond,eebond
    real*8 ebb,ebe,abnz,aeth,ble,blb
    real*8 xij,yij,zij,rij,rijsq
    real*8 gii,gij,g11,g11sq,g12,g14
    real*8 ovlap,covlap
    real*8 cionize,iionize,jionize
    real*8 ip(norbit)
    ! variables for population analysis
real*8 Smatrix(norbit,norbit), pop(norbit)
! variables for iterative output
integer lext
character*7 ext
integer freeunit
logical exist
variables for total energy calculation
complex*16 energy, paij, pbij
! Dipole calculation
real*8 hcom(3)
real*8 ecom(3)
real*8 qii
real*8 dipl(3)
!--------Testing------------
! Seeing if original method of calculating energy
! results in regular fluctuations
complex*8 xi,xj,xk,xg,xcor
complex*8 pii,pjj,pij
!---------------------------
Electron current
real*8 currax, curray, curraz
real*8 currbx, currby, currbz

```
```

real*8 cc1,cc2,cc3

```
format (2E17.6, 3X)
301 format(8E16.5)
    open an output file
    outiter = outiter + 1
    printq \(=\bmod (o u t i t e r, o u t f r e q) . e q .0\)
    printq \(=\) printq.or.(outiter.eq.1)
    lext \(=6\)
    if (printq) then
        call numeral (outiter, ext, lext)
        tdhfout \(=\) freeunit()
        inquire(file=filename//'.tdhf.'//ext(1:lext), exist=exist)
        if (exist) then
            open(unit=tdhfout,
\&
\&

309
```

    format(A18, E16.5)
    ```

    write (tdhfout,*) ,
    write(tdhfout, 309) ' \(\sqcup\) Coupling r radius: \(\mathrm{b}^{\prime}\), tdhfcr
    write (tdhfout, 309) 'பTimeபStep: பபபபபபப', tdhfdt
    write(tdhfout,*) ,'
end if
```

! Following code develops the gamma matrix as well
1 0 1
! and the Hatree Core matrix
! Taken straight from the piscf subroutine
! of picalc.f
!----------------------------------------------------------------------
initialize some constants and parameters
cionize = -11.16d0 / evolt
! set the bond energies, alpha values and ideal bond length
parameter for carbon-carbon pibond type parameters
ebe = 129.37d0
ebb = 117.58d0
aeth=2.309d0
abnz = 2.142d0
ble=1.338d0
blb=1.397d0
assign empirical one-center Coulomb integrals, and
first or second ionization potential depending on
whether the orbital contribures one or two electrons
do i = 1, norbit
iorb = iorbit(i)
tdhfgamma(i,i)= emorb(iorb)
ip(i) = worb(iorb) + (1.0d0-qorb(iorb))*emorb(iorb)
end do
1 2 6

```
```

! calculate two-center repulsion integrals

```
! calculate two-center repulsion integrals
! according to Ohno's semi-empirical formula
```

! according to Ohno's semi-empirical formula

```
```

do i = 1, norbit
iorb = iorbit(i)
gii = tdhfgamma(i,i)
do j = i+1, norbit
jorb = iorbit(j)
g11 = 0.5d0 * (gii+tdhfgamma(j,j))
g11sq=1.0d0 / g11**2
xij = x(iorb) - x(jorb)
yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rijsq = (xij**2 + yij**2 + zij**2) / bohr**2
g12 = 1.0d0 / sqrt(rijsq + g11sq)
tdhfgamma(i,j) = g12
tdhfgamma(j,i) = g12
end do
end do
the first term in the sum to find alpha is the first
or second ionization potential, then the two-center
repulsion integrals are added
do i = 1, norbit
hcii = ip(i)
do j = 1, norbit
if(i.ne.j) then
jorb = iorbit(j)
hcii = hcii - qorb(jorb)*tdhfgamma(i,j)
end if
end do
tdhfhc(i,i) = hcii
end do

```
```

get two-center repulsion integrals via Ohno's formula
do k = 1, nbpi
i = ibpi(2,k)
j = ibpi(3,k)
do i = 1, norbit-1
do j = i+1, norbit
iorb = iorbit(i)
jorb = iorbit(j)
iatn = atomic(iorb)
jatn = atomic(jorb)
xij = x(iorb) - x(jorb)
yij = y(iorb) - y(jorb)
zij = z(iorb) - z(jorb)
rij = sqrt(xij**2 + yij**2 + zij**2)
rijsq = rij**2 / bohr**2
g11 = 0.5d0 * (tdhfgamma(i,i) + tdhfgamma(j,j))
g11sq= 1.0d0 / g11**2
g12 = tdhfgamma(i,j)
compute the bond energy using a Morse potential
erij = aeth * (ble-rij)
brij = abnz * (blb-rij)
eebond = (2.0d0*exp(erij)-exp(2.0d0*erij)) * ebe / hartree
bebond = (2.0d0*exp(brij)-exp(2.0d0*brij)) * ebb / hartree
compute the carbon-carbon resonance integral using
the Whitehead and Lo formula
g14 = 1.0d0 / sqrt(4.0d0*rijsq+g11sq)
hcij = 1.5d0*(bebond-eebond) - 0.375d0*g11
\&
+(5.0d0/12.0d0)*g12 - g14/24.0d0

```
```

    if either atom is non-carbon, then factor the resonance
    integral by overlap ratio and ionization potential ratio
    if(iatn.ne.6 .or. jatn.ne.6) then
            call overlap(iatn,jatn,rij,ovlap)
            call overlap(6,6,rij, covlap)
            hcij = hcij * (ovlap/covlap)
            iionize = ip(i)
            if(qorb(iorb) .ne. 1.0d0) then
                if(iatn .eq. 7) iionize = 0.595d0 * iionize
                    if(iatn .eq. 8) iionize = 0.525d0 * iionize
                if(iatn .eq. 16) iionize = 0.890d0 * iionize
                    end if
            jionize = ip(j)
            if(qorb(jorb) .ne. 1.0d0) then
                    if(jatn .eq. 7) jionize = 0.595d0 * jionize
                    if(jatn .eq. 8) jionize = 0.525d0 * jionize
                    if(jatn .eq. 16) jionize = 0.890d0 * jionize
            end if
            hcij = hcij * (iionize+jionize)/(2.0dO*cionize)
            end if
    211 !-----Test Code 11.04.16--------------------------------------------
! This code is the pitdhf copy of the similar thing in fullpi.f.
! Applies Yukowa scaling to hcij terms of nonbonded atoms
bonded = .false.
do k=1, nbpi
iorb = ibpi(2,k)
jorb = ibpi(3,k)
bonded = (iorb.eq.i . and. jorb.eq.j) .or. bonded
end do
if(.not.bonded) then

```
```

                    hcij = hcij*(exp(-1.0d0*rij/tdhfcr))/rij
                            end if
    226 !
set symmetric elements to the same value
tdhfhc(i,j) = hcij
tdhfhc(j,i)=hcij
end do
end do
2 3 1

```

236
```

    reconstruct the Fock Matrix
    do i=1, norbit
    do j=1, norbit
        s1a = (0.0d0, 0.0d0) ! Total Density matrix element
        s1b=(0.0d0, 0.0d0) ! rho(k,k)*J(i,k)
        s2a}=-1.0d0*tdhfgamma(i,j)*tdhfeda(i,j
        s2b}=-1.0d0*tdhfgamma(i,j)*tdhfedb(i,j
            if(i.eq.j) then
                do k=1, norbit
                s1a = tdhfeda(k,k) + tdhfedb(k,k)
                s1b=s1b + s1a*tdhfgamma(i,k)
            end do
        end if
            tdhffocka(i,j) = tdhfhc(i,j) + s2a + s1b
            tdhffockb(i,j) = tdhfhc(i,j) + s2b + s1b
    end do
    end do

```
```

diagonalize the fock matrices to obtain eigenvalues
for the superoperator
do m=1,2
print density matrices
if(printq) then
if(m.eq.1) then
write(tdhfout,*) 'TDHF
else
write(tdhfout,*) 'TDHF}\mp@subsup{\mp@code{LElectron}\sqcup\perpDensity\sqcupMatrix}{\sqcup}{\prime}(beta)'
end if
do i=1, norbit
do j=1, norbit
if(m.eq.1) then
write(tdhfout, 300, advance='no') tdhfeda(i,j)
else
write(tdhfout, 300, advance='no') tdhfedb(i,j)
end if
end do
write(tdhfout,*) ,'
end do
write(tdhfout,*) , ,
Print the diagonal elements
format(2E20.9,3X)
if(m.eq.1) then

```

```

    else
            write(tdhfout,*) 'TDHF
    ```
end if
end if
\(\mathrm{s} 1 \mathrm{a}=(0.0 \mathrm{~d} 0,0.0 \mathrm{~d} 0)\)
do \(j=1\), norbit
if(m.eq.1) then
s1a = s1a + tdhfeda(j,j)
if (printq) write(tdhfout, 307) tdhfeda(j,j)
else
\(\mathrm{s} 1 \mathrm{a}=\mathrm{s} 1 \mathrm{a}+\mathrm{tdhfedb}(\mathrm{j}, \mathrm{j})\)
if (printq) write(tdhfout, 307) tdhfedb(j,j)
end if
end do
if (printq) then
format (A12, 2F17.6)
write (tdhfout, *) , '
write(tdhfout, 302) 'Trace: \({ }^{\prime}\), s1a
write(tdhfout,*) ,
\(\mathrm{s} 1 \mathrm{a}=(0.0 \mathrm{~d} 0,0.0 \mathrm{~d} 0)\)
do i=1, norbit
s1a = s1a + tdhfeda(i,i) + tdhfedb(i,i)
end do
if(m.eq.2) then
format (A19, 2F17.6)

write(tdhfout,*) ,
end if
end if
```

! copy fock matrix to tdhfcopy
! occasionally recalculate the eigenvalues
if(mod(outiter,100).eq.1 .or. res1) then
res1 = .false.

```

316 !
    \(!\)
                if(tdhfdebug) then

                end if
! tridiagonalize
\&
```

    call zhetrd('U',norbit,fockcopy,norbit,d,e,tau,
        work,8*norbit,info)
    if(tdhfdebug) then
        write(debugout,*) 'Info:ь', info
        write(debugout,*) ',
        write(debugout,*) 'Post\sqcupTridiagonal\sqcupFock'
        do i=1,norbit
        do j=1, norbit
            if(m.eq.1) then
                write(debugout, 300, advance='no') tdhffocka(i,j)
                else
                    write(debugout,300, advance='no') tdhffockb(i,j)
                end if
        end do
        write(debugout,*)''
        end do
        write(debugout,*)''
    ```
    write(debugout,*) 'tri-diagonalபmatrix'
    write(debugout,*) 'diagonal பபபபபsuperdiagonal'
    do i=1, norbit
        write(debugout, 301, advance='no') d(i)
        if(i.ne.norbit) then
                write(debugout, 301, advance='no') e(i)
        end if
```

            write(debugout,*) ,'
            end do
            write(debugout,*) ',
            end if
    ```
```

    get the eigenvalues
    if(m.eq.1) then
            superevmax = 0.0d0
            superevmin = 0.0d0
        end if
        call zsteqr('N',norbit,d,e,'null',norbit,'null',info)
        if(printq) then
            if (m.eq.1) then
                write(tdhfout,*) 'Fock
            else
            write(tdhfout,*) 'Fock
            end if
            write(tdhfout,301) (d(i),i=1,norbit)
            write(tdhfout,*)',
        end if
        superevmax = max(superevmax,d(norbit)-d(1))
        superevmin = min(superevmin,d(1)-d(norbit))
        if(printq) then
        write(tdhfout,*) 'Supereigenvalues:\sqcup{', superevmin,', \sqcup',
            superevmax, '}'
            write(tdhfout,*) ,'
        end if
        superevmax = 1.5d0*superevmax
        superevmin = 1.5d0*superevmin
    ```
end if
calculate total electronic energy
    if (printq) then
    if(m.eq.2) then
        energy \(=(0.0 \mathrm{do}, 0.0 \mathrm{~d} 0)\)
        \(s 1 \mathrm{a}=(0.0 \mathrm{~d} 0,0.0 \mathrm{~d} 0)\)
        \(\mathrm{s} 1 \mathrm{~b}=(0.0 \mathrm{~d} 0,0.0 \mathrm{~d} 0)\)
        do i=1, norbit
                do \(j=1\), norbit
                    paij = tdhfeda(i,j)
                pbij = tdhfedb(i,j)
                    s1a = s1a + 0.5d0*paij*(tdhfhc(j,i)+tdhffocka(j,i))
                    \(\mathrm{s} 1 \mathrm{~b}=\mathrm{s} 1 \mathrm{~b}+0.5 \mathrm{~d} 0 * \mathrm{pbi} j *(\mathrm{tdhfh} \mathrm{c}(\mathrm{j}, \mathrm{i})+\mathrm{tdhffockb}(\mathrm{j}, \mathrm{i}))\)
                end do
        end do
        energy \(=s 1 a+s 1 b\)
        format (A25, 2E16.5)
                write(tdhfout, 305) 'Total」alpha」Energy: \({ }^{\prime}\) ', s1a
                write(tdhfout, 305) 'TotalபbetaபEnergy: \({ }^{\prime}\) ' , s1b
                write (tdhfout, 305) 'TotalபElectronic Energy: ', energy
        write(tdhfout,*) ,
    end if
    end if
    if(m.eq. 2 . and. probcurr .and. printq) then
    write(tdhfout,*) 'Probability Current'

    do i=1, norbit
```

            iorb = iorbit(i)
            currax = 0.0d0
            curray = 0.0d0
            curraz = 0.0d0
            currbx = 0.0d0
            currby = 0.0d0
            currbz = 0.0d0
            do j=1, norbit
        jorb = iorbit(j)
        cc1 = 2.0d0*tdhfhc(j,i)*aimag(tdhfeda(j,i))
        cc2 = 2.0d0*tdhfhc(j,i)*aimag(tdhfedb(j,i))
        currax = currax + cc1* (x(jorb)-x(iorb))
        curray = curray + cc1* (y(jorb)-y(iorb))
        curraz = curraz + cc1* (z(jorb)-z(iorb))
        currbx = currbx + cc2* (x(jorb)-x(iorb))
        currby = currby + cc2* (y(jorb)-y(iorb))
        currbz = currbz + cc2* (z(jorb)-z(iorb))
            end do
        format(9E16.5)
            write(tdhfout, 306) x(iorb),y(iorb),z(iorb),currax,curray,
        &
            curraz,currbx,currby,currbz
            end do
        end if
        end do
    ```
    call tdhfiterate and update rho
    call tdhfiterate (tdhfeda, tdhffocka, superevmax,
    \& superevmin,tdhfdt,norbit, 9)
    call tdhfiterate (tdhfedb, tdhffockb, superevmax,
    \& superevmin,tdhfdt,norbit, 9)
```

4 7 1
! Impose zero for imaginary parts on diagonal
do i=1,norbit
tdhfeda(i,i) = realpart(tdhfeda(i,i))
tdhfedb(i,i) = realpart(tdhfedb(i,i))
end do
!--------------------------------------------------------------------
!
! update the nonplanar pi bond orders (pnpl)
this is the same code that's at the end of picalc
!
401 format(5i5,2f12.2)
402 format(3A5,2A15)
if(printq) write(tdhfout,402) 'Bond','i','j','old','new'
4 8 6
do k=1, nbpi
i = ibpi(2,k)
j = ibpi(3,k)
p = pnpl(k)
4 9 1
take just the real part of electron density
pnpl(k) = realpart( tdhfed(i,j) )
take the real part of the electron density
pnpl(k) = zabs( tdhfeda(i,j) + tdhfedb(i,j))
pnpl(k) = realpart( tdhfeda(i,j) + tdhfedb(i,j) )
pbpl(k) = pnpl(k) * tdhfhc(i,j)/(-0.0757d0)
i = ibnd(1,ibpi(1,k))
j = ibnd(2,ibpi(1,k))
if(printq)

```
```

\&
write(tdhfout,401) k,ibpi(2,k),ibpi(3,k),i,j,p,pnpl(k)
end do
if(printq) write(tdhfout,*)',

```
!-----------------------------
    if (printq) then
        \(x i=0.0 d 0\)
        \(x j=0.0 d 0\)
        \(\mathrm{xk}=0.0 \mathrm{~d} 0\)
        \(x g=0.0 d 0\)
        \(\mathrm{xcor}=0.0 \mathrm{~d} 0\)
        write(tdhfout, *) 'Original Type \(_{\sqcup}\) Energy Calculation'
        do i=1, norbit
            do \(j=1\), norbit
                    pii \(=\) tdhfeda(i,i) + tdhfedb(i,i)
                    pjj = tdhfeda(j, j) + tdhfedb(j,j)
                    pij = tdhfeda(i,j) + tdhfedb(i,j)
                    xi = xi + pij*tdhfhc(i,j)
                    \(x j=x j+0.50 d 0 * p i j * t d h f g a m m a(i, j)\)
                    \(x k=x k-0.25 d 0 * p i j * t d h f g a m m a(i, j)\)
                xcor \(=x \operatorname{cor}-0.5 d 0 *(p i j * p i j-p i i * p j j) * t d h f g a m m a(i, j)\)
            end do
        end do
        do i=1, norbit-1
            do \(j=i+1\), norbit
                    \(\mathrm{xg}=\mathrm{xg}+\mathrm{tdhfgamma(i,j)}\)
            end do
        end do
        write(tdhfout,*) 'OEnergy: பப', \(x i+x j+x k+x g+x\) cor
        write(tdhfout,*) 'Core: பபபபப', xi
```

    write(tdhfout,*) 'Coulomb: பப', xj
    write(tdhfout,*) 'Exchange: ப', xk
    write(tdhfout,*) 'Nuclear:பப', xg
    write(tdhfout, *) 'Xcorrect: ', xcor
    ! Close the output file
flush(tdhfout)
close(unit=tdhfout)
54
! Write restart information
call writerestart()
end if
551
end subroutine

```
A. 8 redirects.f
```

! The following lines of code must be inserted into the indicated
! files. This code is written for TINKER version 7.1.2. Users must
ensure compatibility with newer versions.

```
```

! =======================

```
! dynamic.f
\(!======================\)
```

        insert this section in the header to inlude usage of variables
    !-----------------------
            use tdhfvars
            use civars
    !---------------------
    ```
13
    ! insert this section before the integration steps are started

    call tdhfinit to see if TDHF is requested and initialize necessary
    parameters
18
    ! Copy dt to a variable TDHF will use
    if(usetdhf) then
            \(t d h f d t=d t\)
23
    end if

    ! call ciinit to see if CI theory/excited calculations are requested
    ! and initialize the necessary parameters
    C
            call ciinit
    \(!=====================\)
33 ! picalc.f

    ! insert this section in the header to inlude usage of variables
    ! ------------------------
    use tdhfvars
    use civars

A. 9 tdhfinit.f
\(!\)
! \(\quad\) \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
! \#\# Written by Kush Patel - 2/01/16 \#\#
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

5 !
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
\# \# \# \#
! \#\# subroutine tdhfinit -- checks for keyword tdhf and \#\#
! \#\# and initializes necessary
\# \# \# \# \#
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
!
! "tdhfinit" checks for the keyword "TDHF" which decides whether the tchebychev propagator will be used or not
```

subroutine tdhfinit
use sizes
use keys
use tdhfvars
logical exist, resumeq
integer i, next, freeunit
character*20 keyword
character*120 record, string

```
usetdhf = .false.
tdhfdebug = .false.
printq \(=\).false.
probcurr \(=\).false.
useurhf = .false.
resumeq \(=. f a l s e\).
res1 = .false.
outiter \(=0\)
outfreq = 1
do \(i=1\), nkey
    next \(=1\)
    record \(=\) keyline(i)
    call gettext (record,keyword, next)
    call upcase (keyword)
    if (keyword (1:5) .eq. 'TDHF」') then
        usetdhf \(=\).true.
        tdhffirst \(=\).true.
    else if(keyword (1:7) .eq. 'TDHFCR \({ }_{\sqcup}\) ') then
        string \(=\operatorname{record}(\) next:120)
        tdhfcr \(=0.0 \mathrm{dO}\)
```

            read(string,*,err=10, end=10) tdhfcr
            continue
    else if(keyword(1:10).eq.''TDHFDEBUGG') then
        tdhfdebug = .true.
        debugout = freeunit()
    open the debugging output
inquire(file='tdhf.debug',exist=exist)
if(exist) then
open(unit=debugout,file='tdhf.debug',status='old')
rewind(unit=debugout)
else
open(unit=debugout,file='tdhf.debug',status='new')
end if
else if(keyword(1:8).eq.'USEURHF\sqcup') then
useurhf = .true.
else if(keyword(1:11).eq.'PRINTEVERY!') then
string = record(next:120)
read(string,*,err=20, end=20) outfreq
if(outfreq.lt.1) outfreq = 1
continue
else if(keyword(1:9).eq.'PROBCURR}\mp@subsup{}{\square}{\prime})\mathrm{ ) then
probcurr = .true.
else if(keyword(1:8).eq.' RESUME }\mp@subsup{|}{}{\prime}\mathrm{ ') then
resumeq = .true.
res1 = .true.
end if
end do
if(resumeq) call tdhfload()
return

```

\section*{A. 10 tdhfvars.f}

1
! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# \# \# \#\#
    ! \#\# module tdhfvars -- contents of the PITDHF \#\#
    ! \#\# calculation \#\#
    6 \#\# \#\#
    ! \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
    !
    \(!\)
    ! maxkey maximum number of lines in the keyword file
11 !
    ! nkey number of nonblank lines in the keyword file
    ! keyline contents of each individual keyword file line
    !
    ! usetdhf logical that indicates whether TDHF is used
    6 ! tdhffirst logical switch that indicates whether the dynamics
    ! are in the first time step
    ! tdhfdebug logical for deciding whether to print debugging
    information
    ! tdhfdt time step for dynamics
21 ! tdhfout output file unit number
    ! tdhf_ nfill fill level for the orbitals (\# of electrons / 2)
    ! tdhfeda tdhf electron density matrix (spin up)
    ! tdhfedb tdhf electron density matrix (spin down)
! tdhffocka tdhf fock matrix (spin up)
6 ! tdhffockb tdhf fock matrix (spin down)
! tdhfgamma tdhf gamma matrix
```

tdhfh! tdhf core matrix
bonded logical that indicates whether a pair of atoms
are bonded
tdhfcr coupling radius for the exponetial scaling term (Angstrom)
module tdhfvars
implicit none
logical usetdhf, tdhffirst, tdhfdebug, printq
logical probcurr, useurhf, res1
integer tdhfout, debugout, tdhf_nfill, outiter
integer outfreq
real*8 tdhfdt, superevmin, superevmax
complex*16, allocatable :: tdhfeda(:,:)
complex*16, allocatable :: tdhfedb(:,:)
complex*16, allocatable :: tdhffocka(:,:)
complex*16, allocatable :: tdhffockb(:,:)
complex*16, allocatable :: tdhfgamma(:,:)
complex*16, allocatable :: tdhfhc(:,:)
logical bonded
real*8 tdhfcr
complex*16, allocatable :: tdhfed(:,:)
complex*16, allocatable :: tdhffock(:,:)
save
end

```

\section*{A. 11 mpacf.py}
```

    " " "
    Program for computing velocity autocorrelation of TINKER
    files (multiprocessor)
    Written by Kush Patel, May 2019
    Tinker velocity files have names in the form:
        root.###v
    Input for this program is a JSON file with the following
parameters defined:
root (string)

- Root title of the TINKER coordinate file outtag (string)
- User defined output label for section of system autocorrelated
- output file will be named "[root].[outtag].acf"
atoms (array of integers)
- Indices of atoms to consider in autocorrelation
Example:
[ \{
"root": "TPP",
"outtag": "diaryl",
"atoms: [35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67]
\}]

```
```

    ! This code is non-general and written for use in a specific
    ! directory and ensemble nomenclature. Furthermore, it
    ! includes velocity files of a prior calculation for
    ! pre-excitation dynamics. Users should adjust this code to
    ! their directory setup.
    " " "
    40
import multiprocessing as mp
import time
import os
import glob
import sys
import numpy as np
import json
def autocorr( tau ):
sm=0.0
for i in range(0,nfiles-tau):
for j in atomlist:
sm += np.sum( vels[i,j]*vels[i+tau,j] )
return sm/(nfiles-tau)
def importvel(fn):
tfn = "temp.vel."+str(os.getpid())
os.system('cpu''+fn+',''ttfn )
os.system("sed

```
```

        vels = np.loadtxt(tfn,skiprows=1,usecols=(2, 3,4))
        os.remove(tfn)
    ```
    if __name__ == '__main__':
        print("Loadingparameters..")
        jsonfile \(=\) sys.argv[1]
        with open(jsonfile) as jf: jstr = jf.read()
        prms \(=\) json.loads (jstr) [0]
        try:
            root \(=\) prms["root"]
    except KeyError:
        print("No root \(_{\sqcup}\) name \(_{\sqcup}\) found")
            sys.exit()
        try:
            alst \(=\) prms["atoms"]
    except KeyError:
            alst \(=-1\)
    try:
            outtag = "."+prms["outtag"]
    except KeyError:
        outtag = ""
    print("parameters found ")
    print("root \(\dot{\text { bபபபபபபப: }}\) " + root)
    try:
            nprocs \(=\) int(os.environ["SLURM_JOBS_CPUS_PER_NODE"])
    except KeyError:
            nprocs \(=16\)
```

print( "nprocsutபபபபப:ப"+ str(nprocs) )

```
simdirs \(=\) glob.glob("../"+root+"/sim0*/")
simdirs \(=[\operatorname{str}(s d)\) for \(s d\) in simdirs ]
timefiles \(=[\) str ( root+"." + str (i). zfill (3) +"v" )
    for \(i\) in range \((1,10001)\) ]
for sd in simdirs:
    simitr \(=\) sd.split('/') [2]
    simitr \(=\) int(simitr [4:])
    shortitr \(=\operatorname{str}(\) simitr/100)
    outfile = root+"/"+root+"."+shortitr+outtag+".acf"
    \# check if the output file exists
    \# if so, proceed. (notify main out)
    \# otherwise, perform the ACF
    if os.path.isfile(outfile):
                print( outfile + "ьalreadyபexists.ьSkipping..." )
                continue
```

prefiles = [ str( root+"pre/"+root+"."+str(i).zfill(5)+"v" )
for i in range(simitr-2000,simitr) ]
localfiles = [ sd+f for f in timefiles ]
velfiles = prefiles + localfiles
global vels
t1 = time.time()
p = mp.Pool(processes=nprocs)

```
```

vels = np.asarray(p.map( importvel, velfiles ))
p.terminate()
t2 = time.time()
print('loadபtime பபபப: '' + str(t2-t1))

```
natoms \(=\) len(vels [0])
print("natoms பபபபபபப: \("\) + str(natoms))
global atomlist
if alst==-1 or len(alst)<1:
    atomlist \(=\) range (natoms)
else:
    atomlist = alst
print("atomlist பபபபப: ப")
print(np.asarray(atomlist))
global nfiles
nfiles \(=\) len(vels)
\(\mathrm{p}=\mathrm{mp}\). Pool (processes=nprocs)
acf \(=\) p.map(autocorr, range(nfiles))
p.terminate()
wrtr = open(outfile,"w")
for i in range(nfiles):
    wrtr.write ("\%7iப\%15.6e\n" \% (i, acf[i]/acf[0]) )
wrtr.close()

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[^0]:    ${ }^{1}$ Hartree-Fock (HF) treatments scale as $O\left(n^{4}\right)$ and Density Functional Theory (DFT) as $O\left(n^{3}\right)$ for $n$ basis functions.

